

Chapter 3

Exercise Solutions

E3.1

$$\beta = \frac{\alpha}{1 - \alpha}$$

$$\text{For } \alpha = 0.980, \beta = \frac{0.980}{1 - 0.980} = 49$$

$$\text{For } \alpha = 0.995, \beta = \frac{0.995}{1 - 0.995} = 199$$

$$49 \leq \beta \leq 199$$

E3.2

$$\alpha = \frac{\beta}{1 + \beta} = \frac{75}{76} = 0.9868$$

$$\alpha = \frac{125}{126} = 0.9921$$

E3.3

$$I_E = (1 + \beta)I_B$$

$$\text{So } (1 + \beta) = \frac{I_E}{I_B} = \frac{0.780}{0.00960} = 81.25 \Rightarrow \beta = 80.3$$

$$\alpha = \frac{\beta}{1 + \beta} = \frac{80.3}{81.3} \Rightarrow \alpha = 0.9877$$

$$I_C = \beta I_B = (80.3)(9.60 \mu\text{A}) \Rightarrow I_C = 0.771 \text{ mA}$$

E3.4

$$\beta = \frac{\alpha}{1 - \alpha} = \frac{0.990}{1 - 0.990} \Rightarrow \beta = 99$$

$$I_B = \frac{I_E}{(1 + \beta)} = \frac{2.150}{100} \Rightarrow I_B = 21.50 \mu\text{A}$$

$$I_C = \alpha I_E = (0.990)(2.150) \Rightarrow I_C = 2.13 \text{ mA}$$

E3.5

$$r_0 = \frac{V_A}{I_C} = \frac{150}{I_C}$$

$$I_C = 0.1 \text{ mA} \Rightarrow r_0 = 1.5 \text{ M}\Omega$$

$$I_C = 1.0 \text{ mA} \Rightarrow r_0 = 150 \text{ k}\Omega$$

$$I_C = 10 \text{ mA} \Rightarrow r_0 = 15 \text{ k}\Omega$$

E3.6

$$I_C = I_0 \left(1 + \frac{V_{CE}}{V_A}\right)$$

$$\text{At } V_{CE} = 1, I_C = 1$$

$$\text{a. } V_A = 75$$

$$I_C = 1 = I_0 \left(1 + \frac{1}{75}\right) \Rightarrow I_0 = 0.9868 \text{ mA}$$

$$\text{At } V_{CE} = 10, I_C = (0.9868) \left(1 + \frac{10}{75}\right) \Rightarrow$$

$$I_C = 1.12 \text{ mA}$$

$$\text{b. } V_A = 150$$

$$I_C = 1 = I_0 \left(1 + \frac{1}{150}\right) \Rightarrow I_0 = 0.9934 \text{ mA}$$

$$\text{At } V_{CE} = 10, I_C = (0.9934) \left(1 + \frac{10}{150}\right) \Rightarrow$$

$$I_C = 1.06 \text{ mA}$$

E3.7

$$BV_{CE0} = \frac{BV_{CB0}}{\sqrt{\beta}} = \frac{200}{\sqrt{120}} = 40.5 \text{ volts}$$

E3.8

$$BV_{CE0} = \frac{BV_{CB0}}{\sqrt{\beta}}$$

$$BV_{CB0} = (\sqrt{100})(30) = 139 \text{ V}$$

E3.9

$$\text{a. } V_i = 0.2 < V_{BE(\text{on})} \Rightarrow I_B = I_C = 0, V_o = 5 \text{ V}$$

$$P = 0$$

$$\text{b. } V_i = 3.6 \text{ Transistor is driven into saturation.}$$

$$I_B = \frac{3.6 - 0.7}{0.64} \Rightarrow I_B = 4.53 \text{ mA}$$

$$I_C = \frac{5 - V_{CE(\text{sat})}}{R_C} = \frac{5 - 0.2}{0.44} \Rightarrow I_C = 10.9 \text{ mA}$$

$$\text{Note that } \frac{I_C}{I_B} = \frac{10.9}{4.53} = 2.41 < \beta \text{ which shows}$$

that the transistor is indeed in saturation.

$$P = I_C V_{CE} + I_B V_{BE} = (10.9)(0.2) + (4.53)(0.7) \\ = 2.18 + 3.17$$

$$P = 5.35 \text{ mW}$$

E3.10

$$\text{For } V_{BC} = 0 \Rightarrow V_o = 0.7 \text{ V}$$

$$\text{Then } I_C = \frac{5 - 0.7}{0.44} \Rightarrow I_C = 9.77 \text{ mA}$$

$$\text{and } I_B = \frac{I_C}{\beta} = \frac{9.77}{50} = 0.195 \text{ mA}$$

$$V_i = I_B R_B + V_{BE(\text{on})} = (0.195)(0.64) + 0.7 \\ \Rightarrow V_i = 0.825 \text{ V}$$

$$\text{Power} = I_C V_{CE} + I_B V_{BE}$$

$$= (9.77)(0.7) + (0.195)(0.7)$$

$$\text{Power} = 6.98 \text{ mW}$$

E3.11

For $V_C = 4$ V and $I_{CQ} = 1.5$ mA

$$R_C = \frac{10 - 4}{1.5} \Rightarrow \underline{R_C = 4 \text{ k}\Omega}$$

$$I_E = \frac{-V_{BE(\text{on})} - (-10)}{R_E}$$

$$I_E = \left(\frac{101}{100}\right) I_C = 1.515 \text{ mA}$$

$$R_E = \frac{10 - 0.70}{1.515} \Rightarrow \underline{R_E = 6.14 \text{ k}\Omega}$$

E3.12

$$I_C = \frac{10 - V_C}{R_C} = \frac{10 - 6.34}{4} \Rightarrow I_C = 0.915 \text{ mA}$$

$$I_E = \frac{-V_{BE(\text{on})} - (-10)}{R_E} = \frac{10 - 0.7}{10} \Rightarrow$$

$$\underline{I_E = 0.930 \text{ mA}}$$

$$I_C = \alpha I_E \Rightarrow \alpha = \frac{I_C}{I_E} = \frac{0.915}{0.930} \Rightarrow \underline{\alpha = 0.9839}$$

$$I_B = I_E - I_C = 0.930 - 0.915 \Rightarrow \underline{I_B = 0.0150 \text{ mA}}$$

$$\beta = \frac{I_C}{I_B} = \frac{0.915}{0.015} \Rightarrow \underline{\beta = 61}$$

$$V_{CE} = V_C - V_E = 6.34 - (-0.70) \Rightarrow$$

$$\underline{V_{CE} = 7.04 \text{ V}}$$

E3.13

$$I_E = \frac{10 - V_{EB(\text{on})}}{R_E} = \frac{10 - 0.7}{8} \Rightarrow \underline{I_E = 1.16 \text{ mA}}$$

$$I_B = \frac{I_E}{(1 + \beta)} = \frac{1.16}{51} \Rightarrow \underline{I_B = 2.27 \mu\text{A}}$$

$$I_C = \frac{\beta}{1 + \beta} I_E = \frac{50}{51} (1.16) \Rightarrow \underline{I_C = 1.14 \text{ mA}}$$

$$V_C = I_C R_C - 10 = (1.14)(4) - 10 = -5.44$$

$$V_{EC} = 0.7 - (-5.44) \Rightarrow \underline{V_{EC} = 6.14 \text{ V}}$$

E3.14

$$I_E = \frac{V_{BB} - V_{EB(\text{on})}}{R_E}$$

$$\Rightarrow R_E = \frac{4 - 0.7}{1.0} \Rightarrow \underline{R_E = 3.3 \text{ k}\Omega}$$

$$I_C = \alpha I_E = (0.9920)(1.0) \Rightarrow \underline{I_C = 0.992 \text{ mA}}$$

$$I_B = I_E - I_C = 1.0 - 0.9920 \Rightarrow \underline{I_B = 0.0080 \text{ mA}}$$

$$V_{CB} = -V_{BC} = I_C R_C - V_{CC} = (0.992)(1) - 5$$

$$\Rightarrow \underline{V_{BC} = 4.01 \text{ V}}$$

E3.15

$$V_{BB} = I_B R_B + V_{BE(\text{on})} + I_E R_E$$

$$= I_B R_B + V_{BE(\text{on})} + (1 + \beta) I_B R_E$$

$$I_B = \frac{V_{BB} - V_{BE}}{R_B + (1 + \beta) R_E} = \frac{2 - 0.7}{10 + (76)(1)}$$

$$\Rightarrow \underline{I_B = 15.1 \mu\text{A}}$$

$$I_C = \beta I_B = (75)(15.1 \mu\text{A}) \Rightarrow \underline{I_C = 1.13 \text{ mA}}$$

$$I_E = (1 + \beta) I_B = (76)(15.1 \mu\text{A}) \Rightarrow \underline{I_E = 1.15 \text{ mA}}$$

$$V_{CE} = V_{CC} + V_{BB} - I_C R_C - I_E R_E$$

$$= 8 + 2 - (1.13)(2.5) - (1.15)(1)$$

$$\underline{V_{CE} = 6.03 \text{ V}}$$

E3.16

$$V_{CE} = 2.5 \Rightarrow V_E = 2.5 \text{ V} = I_E R_E$$

$$V_{BB} = I_B R_B + V_{BE(\text{on})} + V_E$$

$$I_B = \frac{V_{BB} - V_{BE(\text{on})} - V_E}{R_B} = \frac{5 - 0.7 - 2.5}{10}$$

$$I_B = 0.18 \text{ mA} \Rightarrow I_E = (101)(0.18)$$

$$\Rightarrow \underline{I_E = 18.18 \text{ mA}}$$

$$\text{So } R_E = \frac{2.5}{18.18} \Rightarrow \underline{R_E = 0.138 \text{ k}\Omega = 138 \Omega}$$

E3.17

$$V_{BB} = I_E R_E + V_{EB(\text{on})} + I_B R_B$$

$$I_E = 2.2 \text{ mA} \Rightarrow I_B = \frac{2.2}{51} = 0.0431 \text{ mA}$$

$$I_C = \left(\frac{\beta}{1 + \beta}\right) I_E = \left(\frac{50}{51}\right) (2.2) \Rightarrow \underline{I_C = 2.16 \text{ mA}}$$

$$V_{BB} = (2.2)(1) + 0.7 + (0.0431)(50)$$

$$\Rightarrow \underline{V_{BB} = 5.06 \text{ V}}$$

$$V_{EC} = 5 - I_E R_E = 5 - (2.2)(1)$$

$$\Rightarrow \underline{V_{EC} = 2.8 \text{ V}}$$

E3.18

$$(1) \quad 6 = I_B R_B + V_{BE(\text{on})} + I_E R_E$$

$$(2) \quad 5 = I_C R_C + V_{CE(\text{sat})} + I_E R_E$$

$$I_E = I_B + I_C$$

$$(1) \quad 6 = 10 I_B + 0.7 + (I_B + I_C)(1)$$

$$(2) \quad 5 = 4 I_C + 0.2 + (I_B + I_C)(1)$$

$$(1) \quad [5.3 = I_C + 11 I_B] \times 5 \Rightarrow 26.5 = 5 I_C + 55 I_B$$

$$(2) \quad 4.8 = 5 I_C + I_B \quad \underline{4.8 = 5 I_C + I_B}$$

$$21.7 = 54 I_B$$

$$\Rightarrow \underline{I_B = 0.402 \text{ mA}}$$

$$\text{From (1), } I_C = 5.3 - 11 I_B \Rightarrow \underline{I_C = 0.880 \text{ mA}}$$

$$\underline{I_E = 1.28 \text{ mA}}, \quad \underline{V_{CE} = V_{CE(\text{sat})} = 0.2 \text{ V}}$$

E3.19

$$\underline{V_{EC} = V_{EC(\text{sat})} = 0.2 \text{ V}}$$

$$I_C = \frac{-0.2 - (-5)}{R_C} = \frac{5 - 0.2}{10} \Rightarrow \underline{I_C = 0.48 \text{ mA}}$$

$$I_B = \frac{I_C}{\beta} = \frac{0.48}{2} = 0.24 = I_B$$

$$V_I + I_B R_B + V_{EB(\text{on})} = 0$$

$$\Rightarrow V_I = -(0.24)(20) - 0.7 \Rightarrow \underline{V_I = -5.5 \text{ V}}$$

E3.20

- a. $V_I = -4.5 \text{ V} \Rightarrow V_{BE} < V_{BE(\text{on})} \Rightarrow$ Transistor is cutoff. $I_B = I_C = I_E = 0$. $V_{CE} = 10 \text{ V}$
 b. $V_I = -3.5 \text{ V}$ Transistor is active.

$$V_I = I_B R_B + V_{BE(\text{on})} + I_E R_E - 5$$

$$5 - 3.5 = I_B(10) + 0.7 + (76)I_B(4)$$

$$I_B = \frac{5 - 3.5 - 0.7}{10 + (76)(4)} = 0.00255 \text{ mA}$$

$$\Rightarrow I_B = 2.55 \mu\text{A}$$

$$I_C = \beta I_B = (75)(2.55 \mu\text{A}) \Rightarrow I_C = 0.191 \text{ mA}$$

$$I_E = (1 + \beta)I_B = (76)(2.55 \mu\text{A})$$

$$\Rightarrow I_E = 0.194 \text{ mA}$$

$$V_{CE} = 10 - I_C R_C - I_E R_E$$

$$= 10 - (0.191)(2) - (0.194)(4)$$

$$\underline{V_{CE} = 8.84 \text{ V}}$$

- c. $V_I = +3.5 \text{ V}$ Transistor is in saturation.

$$(1) 3.5 = I_B R_B + V_{BE(\text{on})} + I_E R_E - 5$$

$$(2) 5 = I_C R_C + V_{CE(\text{sat})} + I_E R_E - 5$$

$$(3) I_E = I_B + I_C$$

$$(1) 3.5 + 5 - 0.7 = 10I_B + 4(I_B + I_C)$$

$$(2) 5 + 5 - 0.2 = 2I_C + 4(I_B + I_C)$$

$$(1) 7.8 = 14I_B + 4I_C$$

$$(2) 9.8 = 4I_B + 6I_C$$

$$3 \times (1) \Rightarrow 23.4 = 42I_B + 12I_C$$

$$2 \times (2) \Rightarrow 19.6 = 8I_B + 12I_C$$

$$3.8 = 34I_B$$

$$\Rightarrow I_B = 0.112 \text{ mA}$$

$$7.8 = 14(0.112) + 4I_C = 1.568 + 4I_C$$

$$\Rightarrow I_C = 1.56 \text{ mA}$$

$$\frac{I_C}{I_B} = 13.9 < \beta \Rightarrow \text{In saturation,}$$

$$I_E = I_B + I_C \Rightarrow I_E = 1.67 \text{ mA}$$

$$\underline{V_{CE} = V_{CE(\text{sat})} = 0.2}$$

E3.21

$$I_C(\text{sat}) = \frac{5 - 1.5 - 0.2}{R} = 15 \Rightarrow R = 0.220 \text{ k}\Omega$$

$$I_B = \frac{I_C}{20} = \frac{15}{20} = 0.75 \text{ mA} = \frac{5 - 0.8}{R_B}$$

or

$$\underline{R_B = 5.6 \text{ k}\Omega}$$

E3.22

- a. $V_1 = V_2 = 0$, $I_{B1} = I_{B2} = I_{C1} = I_{C2} = I_R = 0$
 $V_0 = 5 \text{ V}$

- b. $V_1 = 5 \text{ V}$, $V_2 = 0$, $I_{B2} = I_{C2} = 0$

$$I_{B1} = \frac{5 - 0.7}{0.95} \Rightarrow I_{B1} = 4.53 \text{ mA}$$

$$I_{C1} = \frac{5 - 0.2}{0.6} \Rightarrow I_{C1} = I_R = 8 \text{ mA}$$

$$V_0 = 0.2 \text{ V}$$

- c. $V_1 = V_2 = 5 \text{ V}$, $I_{B1} = I_{B2} = 4.53 \text{ mA}$

$$I_R = 8 \text{ mA}, I_{C1} = I_{C2} = 4 \text{ mA}, V_0 = 0.2 \text{ V}$$

E3.23

$$v_o = 5 - i_c R_C = 5 - \beta i_b R_C$$

and

$$i_b = \frac{V_{BB} + \Delta v_i - V_{BE(\text{on})}}{R_B}$$

Then

$$\Delta v_o = \frac{-\beta R_C \Delta v_i}{R_B}$$

or

$$\frac{\Delta v_o}{\Delta v_i} = \frac{-\beta R_C}{R_B}$$

$$\text{Let } \beta = 100, R_C = 5 \text{ k}\Omega, R_B = 100 \text{ k}\Omega$$

Then

$$\frac{\Delta v_o}{\Delta v_i} = \frac{-(100)(5)}{100} = -5$$

Want Q-point to be

$$v_o(Q - pt) = 2.5 = 5 - (100)I_{BQ}(5)$$

Then

$$I_{BQ} = 0.005 \text{ mA}, I_{BQ} = 0.005 = \frac{V_{BB} - 0.7}{100}$$

or

$$V_{BB} = 12 \text{ V}$$

$$\text{Also } I_{CQ} = \beta I_{BQ} = (100)(0.005)$$

Or

$$\underline{I_{CQ} = 0.5 \text{ mA}}$$

E3.24

- a. For $V_{CEQ} = 2.5 \text{ V} \Rightarrow I_{CQ} = \frac{5 - 2.5}{2}$
 $\Rightarrow I_{CQ} = 1.25 \text{ mA}$

$$I_{BQ} = \frac{I_{CQ}}{\beta} = \frac{1.25}{100} \Rightarrow I_{BQ} = 12.5 \mu\text{A}$$

$$\text{Then } R_B = \frac{5 - 0.7}{0.0125} \Rightarrow \underline{R_B = 344 \text{ k}\Omega}$$

- b. I_{BQ} is independent of β .

$$\text{For } V_{CEQ} = 1 \text{ V}, I_C = \frac{5 - 1}{2} = 2 \text{ mA}$$

$$\beta = \frac{I_C}{I_B} = \frac{2}{0.0125} \Rightarrow \beta = 160$$

$$\text{For } V_{CEQ} = 4 \text{ V, } I_C = \frac{5 - 4}{2} = 0.5 \text{ mA}$$

$$\beta = \frac{I_C}{I_B} = \frac{0.5}{0.0125} \Rightarrow \beta = 40$$

$$\text{So } 40 \leq \beta \leq 160$$

E3.25

$$I_{BQ} = \frac{5 - 0.7}{800} \Rightarrow I_{BQ} = 0.005375 \text{ mA}$$

$$\beta = 75 \Rightarrow I_{CQ} = (75)(0.005375) = 0.403 \text{ mA}$$

$$\beta = 150 \Rightarrow I_{CQ} = (150)(0.005375) = 0.806 \text{ mA}$$

Largest $I_{CQ} \Rightarrow$ Smallest V_{CEQ}

$$\beta = 150 \Rightarrow R_C = \frac{5 - 1}{0.806} = 4.96 \text{ k}\Omega$$

$$\beta = 75 \Rightarrow R_C = \frac{5 - 4}{0.403} = 2.48 \text{ k}\Omega$$

For a nominal $I_C = 0.604 \text{ mA}$ and $V_{CEQ} = 2.5$

$$R_C = \frac{5 - 2.5}{0.604} = 4.14 = R_C$$

For $I_{CQ} = 0.403$,

$$V_{CEQ} = 5 - (0.403)(4.14) = 3.33 \text{ V}$$

For $I_{CQ} = 0.806$,

$$V_{CEQ} = 5 - (0.806)(4.14) = 1.66 \text{ V}$$

So for $R_C = 4.14$, $1.66 \text{ V} \leq V_{CEQ} \leq 3.33 \text{ V}$

E3.26

$$\text{a. } R_{TH} = R_1 \parallel R_2 = 9 \parallel 2.25 \Rightarrow R_{TH} = 1.8 \text{ k}\Omega$$

$$V_{TH} = \left(\frac{R_2}{R_1 + R_2} \right) V_{CC} = \left(\frac{2.25}{9 + 2.25} \right) (5)$$

$$\Rightarrow V_{TH} = 1.0 \text{ V}$$

$$\text{b. } I_{BQ} = \frac{V_{TH} - V_{BE(on)}}{R_{TH} + (1 + \beta)R_E} = \frac{1 - 0.7}{1.8 + (151)(0.2)}$$

$$\Rightarrow I_{BQ} = 9.375 \mu\text{A}$$

$$I_{CQ} = \beta I_{BQ} = (150)(9.375 \mu\text{A})$$

$$\Rightarrow I_{CQ} = 1.41 \text{ mA}$$

$$I_{EQ} = (1 + \beta)I_{BQ} \Rightarrow I_{EQ} = 1.42 \text{ mA}$$

$$V_{CEQ} = 5 - I_{CQ}R_C - I_{EQ}R_E$$

$$= 5 - (1.41)(1) - (1.42)(0.2)$$

$$V_{CEQ} = 3.31 \text{ V}$$

c. For $\beta = 75$

$$I_{BQ} = \frac{1 - 0.7}{1.8 + (76)(0.2)} \Rightarrow I_{BQ} = 17.6 \mu\text{A}$$

$$I_{CQ} = \beta I_{BQ} = (75)(17.6 \mu\text{A})$$

$$\Rightarrow I_{CQ} = 1.32 \text{ mA}$$

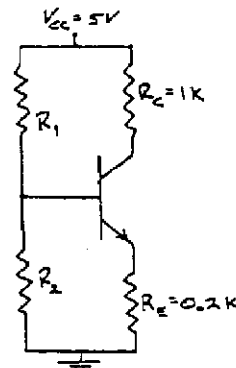
$$I_{EQ} = (1 + \beta)I_{BQ} = (76)(17.6 \mu\text{A})$$

$$\Rightarrow I_{EQ} = 1.34 \text{ mA}$$

$$V_{CEQ} = 5 - (1.32)(1) - (1.34)(0.2)$$

$$\Rightarrow V_{CEQ} = 3.41 \text{ V}$$

E3.27



$$R_1 + R_2 = 11.25 \text{ k}\Omega, \beta = 150$$

$$I_C \approx I_E, V_{CEQ} = 2.5 \text{ V}$$

$$\text{So } I_{CQ} \approx I_{EQ} = \frac{5 - 2.5}{1 + 0.2} = 2.081 \text{ mA}$$

$$I_{BQ} = \frac{I_{CQ}}{\beta} = \frac{2.08}{150} = 13.9 \mu\text{A}$$

$$I_{BQ} = \frac{V_{TH} - V_{BE(on)}}{R_{TH} + (1 + \beta)R_E}$$

$$\begin{aligned} 0.0139 &= \frac{\left(\frac{R_2}{R_1 + R_2} \right) V_{CC} - V_{BE(on)}}{\frac{R_1 R_2}{R_1 + R_2} + (1 + \beta)R_E} \\ &= \frac{\left(\frac{R_2}{11.25} \right) (5) - 0.7}{\frac{R_1 R_2}{(11.25)} + (151)(0.2)} \end{aligned}$$

$$R_2 = 11.25 - R_1, \text{ so}$$

$$0.0139[R_1(11.25 - R_1) + (151)(0.2)(11.25)]$$

$$= 5R_2 - (0.7)(11.25)$$

$$= 5(11.25 - R_1) - (0.7)(11.25)$$

$$0.156R_1 - 0.0139R_1^2 + 4.72 = 56.25 - 5R_1 - 7.875$$

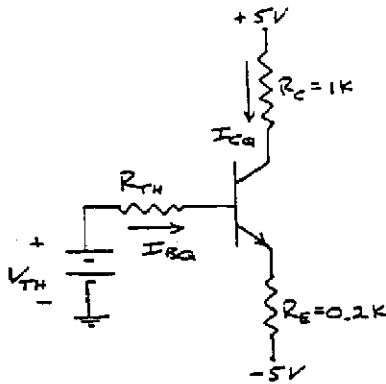
$$0.0139R_1^2 - 5.156R_1 + 43.66 = 0$$

$$R_1 = \frac{5.156 \pm \sqrt{(5.156)^2 - 4(0.0139)(43.66)}}{2(0.0139)}$$

$$\Rightarrow R_1 = 8.67 \text{ k}\Omega \text{ and } R_2 = 2.58 \text{ k}\Omega$$

E3.28

dc equivalent circuit



$$\beta = 150, R_{TH} = R_1 \parallel R_2,$$

$$V_{TH} = \left(\frac{R_2}{R_1 + R_2} \right) (10) - 5$$

$$I_{CQ} = \frac{5 - 0}{1} = 5 \text{ mA}$$

$$I_{BQ} = \frac{I_{CQ}}{\beta} = \frac{5}{150} = 0.0333 \text{ mA}$$

$$I_{BQ} = \frac{V_{TH} + 5 - 0.7}{R_{TH} + (1 + \beta)R_E}$$

$$\text{Set } R_{TH} = (0.1)(1 + \beta)R_E$$

$$I_{BQ} = \frac{V_{TH} + 4.3}{(1.1)(1 + \beta)R_E}$$

$$\Rightarrow 0.0333 = \frac{\left(\frac{R_2}{R_1 + R_2} \right) (10) - 5 + 4.3}{(1.1)(151)(0.2)}$$

$$(0.0333)(1.1)(151)(0.2) = \left(\frac{R_2}{R_1 + R_2} \right) (10) - 0.7$$

$$\text{So } \left(\frac{R_2}{R_1 + R_2} \right) = 0.1806$$

$$R_{TH} = \frac{R_1 R_2}{R_1 + R_2} = (0.1)(151)(0.2) = 3.02 \text{ k}\Omega$$

$$\text{Then } R_1(0.1806) = 3.02 \Rightarrow R_1 = 16.7 \text{ k}\Omega$$

$$R_2 = (0.1806)(16.7 + R_2) \Rightarrow 0.8194 R_2 = 3.02$$

$$\Rightarrow R_2 = 3.68 \text{ k}\Omega$$

E3.29

$$\beta = 120, V_{CEQ} = 5 \text{ V}$$

$$R_{TH} = R_1 \parallel R_2, V_{TH} = \left(\frac{R_2}{R_1 + R_2} \right) (10) - 5$$

$$I_{CQ} \approx I_{EQ}$$

$$\text{So } I_{CQ} = \frac{10 - V_{CEQ}}{R_C + R_E}$$

$$I_{CQ} = \frac{10 - 5}{1.2 + 0.3} \Rightarrow I_{CQ} = 3.33 \text{ mA}$$

$$I_{BQ} = \frac{I_{CQ}}{\beta} = \frac{3.33}{120} \Rightarrow I_{BQ} = 0.0278 \text{ mA}$$

$$I_{BQ} = \frac{V_{TH} + 5 - 0.7}{R_{TH} + (1 + \beta)R_E}$$

$$\text{Set } R_{TH} = (0.1)(1 + \beta)R_E$$

$$I_{BQ} = 0.0278 = \frac{\left(\frac{R_2}{R_1 + R_2} \right) (10) - 5 + 5 - 0.7}{(1.1)(121)(0.3)}$$

$$(0.0278)(1.1)(121)(0.3) = \left(\frac{R_2}{R_1 + R_2} \right) (10) - 0.7$$

$$\left(\frac{R_2}{R_1 + R_2} \right) = 0.181$$

$$R_{TH} = \frac{R_1 R_2}{R_1 + R_2} = R_1(0.181) = (0.1)(121)(0.3)$$

$$\Rightarrow R_1 = 20.1 \text{ k}\Omega$$

$$R_2 = (0.181)(20.1 + R_2) \Rightarrow 0.819 R_2 = 3.63 \text{ k}\Omega$$

$$\Rightarrow R_2 = 4.44 \text{ k}\Omega$$

E3.30

$$\text{a. } I_{CQ} = \left(\frac{\beta}{1 + \beta} \right) I_{EQ} = \left(\frac{100}{101} \right) (1) = 0.99 \text{ mA}$$

$$I_{BQ} = \frac{1 \text{ mA}}{1 + \beta} = \frac{1}{101} \Rightarrow 9.90 \mu\text{A}$$

$$V_B = -I_{BQ} R_B = -(0.0099)(50)$$

$$\Rightarrow V_B = -0.495 \text{ V}$$

$$V_{BE} = V_T \ln \left(\frac{I_{CQ}}{I_S} \right) = (0.026) \ln \left(\frac{0.99 \times 10^{-3}}{3 \times 10^{-14}} \right)$$

$$\Rightarrow V_{BE} = 0.630 \text{ V}$$

$$V_E = V_B - V_{BE} = -0.495 - 0.630$$

$$\Rightarrow V_E = -1.13 \text{ V}$$

$$V_C = 10 - (0.99)(5) = 5.05 \text{ V}$$

$$V_{CEQ} = V_C - V_E = 5.05 - (-1.13)$$

$$\Rightarrow V_{CEQ} = 6.18 \text{ V}$$

$$\text{b. } I_{EQ} = 1 \text{ mA}, I_B = \frac{1}{51} = 0.0196 \text{ mA}$$

$$V_B = -(0.0196)(50) = -0.98 \text{ V} = V_B$$

$$I_{CQ} = \left(\frac{50}{51} \right) (1) = 0.98 \text{ mA}$$

$$V_{BE} = (0.026) \ln \left(\frac{0.98 \times 10^{-3}}{3 \times 10^{-14}} \right) = 0.629 \text{ V}$$

$$V_E = -0.98 - 0.629 = -1.61$$

$$V_C = 10 - (0.98)(5) = 5.1 \text{ V}$$

$$V_{CEQ} = 5.1 - (-1.61) \Rightarrow V_{CEQ} = 6.71 \text{ V}$$

E3.31

$$I_B = \frac{I_Q}{1 + \beta} = \frac{I_Q}{121}, V_B = \left(\frac{I_Q}{121} \right) (20) = I_Q (0.165)$$

$$V_E = I_Q (0.165) + 0.7$$

$$I_{CQ} = \left(\frac{\beta}{1 + \beta} \right) I_{EQ} = \left(\frac{120}{121} \right) I_Q = (0.992) I_Q$$

$$V_C = I_{CQ} R_C - 5 = (0.992) I_Q (4) - 5$$

$$= 3.97 I_Q - 5$$

$$V_{ECQ} = V_E - V_C$$

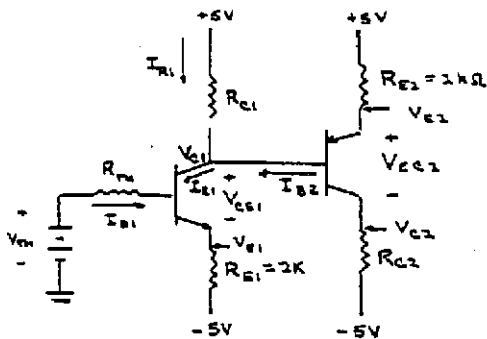
$$= [I_Q (0.165) + 0.7] - [3.97 I_Q - 5]$$

$$= -3.805 I_Q + 5.7$$

$$-3.805 I_Q + 5.7 = 3$$

$$\Rightarrow I_Q = 0.710 \text{ mA}$$

E3.32



$$R_{TH} = 50 \parallel 100 = 33.3 \text{ k}\Omega$$

$$V_{TH} = \left(\frac{50}{150} \right) (10) - 5 = -1.67 \text{ V}$$

$$I_{B1} = \frac{5 - 1.67 - 0.7}{33.3 + (101)(2)} = \frac{2.63}{235} = 11.2 \text{ }\mu\text{A}$$

$$I_{C1} = 1.12 \text{ mA}, I_{E1} = 1.13 \text{ mA}$$

$$V_{E1} = I_{E1} R_{E1} - 5 = (1.13)(2) - 5 = -2.74 \text{ V}$$

$$V_{CE1} = 3.25 \text{ V} \Rightarrow V_{C1} = 0.51 \text{ V}$$

$$\Rightarrow V_{E2} = 0.51 + 0.7 = 1.21 \text{ V}$$

$$I_{E2} = \frac{5 - 1.21}{2} = 1.90 \text{ mA} \Rightarrow I_{B2} = 18.8 \text{ }\mu\text{A}$$

$$I_{C2} = 1.88 \text{ mA}$$

$$I_{R1} = I_{C1} - I_{B2} = 1.12 - 0.0188 = 1.10 \text{ mA}$$

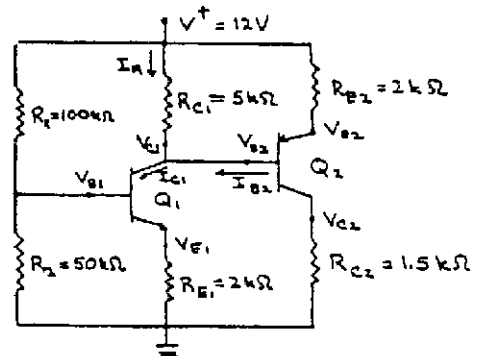
$$R_{C1} = \frac{5 - 0.51}{1.10} \Rightarrow R_{C1} = 4.08 \text{ k}\Omega$$

$$V_{EC2} = 2.5 \Rightarrow V_{C2} = V_{E2} - V_{EC2}$$

$$= 1.21 - 2.5 = -1.29$$

$$R_{C2} = \frac{-1.29 - (-5)}{1.88} \Rightarrow R_{C2} = 1.97 \text{ k}\Omega$$

E3.33



$$I_{B1} = \frac{V_{TH} - V_{BE(on)}}{R_{TH} + (1 + \beta) R_{E1}} = \frac{4 - 0.7}{33.3 + (101)(2)}$$

$$I_{B1} = 14 \text{ }\mu\text{A}, I_{C1} = 1.40 \text{ mA}, I_{E1} = 1.42 \text{ mA},$$

$$V_{B1} = 4 - (0.014)(33.3)$$

$$\Rightarrow V_{B1} = 3.53 \text{ V}, V_{E1} = 2.83 \text{ V}$$

$$I_R + I_{B2} = I_{C1}$$

$$\Rightarrow \frac{12 - V_{C1}}{5} + \frac{12 - (V_{C1} + 0.7)}{(101)(2)} = 1.40$$

$$\frac{12}{5} + \frac{(12 - 0.7)}{(101)(2)} - 1.40 = \frac{V_{C1}}{5} + \frac{V_{C1}}{(101)(2)}$$

$$2.4 + 0.0559 - 1.40 = V_{C1}(0.2 + 0.00495)$$

$$V_{C1} = V_{B2} = 5.15 \text{ V}, V_{E2} = 5.85$$

$$I_{E2} = \frac{12 - 5.85}{2} \Rightarrow I_{E2} = 3.08 \text{ mA}$$

$$I_{C2} = 3.04 \text{ mA}, I_{B2} = 30.4 \text{ }\mu\text{A}$$

$$V_{C2} = (3.04)(1.5) \Rightarrow V_{C2} = 4.56 \text{ V}$$

Chapter 3

Problem Solutions

3.1

$$(a) \beta_F = \frac{i_C}{i_B} = \frac{510}{6} \Rightarrow \beta_F = 85$$

$$\alpha_F = \frac{\beta_F}{1 + \beta_F} = \frac{85}{86} \Rightarrow \alpha_F = 0.9884$$

$$i_E = (1 + \beta_F)i_B = (86)(6) \Rightarrow i_E = 516 \mu A$$

$$(b) \beta_F = \frac{2.65}{0.050} \Rightarrow \beta_F = 53$$

$$\alpha_F = \frac{53}{54} \Rightarrow \alpha_F = 0.9815$$

$$i_E = (1 + \beta_F)i_B = (54)(0.050) \Rightarrow i_E = 2.70 \text{ mA}$$

3.2

(a)

For $\beta = 110$:

$$\alpha = \frac{\beta}{1 + \beta} = \frac{110}{111} = 0.99099$$

For $\beta = 180$:

$$\alpha = \frac{180}{181} = 0.99448$$

$$0.99099 < \alpha < 0.99448$$

$$(b) I_C = \beta I_B = 110(50 \mu A) \Rightarrow I_C = 5.50 \text{ mA}$$

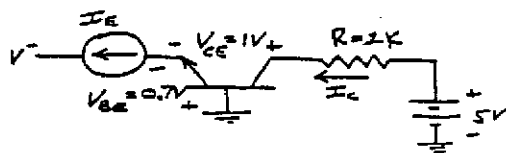
or

$$I_C = 180(50 \mu A) \Rightarrow I_C = 9.00 \text{ mA}$$

so

$$5.50 \leq I_C \leq 9.0 \text{ mA}$$

3.3



$$5 = I_C R + V_{CE} - V_{BE} = I_C(2) + 1 - 0.7$$

$$\Rightarrow I_C = 2.35 \text{ mA}$$

$$I_E = \frac{I_C}{\alpha} = \frac{2.35}{0.982} \Rightarrow I_E = 2.39 \text{ mA}$$

3.4

Same Figure as Problem 3.3

$$v_C = -0.7 + 2 = 1.3 \text{ V}; i_C = \frac{5 - 1.3}{2} \Rightarrow i_C = 1.85 \text{ mA}$$

$$\text{For } \beta_F = 120, i_B = \frac{i_C}{\beta_F} = \frac{1.85}{120} \Rightarrow i_B = 15.4 \mu A$$

$$i_E = \left(\frac{1 + \beta_F}{\beta_F} \right) i_C = \left(\frac{121}{120} \right) (1.85) \Rightarrow i_E = 1.865 \text{ mA}$$

3.5

$$\alpha = \frac{\beta}{1 + \beta} = \frac{60}{61} \Rightarrow \alpha = 0.9836$$

$$I_E = \frac{I_C}{\alpha} = \frac{0.85}{0.9836} \Rightarrow I_E = 0.864 \text{ mA}$$

$$I_B = \frac{I_C}{\beta} = \frac{0.85}{60} \Rightarrow I_B = 14.2 \mu A$$

3.6

$$i_E = I_S e^{v_{BE}/V_T} = (10^{-13}) e^{0.685/0.026} \Rightarrow i_E = 27.7 \text{ mA}$$

$$i_C = \left(\frac{90}{91} \right) (27.7) \Rightarrow i_C = 27.4 \text{ mA}$$

$$i_B = \frac{i_E}{1 + \beta} = \frac{27.7}{91} \Rightarrow i_B = 0.304 \text{ mA}$$

3.7

$$\text{Device 1: } i_E = I_{S1} e^{v_{BE}/V_T} \Rightarrow 0.5 \times 10^{-3} = I_{S1} e^{0.650/0.026}$$

So that

$$I_{S1} = 6.94 \times 10^{-15} \text{ A}$$

$$\text{Device 2: } 12.2 \times 10^{-3} = I_{S2} e^{0.650/0.026}$$

Or

$$I_{S2} = 1.69 \times 10^{-13} \text{ A}$$

$$\text{Ratio of areas} = \frac{I_{S2}}{I_{S1}} = \frac{1.69 \times 10^{-13}}{6.94 \times 10^{-15}} \Rightarrow \text{Ratio} = 24.4$$

3.8

$$(a) r_o = \frac{V_A}{I_C} = \frac{250}{1} \Rightarrow r_o = 250 \text{ k}\Omega$$

$$(b) r_o = \frac{V_A}{I_C} = \frac{250}{0.1} \Rightarrow r_o = 2.50 \text{ M}\Omega$$

3.9

$$BV_{CE0} = \frac{BV_{CB0}}{\sqrt{\beta}} = \frac{60}{\sqrt{100}}$$

$$BV_{CE0} = 12.9 \text{ V}$$

3.10

$$BV_{CE0} = \frac{BV_{CE0}}{\sqrt[3]{\beta}}$$

$$56 = \frac{220}{\sqrt[3]{\beta}} \Rightarrow \sqrt[3]{\beta} = \frac{220}{56} = 3.93$$

$$\beta = 60.6$$

3.11

$$BV_{CE0} = \frac{BV_{CE0}}{\sqrt[3]{\beta}}$$

$$BV_{CE0} = (BV_{CE0}) \sqrt[3]{\beta} = (50) \sqrt[3]{50}$$

$$BV_{CE0} = 184 \text{ V}$$

3.12

$$(a) I_B = \frac{12 - 0.7}{10} \Rightarrow I_B = 1.13 \text{ mA}$$

$$I_C = \left(\frac{75}{76}\right)(1.13) = 1.12 \text{ mA}$$

$$V_{CE} = 24 - (1.13)(10) - (1.12)R_C = 6$$

so that

$$R_C = 5.98 \text{ k}\Omega$$

$$(b) I_B = \frac{1}{76} = 0.0132 \text{ mA}$$

$$V_B = -I_B R_B = -(0.0132)(50) \Rightarrow V_B = -0.658 \text{ V}$$

$$I_C = \left(\frac{75}{76}\right)(1) = 0.987 \text{ mA}$$

$$R_C = \frac{5 - 2}{0.987} \Rightarrow R_C = 3.04 \text{ k}\Omega$$

$$c. I_B = \frac{8 - 0.7 - (-2)}{10 + (76)(10)} \Rightarrow I_B = 12.1 \mu\text{A}$$

$$I_C = 0.906 \text{ mA}$$

$$V_E = 0.7 + (0.0121)(10) - 2$$

$$V_E = -1.18 \text{ V}$$

$$V_C = I_C R_C - 8 = (0.906)(3) - 8$$

$$\Rightarrow V_C = -5.28 \text{ V}$$

$$V_{EC} = V_E - V_C = -1.18 - (-5.28)$$

$$\Rightarrow V_{EC} = 4.1 \text{ V}$$

$$d. 5 = (1 + \beta)I_B(10) + I_B(20) + 0.7 + (1 + \beta)I_B(2)$$

$$5 = I_B[760 + 20 + 152] + 0.7 \Rightarrow I_B = 4.61 \mu\text{A}$$

$$I_C = \beta I_B = (75)(4.61) \Rightarrow I_C = 0.346 \text{ mA}$$

$$V_C = 5 - (1 + \beta)I_B R_C = 5 - (76)(0.00461)(10)$$

$$\Rightarrow V_C = 1.50$$

3.13

(a) Figure P3.12(c)

$$8 = (76)I_B(10) + 0.7 + I_B(10) - 2$$

$$I_B = \frac{10 - 0.7}{10 + (76)(10)} = 0.01208 \text{ mA}$$

Then

$$I_C = (75)I_B \Rightarrow I_C = 0.906 \text{ mA}$$

$$\text{and } I_E = 0.918 \text{ mA}$$

$$V_{EC} = 8 - I_E R_E - I_C R_C - (-8)$$

$$V_{EC} = 16 - (0.918)(10) - (0.906)(R_C)$$

$$V_{EC} = 6.82 - (0.906)R_C$$

$$R_C = 3 \text{ k}\Omega \pm 5\% \Rightarrow 2.85 \leq R_C \leq 3.15 \text{ k}\Omega$$

Then

$$3.97 \leq V_{EC} \leq 4.24 \text{ V}$$

(b) Figure P3.12(d)

$$5 = (1 + \beta)I_B R_C + I_B(20) + 0.7 + (1 + \beta)I_B(2)$$

$$5 = (76)I_B R_C + I_B(20) + 0.7 + (76)I_B(2)$$

$$\text{Now } R_C = 10 \text{ k}\Omega \pm 5\% \Rightarrow 9.5 \leq R_C \leq 10.5 \text{ k}\Omega$$

$$\text{Then } 0.00443 \leq I_B \leq 0.00481 \text{ mA}$$

$$\text{And } V_C = 5 - (1 + \beta)I_B R_C$$

$$\text{So that } 1.46 \leq V_C \leq 1.53 \text{ V}$$

3.14

$$R_B = \frac{V_{BB} - V_{EB}}{I_B} = \frac{2.5 - 0.7}{0.015} \Rightarrow R_B = 120 \text{ k}\Omega$$

$$I_{CQ} = (70)(15 \mu\text{A}) \Rightarrow 1.05 \text{ mA}$$

$$R_C = \frac{V_{CC} - V_{ECQ}}{I_{CQ}} = \frac{5 - 2.5}{1.05} \Rightarrow R_C = 2.38 \text{ k}\Omega$$

3.15

$$a. V_B = -I_B R_B \Rightarrow I_B = \frac{-V_B}{R_B} = \frac{-(-1)}{500}$$

$$I_B = 2.0 \mu\text{A}$$

$$V_E = -1 - 0.7 = -1.7 \text{ V}$$

$$I_E = \frac{V_E - (-3)}{R_E} = \frac{-1.7 + 3}{4.8} = 0.2708 \text{ mA}$$

$$\frac{I_E}{I_B} = (1 + \beta) = \frac{0.2708}{0.002} = 135.4 \Rightarrow \beta = 134.4$$

$$\alpha = \frac{\beta}{1 + \beta} \Rightarrow \alpha = 0.9926$$

$$I_C = \beta I_B \Rightarrow I_C = 0.269 \text{ mA}$$

$$V_{CE} = 3 - V_E = 3 - (-1.7) \Rightarrow V_{CE} = 4.7 \text{ V}$$

$$b. \quad I_E = \frac{5 - 4}{2} \Rightarrow I_E = 0.5 \text{ mA}$$

$$4 = 0.7 + I_B R_B + (I_B + I_C) R_C - 5$$

$$I_B + I_C = I_E$$

$$4 = 0.7 + I_B(100) + (0.5)(8) - 5$$

$$I_B = 0.043 \Rightarrow \frac{I_E}{I_B} = (1 + \beta) = \frac{0.5}{0.043} = 11.63$$

$$\beta = 10.63, \quad \alpha = \frac{\beta}{1 + \beta} \Rightarrow \alpha = 0.9140$$

3.16

$$a. \quad V_B = 0 \Rightarrow \text{Cutoff} \Rightarrow I_E = 0, \quad V_C = 6 \text{ V}$$

$$b. \quad V_B = 1 \text{ V}, \quad I_E = \frac{1 - 0.7}{1} \Rightarrow I_E = 0.3 \text{ mA}$$

$$I_C \approx I_E \Rightarrow V_C = 6 - (0.3)(10) \Rightarrow V_C = 3 \text{ V}$$

$$c. \quad V_B = 2 \text{ V. Assume active-mode}$$

$$I_E = \frac{2 - 0.7}{1} = I_E = 1.3 \text{ mA} \approx I_C$$

$$V_C = 6 - (1.3)(10) = -7 \text{ V!}$$

Transistor in saturation

$$I_E = \frac{2 - 0.7}{1} \Rightarrow I_E = 1.3 \text{ mA}$$

$$V_E = 1.3 \text{ V}, \quad V_{CE}(\text{sat}) = 0.2 \text{ V}$$

$$V_C = V_E + V_{CE}(\text{sat}) = 1.3 + 0.2$$

$$\Rightarrow V_C = 1.5 \text{ V}$$

3.17

$$a. \quad V_{BB} = 0,$$

$$\text{Cutoff } V_0 = \left(\frac{R_L}{R_C + R_L} \right) V_{CC} = \left(\frac{10}{10 + 5} \right) (5)$$

$$V_0 = 3.33 \text{ V}$$

$$b. \quad V_{BB} = 1 \text{ V}$$

$$I_B = \frac{1 - 0.7}{50} \Rightarrow 6 \mu\text{A}$$

$$I_C = \beta I_B = (75)(6) \Rightarrow I_C = 0.45 \text{ mA}$$

$$\frac{5 - V_0}{5} = I_C + \frac{V_0}{10}$$

$$1 - 0.45 = V_0 \left(\frac{1}{5} + \frac{1}{10} \right) \Rightarrow V_0 = 1.83 \text{ V}$$

$$c. \quad \text{Transistor in saturation}$$

$$V_0 = V_{CE}(\text{sat}) = 0.2 \text{ V}$$

3.18

$$(a) \quad \beta_F = 100$$

$$(i) \quad I_Q = 0.1 \text{ mA} \quad I_C = \left(\frac{100}{101} \right) (0.1) = 0.0990 \text{ mA}$$

$$V_O = 5 - (0.099)(5) \Rightarrow V_O = 4.505 \text{ V}$$

$$(ii) \quad I_Q = 0.5 \text{ mA} \quad I_C = \left(\frac{100}{101} \right) (0.5) = 0.495 \text{ mA}$$

$$V_O = 5 - (0.495)(5) \Rightarrow V_O = 2.525 \text{ V}$$

$$(iii) \quad I_Q = 2 \text{ mA} \quad \text{Transistor is in saturation}$$

$$V_O = -V_{BE}(\text{sat}) + V_{CE}(\text{sat}) = -0.8 + 0.2 \Rightarrow$$

$$V_O = -0.6 \text{ V}$$

$$(b) \quad \beta_F = 150$$

$$(i) \quad I_Q = 0.1 \text{ mA} \quad I_C = \left(\frac{150}{151} \right) (0.1) = 0.09934 \text{ mA}$$

$$V_O = 5 - (0.09934)(5) \Rightarrow V_O = 4.503 \text{ V}$$

$$\% \text{ change} = \frac{4.503 - 4.505}{4.503} \times 100\% = -0.044\%$$

$$(ii) \quad I_Q = 0.5 \text{ mA} \quad I_C = \left(\frac{150}{151} \right) (0.5) = 0.4967 \text{ mA}$$

$$V_O = 5 - (0.4967)(5) \Rightarrow V_O = 2.517 \text{ V}$$

$$\% \text{ change} = \frac{2.517 - 2.525}{2.525} \times 100\% = -0.32\%$$

$$(iii) \quad I_Q = 2 \text{ mA} \quad \text{Transistor in saturation}$$

$$V_O = -0.6 \text{ V} \quad \text{No change}$$

3.19

$$I_E = \frac{V_B - 0.7}{1}$$

$$I_C = \left(\frac{\beta}{1 + \beta} \right) I_E = \left(\frac{50}{51} \right) (V_B - 0.7) = \frac{6 - V_C}{10}$$

$$\text{and } V_C = V_B$$

$$\left(\frac{50}{51} \right) (V_B - 0.7) = \frac{6 - V_B}{10}$$

$$9.80(V_B - 0.7) = 6 - V_B$$

$$10.80V_B = 6 + (0.7)(9.80) \Rightarrow V_B = 1.19 \text{ V}$$

$$I_E = \frac{1.19 - 0.7}{1} \Rightarrow I_E = 0.49 \text{ mA}$$

3.20

$$V_{CB} = 0.5 \text{ V} \Rightarrow V_O = 0.5 \text{ V}, \quad I_C = \frac{5 - 0.5}{5} = 0.90 \text{ mA}$$

$$I_Q = \left(\frac{101}{100} \right) (0.90) \Rightarrow I_Q = 0.909 \text{ mA}$$

3.21

$$I_E = \frac{10 - V_E}{10} = \frac{10 - 2}{10} \Rightarrow I_E = 0.80 \text{ mA}$$

$$V_B = V_E - 0.7 = 2 - 0.7 = 1.3 \text{ V}$$

$$I_B = \frac{V_B}{R_B} = \frac{1.3}{50} \Rightarrow I_B = 0.026 \text{ mA}$$

$$I_C = I_E - I_B = 0.80 - 0.026 \Rightarrow I_C = 0.774 \text{ mA}$$

$$\beta = \frac{I_C}{I_B} = \frac{0.774}{0.026} \Rightarrow \beta = 29.77$$

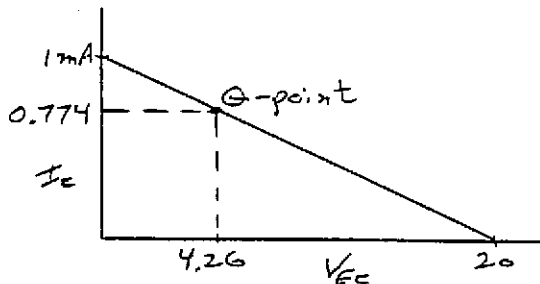
$$\alpha = \frac{\beta}{1 + \beta} = \frac{29.77}{30.77} \Rightarrow \alpha = 0.9673$$

$$V_{EC} = V_E - V_C = V_E - (I_C R_C - 10)$$

$$= 2 - [(0.774)(10) - 10]$$

$$V_{EC} = 4.26 \text{ V}$$

Load line developed assuming the V_B voltage can change and the R_B resistor is removed.



3.22

$$I_C = \left(\frac{50}{51}\right)(1) = 0.98 \text{ mA}$$

$$V_C = I_C R_C - 9 = (0.98)(4.7) - 9$$

$$\text{or } V_C = -4.39 \text{ V}$$

$$I_B = \frac{1}{51} = 0.0196 \text{ mA}$$

$$V_E = I_B R_B + V_{EB}(\text{on}) = (0.0196)(50) + 0.7$$

$$\text{or } V_E = 1.68 \text{ V}$$

3.23

$$I_C = \left(\frac{50}{51}\right)(0.5) = 0.49 \text{ mA}, I_B = \frac{0.5}{51} = 0.0098 \text{ mA}$$

$$V_E = I_B R_B + V_{EB}(\text{on}) = (0.0098)(50) + 0.7$$

$$\text{or } V_E = 1.19 \text{ V}$$

$$V_C = I_C R_C - 9 = (0.49)(4.7) - 9 = -6.70 \text{ V}$$

$$\text{Then } V_{EC} = V_E - V_C = 1.19 - (-6.7) = 7.89 \text{ V}$$

$$P_Q = I_C V_{EC} + I_B V_{EB} = (0.49)(7.89) + (0.0098)(0.7)$$

$$\text{or } P_Q = 3.87 \text{ mW}$$

$$\text{Power Supplied} = P_S = I_Q(9 - V_E) = (0.5)(9 - 1.19)$$

$$\text{Or } P_S = 3.91 \text{ mW}$$

3.24

$$\text{For } I_Q = 0, \text{ then } P_Q = 0$$

$$\text{For } I_Q = 0.5 \text{ mA}, I_C = \left(\frac{50}{51}\right)(0.5) = 0.49 \text{ mA}$$

$$I_B = \frac{0.5}{51} = 0.0098 \text{ mA}, V_B = 0.490 \text{ V}, V_E = 1.19 \text{ V}$$

$$V_C = (0.49)(4.7) - 9 = -6.70 \text{ V} \Rightarrow V_{EC} = 7.89 \text{ V}$$

$$P \approx I_C V_{EC} = (0.49)(7.89) \Rightarrow P = 3.87 \text{ mW}$$

For $I_Q = 1.0 \text{ mA}$, Using the same calculations as above, we find $P = 5.95 \text{ mW}$

$$\text{For } I_Q = 1.5 \text{ mA}, P = 6.26 \text{ mW}$$

$$\text{For } I_Q = 2 \text{ mA}, P = 4.80 \text{ mW}$$

$$\text{For } I_Q = 2.5 \text{ mA}, P = 1.57 \text{ mW}$$

For $I_Q = 3 \text{ mA}$, Transistor is in saturation.

$$0.7 + I_B(50) = 0.2 + I_C(4.7) - 9$$

$$I_E = I_Q = I_B + I_C \Rightarrow I_B = 3 - I_C$$

$$\text{Then, } 0.7 + (3 - I_C)(50) = 0.2 + I_C(4.7) - 9$$

Which yields $I_C = 2.916 \text{ mA}$ and $I_B = 0.084 \text{ mA}$

$$P = I_B V_{EB} + I_C V_{EC} = (0.084)(0.7) + (2.916)(0.2)$$

$$\text{or } P = 0.642 \text{ mW}$$

3.25

$$I_{E1} = I_{E2} = \frac{I}{2} \Rightarrow I_{E1} = I_{E2} = 0.5 \text{ mA}$$

$$I_{C1} = I_{C2} \approx 0.5 \text{ mA}$$

$$V_{C1} = V_{C2} = 5 - (0.5)(4) \Rightarrow V_{C1} = V_{C2} = 3 \text{ V}$$

3.26

$$\text{a. } I_{BQ} = \frac{V_{CC} - V_{BE}(\text{on})}{R_B}$$

$$I_{BQ} = \frac{I_{CQ}}{\beta} = \frac{2}{60} = 0.0333 \text{ mA}$$

$$R_B = \frac{24 - 0.7}{0.0333} \Rightarrow R_B = 699 \text{ k}\Omega$$

$$I_{CQ} = \frac{V_{CC} - V_{CEQ}}{R_C} \Rightarrow R_C = \frac{24 - 12}{2}$$

$$\Rightarrow R_C = 6 \text{ k}\Omega$$

$$\text{b. } I_{BQ} = \frac{V_{CC} - V_{BE}(\text{on})}{R_B} = \frac{24 - 0.7}{699}$$

$$= 0.0333 \text{ mA (Unchanged)}$$

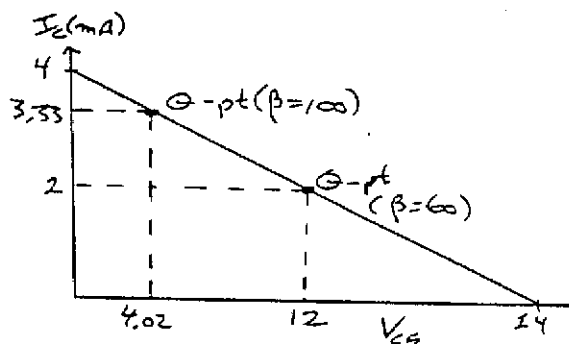
$$I_{CQ} = \beta I_{BQ} = (100)(0.0333)$$

$$\Rightarrow I_{CQ} = 3.33 \text{ mA}$$

$$V_{CEQ} = V_{CC} - I_{CQ} R_C = 24 - (3.33)(6)$$

$$\Rightarrow V_{CEQ} = 4.02 \text{ V}$$

$$(c) V_{CE} = V_{CC} - I_C R_C = 24 - I_C(6)$$



3.27

$$I_E = \frac{V_{EE} - V_{EB(on)}}{R_E} = \frac{9 - 0.7}{4}$$

$$\Rightarrow I_E = 2.075 \text{ mA}$$

$$I_C = \alpha I_E = (0.9920)(2.075)$$

$$\Rightarrow I_C = 2.06 \text{ mA}$$

$$V_{BC} + I_C R_C = V_{CC}$$

$$V_{BC} = 9 - (2.06)(2.2) \Rightarrow V_{BC} = 4.47 \text{ V}$$

3.28

$$I_{CQ} = \frac{V_{CC} - V_{CEQ}}{R_C} = \frac{12 - 6}{2.2} = 2.73 \text{ mA}$$

$$I_{BQ} = \frac{I_{CQ}}{\beta} = \frac{2.73}{30} \Rightarrow I_{BQ} = 0.091 \text{ mA}$$

$$I_{R2} = \frac{0.7 - (-12)}{100} = 0.127 \text{ mA}$$

$$I_{R1} = I_{R2} + I_{BQ} = 0.127 + 0.091 = 0.218 \text{ mA}$$

$$V_1 = I_{R1} R_1 + 0.7 = (0.218)(15) + 0.7$$

$$\Rightarrow V_1 = 3.97 \text{ V}$$

3.29

For $V_{CE} = 4.5$

$$I_{CQ} = \frac{5 - 4.5}{1} = 0.5 \text{ mA}$$

$$I_{BQ} = \frac{0.5}{25} = 0.02 \text{ mA}$$

$$I_{R2} = \frac{0.7 - (-5)}{100} = 0.057 \text{ mA}$$

$$I_{R1} = I_{R2} + I_{BQ} = 0.057 + 0.02 = 0.077 \text{ mA}$$

$$V_1 = I_{R1} R_1 + V_{BE(on)} = (0.077)(15) + 0.7$$

$$= 1.86 \text{ V}$$

For $V_{CE} = 1.0$

$$I_{CQ} = \frac{5 - 1}{1} = 4 \text{ mA}$$

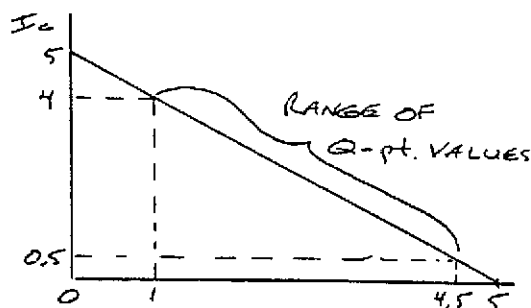
$$I_{BQ} = \frac{4}{25} = 0.16 \text{ mA}$$

$$I_{R2} = 0.057 \text{ mA}$$

$$I_{R1} = I_{R2} + I_{BQ} = 0.057 + 0.16 = 0.217 \text{ mA}$$

$$V_1 = (0.217)(15) + 0.7 \Rightarrow 3.96 \text{ V}$$

$$\text{So } 1.86 < V_1 < 3.96 \text{ V}$$



3.30

$$R_{TH} = R_1 \parallel R_2 = 33 \parallel 10 = 7.67 \text{ k}\Omega$$

$$V_{TH} = \left(\frac{R_2}{R_1 + R_2} \right) V_{CC} = \left(\frac{10}{10 + 33} \right) (18) = 4.19 \text{ V}$$

$$I_{BQ} = \frac{V_{TH} - V_{BE(on)}}{R_{TH} + (1 + \beta) R_E} = \frac{4.19 - 0.7}{7.67 + (51)(1)}$$

$$I_{BQ} = 0.0595 \text{ mA}$$

$$I_{CQ} = \beta I_{BQ} \Rightarrow I_{CQ} = 2.97 \text{ mA}$$

$$I_{EQ} = 3.03 \text{ mA}$$

$$V_{CEQ} = V_{CC} - I_{CQ} R_C - I_{EQ} R_E$$

$$= 18 - (2.97)(2.2) - (3.03)(1)$$

$$\Rightarrow V_{CEQ} = 8.44 \text{ V}$$

3.31

$$I_{CQ} = 12 \text{ mA}, V_{CEQ} = 9 \text{ V}, R_{TH} = 50 \text{ k}\Omega$$

$$\text{Also } I_B = \frac{12}{80} = 0.015 \text{ mA}$$

$$V_{TH} = I_{BQ} R_{TH} + V_{BE(on)} + (1 + \beta) I_{BQ} R_E$$

$$V_{TH} = \left(\frac{R_2}{R_1 + R_2} \right) V_{CC} = \frac{1}{R_1} \cdot R_{TH} \cdot V_{CC} = \frac{1}{R_1} (50)(18)$$

Then

$$\frac{1}{R_1} (50)(18) = (0.015)(50) + 0.7 + (81)(0.015)(1)$$

$$\text{or } R_1 = 338 \text{ k}\Omega. \text{ Then } \frac{338 R_2}{338 + R_2} = 50 \Rightarrow$$

$$R_2 = 58.7 \text{ k}\Omega \quad I_{EQ} = \left(\frac{81}{80} \right) (12) = 1.215 \text{ mA}$$

$$18 = I_{CQ} R_C + V_{CEQ} + I_{BQ} R_E$$

$$18 = (12) R_C + 9 + (1.215)(1) \Rightarrow R_C = 6.49 \text{ k}\Omega$$

3.32

$$R_{TH} = R_1 \parallel R_2 = 20 \parallel 15 = 8.57 \text{ k}\Omega$$

$$V_{TH} = \left(\frac{R_2}{R_1 + R_2} \right) V_{CC} = \left(\frac{15}{15 + 20} \right) (10) = 4.29 \text{ V}$$

$$V_{CC} = I_{BQ} R_E + V_{BE}(\text{on}) + \frac{I_{BQ}}{1 + \beta} R_{TH} + V_{TH}$$

$$10 = I_{BQ}(1) + 0.7 + I_{BQ} \left(\frac{8.57}{101} \right) + 4.29$$

Then

$$I_{BQ} = \frac{10 - 0.7 - 4.29}{1 + \frac{8.57}{101}} = \frac{5.01}{1.085} \Rightarrow I_{BQ} = 4.62 \text{ mA}$$

$$V_E = \frac{I_{BQ}}{1 + \beta} R_{TH} + V_{TH} = \left(\frac{4.62}{101} \right) (8.57) + 4.29$$

$$\text{or } V_E = 4.68 \text{ V}$$

3.33

$$\text{a. } R_{TH} = R_1 \parallel R_2 = 58 \parallel 42 = 24.36 \text{ k}\Omega$$

$$V_{TH} = \left(\frac{R_2}{R_1 + R_2} \right) V_{CC} = \left(\frac{42}{42 + 58} \right) (24) = 10.1 \text{ V}$$

$$I_{BQ} = \frac{V_{TH} - V_{BE}(\text{on})}{R_{TH} + (1 + \beta) R_E} = \frac{10.1 - 0.7}{24.36 + (126)(10)} = 0.00732 \text{ mA}$$

$$I_{BQ} = 0.00732 \text{ mA}$$

$$I_{CQ} = \beta I_{BQ} = (125)(0.00732)$$

$$\Rightarrow I_{CQ} = 0.915 \text{ mA}$$

$$I_{EQ} = 0.922 \Rightarrow V_{CEQ} = 24 - (0.922)(10)$$

$$\Rightarrow V_{CEQ} = 14.8 \text{ V}$$

b. Let

$$R_2 = 42 \text{ k}\Omega + 5\% = 44.1 \text{ k}\Omega$$

$$R_1 = 58 \text{ k}\Omega - 5\% = 55.1 \text{ k}\Omega$$

$$R_E = 10 \text{ k}\Omega - 5\% = 9.5 \text{ k}\Omega$$

$$R_{TH} = R_1 \parallel R_2 = 24.5 \text{ k}\Omega$$

$$V_{TH} = \left(\frac{44.1}{44.1 + 55.1} \right) (24) = 10.7 \text{ V}$$

$$I_{BQ} = \frac{10.7 - 0.7}{24.5 + (126)(9.5)} = 0.00819$$

$$I_{CQ} = 1.02 \text{ mA}, I_{EQ} = 1.03 \text{ mA}$$

$$V_{CEQ} = 24 - (1.03)(9.5) \Rightarrow V_{CEQ} = 14.2 \text{ V}$$

Let

$$R_2 = 42 \text{ k}\Omega - 5\% = 39.9 \text{ k}\Omega$$

$$R_1 = 58 \text{ k}\Omega + 5\% = 60.9 \text{ k}\Omega$$

$$R_E = 10 \text{ k}\Omega + 5\% = 10.5 \text{ k}\Omega$$

$$R_{TH} = R_1 \parallel R_2 = 24.1 \text{ k}\Omega$$

$$V_{TH} = \left(\frac{39.9}{39.9 + 60.9} \right) (24) = 9.5 \text{ V}$$

$$I_{BQ} = \frac{9.5 - 0.7}{24.1 + (126)(10.5)} = 0.00653 \text{ mA}$$

$$I_{CQ} = 0.817 \text{ mA}, I_{EQ} = 0.823 \text{ mA}$$

$$V_{CEQ} = 24 - (0.823)(10.5) \Rightarrow V_{CEQ} = 15.4 \text{ V}$$

$$\text{So } 0.817 \leq I_{CQ} \leq 1.02 \text{ mA and}$$

$$14.2 \leq V_{CEQ} \leq 15.4 \text{ V.}$$

3.34

$$\text{a. } R_{TH} = R_1 \parallel R_2 = 25 \parallel 8 = 6.06 \text{ k}\Omega$$

$$V_{TH} = \left(\frac{R_2}{R_1 + R_2} \right) V_{CC} = \left(\frac{8}{8 + 25} \right) (24) = 5.82 \text{ V}$$

$$I_{BQ} = \frac{V_{TH} - V_{BE}(\text{on})}{R_{TH} + (1 + \beta) R_E} = \frac{5.82 - 0.7}{6.06 + (76)(1)} = 0.0624 \text{ mA}$$

$$I_{CQ} = 4.68 \text{ mA}$$

$$I_{EQ} = 4.74$$

$$V_{CEQ} = V_{CC} - I_{CQ} R_C - I_{EQ} R_E$$

$$= 24 - (4.68)(3) - (4.74)(1)$$

$$V_{CEQ} = 5.22 \text{ V}$$

$$\text{b. } I_{BQ} = \frac{5.82 - 0.7}{6.06 + (151)(1)} \Rightarrow I_{BQ} = 0.0326 \text{ mA}$$

$$I_{CQ} = 4.89 \text{ mA}$$

$$I_{EQ} = 4.92$$

$$V_{CEQ} = 24 - (4.89)(3) - (4.92)(1)$$

$$V_{CEQ} = 4.41 \text{ V}$$

3.35

$$\text{(a) } I_{CQ} \cong I_{BQ} = 0.4 \text{ mA}$$

$$R_C = \frac{3}{0.4} \Rightarrow R_C = 7.5 \text{ k}\Omega; R_E = \frac{3}{0.4} \Rightarrow R_E = 7.5 \text{ k}\Omega$$

$$R_1 + R_2 \cong \frac{9}{(0.2)(0.4)} = 112.5 \text{ k}\Omega$$

$$V_{TH} = \left(\frac{R_2}{R_1 + R_2} \right) V_{CC} = I_{BQ} R_{TH} + V_{BE}(\text{on}) + (1 + \beta) I_{BQ} R_E$$

$$R_{TH} = \frac{R_1 R_2}{R_1 + R_2} = \frac{(112.5 - R_2) R_2}{112.5}$$

$$I_{BQ} = \frac{0.4}{100} = 0.004 \text{ mA}$$

$$R_2 \left(\frac{9}{112.5} \right) = (0.004) \left[\frac{(112.5 - R_2) R_2}{112.5} \right] + 0.7 + (101)(0.004)(7.5)$$

We obtain

$$R_2(0.08) = 0.004 R_2 - 3.56 \times 10^{-3} R_2^2 + 3.73$$

From this quadratic, we find

$$R_2 = 48 \text{ k}\Omega \Rightarrow R_1 = 64.5 \text{ k}\Omega$$

(b) Standard resistor values:

Set $R_F = R_C = 7.5 \text{ k}\Omega$ and

$R_1 = 62 \text{ k}\Omega$, $R_2 = 47 \text{ k}\Omega$

Now $R_{TH} = R_1 \parallel R_2 = 62 \parallel 47 = 26.7 \text{ k}\Omega$

$$V_{TH} = \left(\frac{R_2}{R_1 + R_2} \right) V_{CC} = \left(\frac{47}{47 + 62} \right) (9) = 3.88 \text{ V}$$

$$V_{TH} = I_{BQ} R_{TH} + V_{BE}(\text{on}) + (1 + \beta) I_{BQ} R_F$$

So

$$I_{BQ} = \frac{3.88 - 0.7}{26.7 + (101)(7.5)} = 0.00406 \text{ mA}$$

Then

$$I_{CQ} = 0.406 \text{ mA}$$

$$V_{RC} = V_{RE} = (0.406)(7.5) = 3.05 \text{ V}$$

3.36

a. $R_{TH} = R_1 \parallel R_2 = 12 \parallel 2 = 1.71 \text{ k}\Omega = R_{TH}$

$$V_{TH} = \left(\frac{R_2}{R_1 + R_2} \right) (10) - 5 = \left(\frac{2}{12 + 2} \right) (10) - 5 = -3.57 \text{ V} = V_{TH}$$

b.

$$I_{BQ} = \frac{V_{TH} - V_{BE}(\text{on}) - (-5)}{R_{TH} + (1 + \beta) R_E} = \frac{-3.57 - 0.7 + 5}{1.71 + (101)(0.5)} = \frac{0.73}{52.2}$$

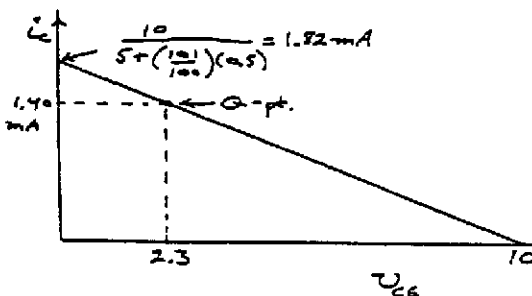
$$\Rightarrow I_{BQ} = 0.0140 \text{ mA}$$

$$I_{CQ} = 1.40 \text{ mA}, I_{EQ} = 1.41 \text{ mA}$$

$$V_{CEQ} = 10 - I_{CQ} R_C - I_{EQ} R_E = 10 - (1.40)(5) - (1.41)(0.5) = 2.30 \text{ V}$$

$$V_{CEQ} = 2.30 \text{ V}$$

c.



d. For

$$R_2 = 2 \text{ k}\Omega + 5\% = 2.1 \text{ k}\Omega$$

$$R_1 = 12 \text{ k}\Omega - 5\% = 11.4 \text{ k}\Omega$$

$$R_E = 0.5 \text{ k}\Omega - 5\% = 0.475 \text{ k}\Omega$$

$$R_{TH} = R_1 \parallel R_2 = 1.77 \text{ k}\Omega$$

$$V_{TH} = \left(\frac{2.1}{2.1 + 1.4} \right) (10) - 5 = -3.44 \text{ V}$$

$$I_{BQ} = \frac{-3.44 - 0.7 + 5}{1.77 + (101)(0.475)} = \frac{0.86}{49.7} = 0.0173 \text{ mA}$$

$$I_{CQ} = 1.73 \text{ mA}, I_{EQ} = 1.75 \text{ mA}$$

$$\text{For } R_C = 5 \text{ k}\Omega + 5\% = 5.25 \text{ k}\Omega$$

$$V_{CEQ} = 10 - (1.73)(5.25) - (1.75)(0.475)$$

$$\Rightarrow V_{CEQ} = 0.0863 \text{ V (Saturation)}$$

For

$$R_2 = 2 \text{ k}\Omega - 5\% = 1.9 \text{ k}\Omega$$

$$R_1 = 12 \text{ k}\Omega + 5\% = 12.6 \text{ k}\Omega$$

$$R_E = 0.5 \text{ k}\Omega + 5\% = 0.525 \text{ k}\Omega$$

$$R_{TH} = R_1 \parallel R_2 = 1.65 \text{ k}\Omega$$

$$V_{TH} = \left(\frac{1.9}{12.6 + 1.9} \right) (10) - 5 = -3.69 \text{ V}$$

$$I_{BQ} = \frac{-3.69 - 0.7 + 5}{1.65 + (101)(0.525)} = \frac{0.61}{54.7} = 0.0112 \text{ mA}$$

$$I_{CQ} = 1.12 \text{ mA}, I_{EQ} = 1.13 \text{ mA}$$

$$\text{For } R_C = 5 \text{ k}\Omega - 5\% = 4.75 \text{ k}\Omega$$

$$V_{CEQ} = 10 - (1.12)(4.75) - (1.13)(0.525)$$

$$\Rightarrow V_{CEQ} = 4.09 \text{ V}$$

$$\text{So } 1.12 \leq I_{CQ} \leq 1.73 \text{ mA and } 0.0863 \leq V_{CEQ} \leq 4.09 \text{ V.}$$

Saturation

3.37

$$R_{TH} = R_1 \parallel R_2 = 9 \parallel 1 = 0.90 \text{ k}\Omega$$

$$V_{TH} = \left(\frac{R_2}{R_1 + R_2} \right) (-12) = \left(\frac{1}{1 + 9} \right) (-12) = -1.2 \text{ V}$$

$$I_{EQ} R_E + V_{EB}(\text{on}) + I_{BQ} R_{TH} + V_{TH} = 0$$

$$I_{BQ} = \frac{-V_{TH} - V_{EB}(\text{on})}{R_{TH} + (1 + \beta) R_E} = \frac{1.2 - 0.7}{0.90 + (76)(0.1)}$$

$$I_{BQ} = 0.0588, I_{CQ} = 4.41 \text{ mA}$$

$$I_{EQ} = 4.47 \text{ mA}$$

$$\text{Center of load line} \Rightarrow V_{ECQ} = 6 \text{ V}$$

$$I_{EQ} R_E + V_{ECQ} + I_{CQ} R_C - 12 = 0$$

$$(4.47)(0.1) + 6 + (4.41) R_C = 12$$

$$\Rightarrow R_C = 1.26 \text{ k}\Omega$$

3.38

$$(a) R_{TH} = (0.1)(1 + \beta)R_E = (0.1)(101)(0.5) = 5.05 \text{ k}\Omega$$

$$V_{TH} = \frac{1}{R_1} \cdot R_{TH} \cdot V_{CC} = I_{BQ}R_{TH} + V_{BE(on)} + (1 + \beta)I_{BQ}R_E$$

$$I_{BQ} = \frac{I_{CQ}}{\beta} = \frac{0.8}{100} = 0.008 \text{ mA}$$

Then

$$\frac{1}{R_1}(5.05)(10) = (0.008)(5.05) + 0.7 + (101)(0.008)(0.5)$$

or

$$R_1 = 44.1 \text{ k}\Omega, \quad \frac{44.1R_2}{44.1 + R_2} = 5.05 \Rightarrow R_2 = 5.70 \text{ k}\Omega$$

$$\text{Now } I_{EQ} = \left(\frac{101}{100}\right)(0.8) = 0.808 \text{ mA}$$

$$V_{CC} = I_{CQ}R_C + V_{CEQ} + I_{EQ}R_E$$

$$10 = (0.8)R_C + 5 + (0.808)(0.5)$$

$$R_C = 5.75 \text{ k}\Omega$$

(b) For $75 \leq \beta \leq 150$

$$V_{TH} = \left(\frac{R_2}{R_1 + R_2}\right)(V_{CC}) = \left(\frac{5.7}{5.7 + 44.1}\right)(10) = 1.145 \text{ V}$$

$$V_{TH} = I_{BQ}R_{TH} + V_{BE(on)} + (1 + \beta)I_{BQ}R_E$$

$$\text{For } \beta = 75, \quad I_{BQ} = \frac{1.145 - 0.7}{5.05 + (76)(0.5)} = 0.0103 \text{ mA}$$

$$\text{Then } I_{CQ} = (75)(0.0103) = 0.775 \text{ mA}$$

$$\text{For } \beta = 150, \quad I_{BQ} = \frac{1.145 - 0.7}{5.05 + (151)(0.5)} = 0.00552 \text{ mA}$$

$$\text{Then } I_{CQ} = 0.829 \text{ mA}$$

$$\% \text{ Change} = \frac{\Delta I_{CQ}}{I_{CQ}} = \frac{0.829 - 0.775}{0.80} \times 100\% \Rightarrow$$

$$\% \text{ Change} = 6.75\%$$

(c) For $R_E = 1 \text{ k}\Omega$

$$R_{TH} = (0.1)(101)(1) = 10.1 \text{ k}\Omega$$

$$V_{TH} = \frac{1}{R_1} \cdot R_{TH} \cdot V_{CC} = \frac{1}{R_1}(10.1)(10) = (0.008)(10.1) + 0.7 + (101)(0.008)(1)$$

$$\text{which yields } R_1 = 63.6 \text{ k}\Omega$$

$$\text{And } \frac{63.6R_2}{63.6 + R_2} = 10.1 \Rightarrow R_2 = 12.0 \text{ k}\Omega$$

$$\text{Now } V_{TH} = \left(\frac{R_2}{R_1 + R_2}\right)(V_{CC}) = \left(\frac{12}{12 + 63.6}\right)(10) = 1.587 \text{ V}$$

$$\text{For } \beta = 75, \quad I_{BQ} = \frac{1.587 - 0.7}{10.1 + (76)(1)} = 0.0103 \text{ mA}$$

$$\text{So } I_{CQ} = 0.773 \text{ mA}$$

$$\text{For } \beta = 150, \quad I_{BQ} = \frac{1.587 - 0.7}{10.1 + (151)(1)} = 0.00551 \text{ mA}$$

$$\text{Then } I_{CQ} = 0.826 \text{ mA}$$

$$\% \text{ Change} = \frac{\Delta I_{CQ}}{I_{CQ}} = \frac{0.826 - 0.773}{0.8} \times 100\% \Rightarrow$$

$$\% \text{ Change} = 6.63\%$$

3.39

$$V_{CC} = I_{CQ}(R_C + R_E) + V_{CEQ}$$

$$10 = (0.8)(R_C + R_E) + 5 \Rightarrow R_C + R_E = 6.25 \text{ k}\Omega$$

$$\text{Let } R_E = 1 \text{ k}\Omega$$

$$\text{Then, for bias stable } R_{TH} = (0.1)(121)(1) = 12.1 \text{ k}\Omega$$

$$I_{BQ} = \frac{0.8}{120} = 0.00667 \text{ mA}$$

$$\frac{1}{R_1}(12.1)(10) = (0.00667)(12.1) + 0.7 + (121)(0.00667)(1)$$

$$\text{So } R_1 = 76.2 \text{ k}\Omega \text{ and } \frac{76.2R_2}{76.2 + R_2} = 12.1 \Rightarrow$$

$$R_2 = 14.4 \text{ k}\Omega$$

$$\text{Then } I_R = \frac{10}{76.2 + 14.4} = 0.110 \text{ mA}$$

This is close to the design specification.

3.40

$$I_{CQ} \approx I_{EQ} \Rightarrow V_{CEQ} = V_{CC} - I_{CQ}(R_C + R_E)$$

$$6 = 12 - I_{CQ}(2 + 0.2)$$

$$I_{CQ} = 2.73 \text{ mA}, \quad I_{BQ} = 0.0218 \text{ mA}$$

$$V_{CEQ} = 6 \text{ V}$$

$$V_{TH} = I_{BQ}R_{TH} + V_{BE(on)} + (1 + \beta)I_{BQ}R_E - 6$$

$$V_{TH} = \left(\frac{R_2}{R_1 + R_2}\right)(12) - 6, \quad R_{TH} = R_1 \parallel R_2$$

Bias stable \Rightarrow

$$R_{TH} = (0.1)(1 + \beta)R_E = (0.1)(126)(0.2) = 2.52 \text{ k}\Omega$$

$$V_{TH} = \left(\frac{1}{R_1}\right)(R_{TH})(12) - 6$$

$$\frac{1}{R_1}(2.52)(12) - 6 = (0.0218)(2.52) + 0.7$$

$$+ (126)(0.0218)(0.2) - 6$$

$$\frac{1}{R_1}(30.24) = 0.7549 + 0.5494$$

$$R_1 = 23.2 \text{ k}\Omega, \quad \frac{23.2R_2}{23.2 + R_2} = 2.52$$

$$R_2 = 2.83 \text{ k}\Omega$$

3.41

$$\begin{aligned}
 a. \quad I_{CQ} &= 1 \text{ mA}, \quad I_{EQ} = \left(\frac{80}{81}\right)(1) = 1.01 \text{ mA} \\
 V_{CEQ} &= 12 - (1)(2) - (1.01)(0.2) \Rightarrow \underline{V_{CEQ} = 9.80 \text{ V}} \\
 I_{BQ} &= \frac{1}{80} = 0.0125 \text{ mA} \\
 R_{TH} &= +(0.1)(1 + \beta)R_E = (0.1)(81)(0.2) = 1.62 \text{ k}\Omega \\
 V_{TH} &= \left(\frac{R_2}{R_1 + R_2}\right)(12) - 6 = \frac{1}{R_1}(R_{TH})(12) - 6 \\
 &= \frac{1}{R_1}(19.44) - 6 \\
 V_{TH} &= I_{BQ}R_{TH} + V_{BE(on)} + (1 + \beta)I_{BQ}R_E - 6 \\
 \frac{1}{R_1}(19.44) - 6 &= (0.0125)(1.62) + 0.7 \\
 &\quad + (81)(0.0125)(0.2) - 6 \\
 \frac{1}{R_1}(19.44) &= 0.923 \\
 \underline{R_1} &= 21.1 \text{ k}\Omega, \quad \frac{21.1 R_2}{21.1 + R_2} = 1.62 \\
 \underline{R_2} &= 1.75 \text{ k}\Omega
 \end{aligned}$$

b.

$$\begin{aligned}
 R_1 &= 22.2 \text{ k}\Omega \text{ or } R_1 = 20.0 \text{ k}\Omega \\
 R_2 &= 1.84 \text{ k}\Omega \text{ or } R_2 = 1.66 \text{ k}\Omega \\
 R_E &= 0.21 \text{ k}\Omega \text{ or } R_E = 0.19 \text{ k}\Omega \\
 R_C &= 2.1 \text{ k}\Omega \text{ or } R_C = 1.9 \text{ k}\Omega \\
 R_2(\text{max}), R_1(\text{min}), R_E(\text{min}) \\
 R_{TH} &= (1.84) \parallel (20.0) = 1.685 \text{ k}\Omega
 \end{aligned}$$

$$\begin{aligned}
 V_{TH} &= \left(\frac{1.84}{1.84 + 20.0}\right)(12) - 6 = -4.99 \text{ V} \\
 I_{BQ} &= \frac{-4.99 - 0.7 - (-6)}{1.685 + (81)(0.19)} = \frac{0.31}{17.08} = 0.0182 \text{ mA} \\
 \underline{I_{CQ}} &= 1.45 \text{ mA}
 \end{aligned}$$

For max. $R_C \Rightarrow$

$$\begin{aligned}
 V_{CE} &= 12 - (1.45)(2.1) - (1.47)(0.19) \\
 \underline{V_{CE}} &= 8.68 \text{ V}
 \end{aligned}$$

$$\begin{aligned}
 R_2(\text{min}), R_1(\text{max}), R_E(\text{max}) \\
 R_{TH} &= (1.66) \parallel (22.2) = 1.547 \text{ k}\Omega \\
 V_{TH} &= \left(\frac{1.66}{1.66 + 22.2}\right)(12) - 6 = -5.165 \text{ V} \\
 I_{BQ} &= \frac{-5.165 - 0.7 + 6}{1.547 + (81)(0.21)} = \frac{0.135}{18.56} = 0.00727 \text{ mA}
 \end{aligned}$$

For min. $R_C \Rightarrow \underline{I_{CQ}} = 0.582 \text{ mA}, I_E = 0.589$

$$V_{CEQ} = 12 - (0.582)(1.9) - (0.589)(0.21)$$

$$\underline{V_{CEQ}} = 10.77 \text{ V}$$

So $0.582 \leq I_C \leq 1.45 \text{ mA}$

$$8.68 \leq V_{CEQ} \leq 10.77 \text{ V}$$

3.42

$$\begin{aligned}
 V_{CEQ} &\equiv V_{CC} - I_{CQ}(R_C + R_E) \\
 5 &= 12 - 3(R_C + R_E) \Rightarrow R_C + R_E = 2.33 \text{ k}\Omega \\
 \text{Let } R_E &= 0.33 \text{ k}\Omega \text{ and } R_C = 2 \text{ k}\Omega \\
 \text{Nominal value of } \beta &= 100 \\
 R_{TH} &= (0.1)(1 + \beta)R_E = (0.1)(101)(0.33) = 3.33 \text{ k}\Omega \\
 I_{BQ} &= \frac{3}{100} = 0.03 \text{ mA} \\
 V_{TH} &= \frac{1}{R_1} \cdot R_{TH} \cdot (12) - 6 = \frac{1}{R_1}(3.33)(12) - 6 \\
 \text{Then} \\
 V_{TH} &= I_{BQ}R_{TH} + V_{BE(on)} + (1 + \beta)I_{BQ}R_E - 6 \\
 \frac{1}{R_1}(3.33)(12) - 6 &= (0.03)(3.33) + 0.7 + (101)(0.03)(0.33) - 6 \\
 \text{which yields } R_1 &= 22.2 \text{ k}\Omega \text{ and } R_2 = 3.92 \text{ k}\Omega
 \end{aligned}$$

Now

$$V_{TH} = \left(\frac{R_2}{R_1 + R_2}\right)(12) - 6 = \left(\frac{3.92}{3.92 + 22.2}\right)(12) - 6$$

or

$$V_{TH} = -4.20 \text{ V}$$

For $\beta = 75$,

$$\begin{aligned}
 V_{TH} &= I_{BQ}R_{TH} + V_{BE(on)} + (1 + \beta)I_{BQ}R_E - 6 \\
 I_{BQ} &= \frac{V_{TH} + 6 - 0.7}{R_{TH} + (1 + \beta)R_E} = \frac{-4.2 + 6 - 0.7}{3.33 + (76)(0.33)} \\
 &= 0.0387 \text{ mA} \Rightarrow \underline{I_C = 2.90 \text{ mA}}
 \end{aligned}$$

For $\beta = 150$,

$$I_{BQ} = \frac{-4.2 + 6 - 0.7}{3.33 + (151)(0.33)} = 0.0207 \text{ mA}$$

Then

$$\underline{I_C = 3.10 \text{ mA}}$$

Specifications are met.

3.43

$$\begin{aligned}
 R_{TH} &= R_1 \parallel R_2 = 3 \parallel 12 = 2.4 \text{ k}\Omega \\
 V_{TH} &= \left(\frac{R_2}{R_1 + R_2}\right)V_{CC} = \left(\frac{12}{12 + 3}\right)(20) = 16 \text{ V}
 \end{aligned}$$

(a) For $\beta = 75$

$$\begin{aligned}
 20 &= (1 + \beta)I_{BQ}R_E + V_{BE(on)} + I_{BQ}R_{TH} + V_{TH} \\
 20 - 0.7 - 16 &= I_{BQ}[(76)(2) + 2.4]
 \end{aligned}$$

So

$$I_{BQ} = 0.0214 \text{ mA}, \quad I_{CQ} = 1.60 \text{ mA}, \quad I_{EQ} = 1.62 \text{ mA}$$

$$V_{ECQ} = 20 - (1.6)(1) - (1.62)(2)$$

or

$$\underline{V_{ECQ}} = 15.16 \text{ V}$$

(b) For $\beta = 100$, we find

$$I_{BQ} = 0.0161 \text{ mA}, \quad I_{CQ} = 1.61 \text{ mA}, \quad V_{ECQ} = 15.13 \text{ V}$$

3.44

$$I_{CQ} = 4.8 \text{ mA} \rightarrow I_{EQ} = 4.84 \text{ mA}$$

$$V_{CEQ} = V_{CC} - I_{CQ}R_C - I_{EQ}R_E$$

$$6 = 18 - (4.8)(2) - (4.84)R_E \Rightarrow \underline{R_E = 0.496 \text{ k}\Omega}$$

$$R_{TH} = (0.1)(1 + \beta)R_E = (0.1)(121)(0.496) = 6.0 \text{ k}\Omega$$

$$V_{TH} = I_{BQ}R_{TH} + V_{BE(on)} + (1 + \beta)I_{BQ}R_E$$

$$I_{BQ} = 0.040 \text{ mA}$$

$$V_{TH} = \frac{1}{R_1} \cdot R_{TH} \cdot V_{CC} = \frac{1}{R_1}(6.0)(18)$$

$$\frac{1}{R_1}(6.0)(18) = (0.04)(6.0) + 0.70$$

$$+ (121)(0.04)(0.496)$$

$$\frac{1}{R_1}(108) = 3.34$$

$$\underline{R_1 = 32.3 \text{ k}\Omega}, \quad \frac{32.3 R_2}{32.3 + R_2} = 6.0$$

$$\underline{R_2 = 7.37 \text{ k}\Omega}$$

3.45

For nominal $\beta = 70$

$$I_{BQ} = \frac{2}{70} = 0.0286 \text{ mA} \rightarrow I_{EQ} = 2.03 \text{ mA}$$

$$V_{CEQ} = V_{CC} - I_{CQ}R_C - I_{EQ}R_E$$

$$10 = 20 - (2)(4) - (2.03)R_E \Rightarrow \underline{R_E = 0.985 \text{ k}\Omega}$$

$$R_{TH} = (0.1)(1 + \beta)R_E = (0.1)(71)(0.985) = 6.99 \text{ k}\Omega$$

$$V_{TH} = I_{BQ}R_{TH} + V_{BE(on)} + I_{EQ}R_E$$

$$\frac{1}{R_1} \cdot R_{TH} \cdot V_{CC} = I_{BQ}R_{TH} + V_{BE(on)} + I_{EQ}R_E$$

$$\frac{1}{R_1}(6.99)(20) = (0.0286)(6.99) + 0.70$$

$$+ (2.03)(0.985)$$

$$\frac{1}{R_1}(139.8) = 2.90$$

$$\underline{R_1 = 48.2 \text{ k}\Omega}, \quad \frac{48.2 R_2}{48.2 + R_2} = 6.99$$

$$\underline{R_2 = 8.18 \text{ k}\Omega}$$

Check: For $\beta = 50$

$$V_{TH} = \left(\frac{8.18}{8.18 + 48.2} \right) (20) = 2.90$$

$$I_{BQ} = \frac{V_{TH} - V_{BE(on)}}{R_{TH} + (1 + \beta)R_E} = \frac{2.90 - 0.7}{6.99 + (51)(0.985)} = 0.0384 \text{ mA}$$

$$\underline{I_{CQ} = 1.92 \text{ mA}}$$

For $\beta = 90$

$$I_{BQ} = \frac{2.90 - 0.7}{6.99 + (91)(0.985)} = 0.0228 \text{ mA}$$

$$\underline{I_{CQ} = 2.05 \text{ mA}}$$

Design criterion is satisfied.

3.46

$$I_{CQ} = 1 \text{ mA} \rightarrow I_{EQ} = 1.02 \text{ mA}$$

$$V_{CEQ} = V_{CC} - I_{CQ}R_C - I_{EQ}R_E$$

$$5 = 15 - (1)(5) - (1.02)R_E \Rightarrow \underline{R_E = 4.90 \text{ k}\Omega}$$

Bias stable:

$$R_{TH} = (0.1)(1 + \beta)R_E = (0.1)(61)(4.9) = 29.9 \text{ k}\Omega$$

$$I_{BQ} = \frac{1}{60} = 0.0167 \text{ mA}$$

$$V_{TH} = \frac{1}{R_1} \cdot R_{TH} \cdot V_{CC} = I_{BQ}R_{TH} + V_{BE(on)} + I_{EQ}R_E$$

$$\frac{1}{R_1}(29.9)(15) = (0.0167)(29.9) + 0.70$$

$$+ (1.02)(4.90)$$

$$\frac{1}{R_1}(448.5) = 6.197$$

$$\underline{R_1 = 72.4 \text{ k}\Omega}, \quad \frac{72.4 R_2}{72.4 + R_2} = 29.9$$

$$\underline{R_2 = 50.9 \text{ k}\Omega}$$

Check: For $\beta = 45$

$$V_{TH} = \left(\frac{50.9}{50.9 + 72.4} \right) (15) = 6.19 \text{ V}$$

$$I_{BQ} = \frac{V_{TH} - V_{BE(on)}}{R_{TH} + (1 + \beta)R_E} = \frac{6.19 - 0.7}{29.9 + (46)(4.90)} = 0.0215 \text{ mA}$$

$$\underline{I_{CQ} = 0.968 \text{ mA}}, \quad \frac{\Delta I_C}{I_C} = 3.2\%$$

Check: For $\beta = 75$

$$I_{BQ} = \frac{6.19 - 0.7}{29.9 + (76)(4.90)} = 0.0136 \text{ mA}$$

$$\underline{I_{CQ} = 1.02 \text{ mA}}, \quad \frac{\Delta I_C}{I_C} = 2.0\%$$

Design criterion is satisfied.

3.47

$$(a) V_{CC} = I_{CQ}(R_C + R_E) + V_{CEQ}$$

$$3 = (0.1)(5R_E + R_E) + 1.4 \Rightarrow \underline{R_E = 2.67 \text{ k}\Omega}$$

$$\underline{R_C = 13.3 \text{ k}\Omega}, \quad I_{BQ} = \frac{100}{120} = 0.833 \mu\text{A}$$

$$R_{TH} = (0.1)(1 + \beta)R_E = (0.1)(121)(2.67) = 32.3 \text{ k}\Omega$$

$$V_{TH} = \frac{1}{R_1} \cdot R_{TH} \cdot V_{CC} = \frac{1}{R_1}(32.3)(3)$$

$$= I_{BQ}R_{TH} + V_{BE(on)} + (1 + \beta)I_{BQ}R_E$$

$$= (0.000833)(32.3) + 0.7 + (121)(0.000833)(2.67)$$

$$\text{which gives } \underline{R_1 = 97.3 \text{ k}\Omega}, \text{ and } \underline{R_2 = 48.4 \text{ k}\Omega}$$

$$(b) I_R = \frac{3}{R_1 + R_2} = \frac{3}{97.3 + 48.4} \Rightarrow 20.6 \mu A$$

$$I_{CQ} = 100 \mu A$$

$$P = (I_{CQ} + I_R)V_{CC} = (100 + 20.6)(3)$$

or

$$P = 362 \mu W$$

3.48

$$I_E = \frac{5 - V_E}{R_E} = \frac{5}{3} = 1.67 \text{ mA}$$

$$R_{TH} = R_1 \parallel R_2 = (0.1)(1 + \beta)R_E$$

$$= (0.1)(101)(3) = 30.3 \text{ k}\Omega$$

$$V_{TH} = \left(\frac{R_2}{R_1 + R_2} \right)(4) - 2 = \frac{1}{R_1} \cdot R_{TH} \cdot (4) - 2$$

$$I_{BQ} = \frac{I_{EQ}}{1 + \beta} = 0.0165 \text{ mA}$$

$$5 = I_{BQ}R_E + V_{EB(ON)} + I_{BQ}R_{TH} + V_{TH}$$

$$5 = (1.67)(3) + 0.7 + (0.0165)(30.3)$$

$$+ \frac{1}{R_1}(30.3)(4) - 2$$

$$0.80 = \frac{1}{R_1}(30.3)(4) \Rightarrow R_1 = 152 \text{ k}\Omega$$

$$\frac{152R_2}{152 + R_2} = 30.3 \Rightarrow R_2 = 37.8 \text{ k}\Omega$$

3.49

$$a. R_{TH} = R_1 \parallel R_2 = 10 \parallel 20 \Rightarrow R_{TH} = 6.67 \text{ k}\Omega$$

$$V_{TH} = \left(\frac{R_2}{R_1 + R_2} \right)(10) - 5 = \left(\frac{20}{20 + 10} \right)(10) - 5$$

$$\Rightarrow V_{TH} = 1.67 \text{ V}$$

$$b. 10 = (1 + \beta)I_{BQ}R_E + V_{EB(ON)} + I_{BQ}R_{TH} + V_{TH}$$

$$I_{BQ} = \frac{10 - 0.7 - 1.67}{6.67 + (61)(2)} = \frac{7.63}{128.7}$$

$$\Rightarrow I_{BQ} = 0.0593 \text{ mA}$$

$$I_{CQ} = 3.65 \text{ mA}, I_{EQ} = 3.62 \text{ mA}$$

$$V_E = 10 - I_{EQ}R_E = 10 - (3.62)(2)$$

$$V_E = 2.76 \text{ V}$$

$$V_C = I_{CQ}R_C - 10 = (3.56)(2.2) - 10$$

$$V_C = -2.17 \text{ V}$$

3.50

$$V^+ - V^- = I_{CQ}(R_C + R_E) + V_{ECQ}$$

$$20 = (0.5)(R_C + R_E) + 8 \Rightarrow (R_C + R_E) = 24 \text{ k}\Omega$$

$$\text{Let } R_E = 10 \text{ k}\Omega \text{ then } R_C = 14 \text{ k}\Omega$$

$$\text{Let } \beta = 60 \text{ from previous problem.}$$

$$R_{TH} = (0.1)(1 + \beta)R_E = (0.1)(61)(10)$$

$$\text{Or } R_{TH} = 61 \text{ k}\Omega$$

$$I_{BQ} = \frac{0.5}{60} = 0.00833 \text{ mA}$$

$$V_{TH} = \left(\frac{R_2}{R_1 + R_2} \right)(10) - 5 = \frac{1}{R_1} \cdot R_{TH} \cdot 10 - 5$$

Now

$$10 = (1 + \beta)I_{BQ}R_E + V_{EB(ON)} + I_{BQ}R_{TH} + V_{TH}$$

$$10 = (61)(0.00833)(10) + 0.7 + (0.00833)(61)$$

$$+ \frac{1}{R_1}(61)(10) - 5$$

$$\text{Then } R_1 = 70.0 \text{ k}\Omega \text{ and } R_2 = 474 \text{ k}\Omega$$

$$I_R = \frac{10}{R_1 + R_2} = \frac{10}{70 + 474} \Rightarrow 18.4 \mu A$$

So the 40 μA current limit is met.

3.51

$$a. R_{TH} = R_1 \parallel R_2 = 35 \parallel 20 \Rightarrow R_{TH} = 12.7 \text{ k}\Omega$$

$$V_{TH} = \left(\frac{R_2}{R_1 + R_2} \right)(7) - 5 = \left(\frac{20}{20 + 35} \right)(7) - 5$$

$$\Rightarrow V_{TH} = -2.45 \text{ V}$$

b.

$$I_{BQ} = \frac{V_{TH} - V_{BE(ON)} - (-10)}{R_{TH} + (1 + \beta)R_E}$$

$$= \frac{-2.45 - 0.7 + 10}{12.7 + (76)(0.5)}$$

$$\Rightarrow I_{BQ} = 0.135 \text{ mA}$$

$$I_{CQ} = 10.1 \text{ mA}, I_{EQ} = 10.3 \text{ mA}$$

$$V_{CEQ} = 20 - I_{CQ}R_C - I_{EQ}R_E$$

$$= 20 - (10.1)(0.8) - (10.3)(0.5)$$

$$V_{CEQ} = 6.77 \text{ V}$$

c.

$$R_2 = 20 + 5\% = 21 \text{ k}\Omega$$

$$R_1 = 35 - 5\% = 33.25 \text{ k}\Omega$$

$$R_E = 0.5 - 5\% = 0.475 \text{ k}\Omega$$

$$R_{TH} = R_1 \parallel R_2 = 21 \parallel 33.25 = 12.9 \text{ k}\Omega$$

$$V_{TH} = \left(\frac{R_2}{R_1 + R_2} \right)(7) - 5$$

$$= \left(\frac{21}{21 + 33.25} \right)(7) - 5 = -2.29 \text{ V}$$

$$I_{BQ} = \frac{-2.29 - 0.7 - (-10)}{12.9 + (76)(0.475)} = 0.143 \text{ mA}$$

$$I_{CQ} = 10.7 \text{ mA}, I_{EQ} = 10.9 \text{ mA}$$

$$\text{For } R_C = 0.8 + 5\% = 0.84 \text{ k}\Omega$$

$$V_{CEQ} = 20 - (10.7)(0.84) - (10.9)(0.475)$$

$$\Rightarrow V_{CEQ} = 5.83 \text{ V}$$

For $R_C = 0.8 - 5\% = 0.76 \text{ k}\Omega$

$$V_{CEQ} = 20 - (10.7)(0.76) - (10.9)(0.475)$$

$$\Rightarrow V_{CEQ} = 6.69 \text{ V}$$

$$R_1 = 20 - 5\% = 19 \text{ k}\Omega$$

$$R_2 = 35 + 5\% = 36.75 \text{ k}\Omega$$

$$R_E = 0.5 + 5\% = 0.525 \text{ k}\Omega$$

$$R_{TH} = R_1 || R_2 = 19 || 36.75 = 12.5 \text{ k}\Omega$$

$$V_{TH} = \left(\frac{19}{19 + 36.75} \right) (7) - 5 = -2.61 \text{ V}$$

$$I_{BQ} = \frac{-2.61 - 0.7 - (-10)}{12.5 + (76)(0.525)} = 0.128 \text{ mA}$$

$$I_{CQ} = 9.58 \text{ mA}, \quad I_{EQ} = 9.70 \text{ mA}$$

For $R_C = 0.84 \text{ k}\Omega$

$$V_{CEQ} = 20 - (9.58)(0.84) - (9.70)(0.525)$$

$$\Rightarrow V_{CEQ} = 6.86 \text{ V}$$

For $R_C = 0.76 \text{ k}\Omega$

$$V_{CEQ} = 20 - (9.58)(0.76) - (9.70)(0.525)$$

$$\Rightarrow V_{CEQ} = 7.63 \text{ V}$$

$$\text{So } 9.58 \leq I_{CQ} \leq 10.7 \text{ mA}$$

and

$$5.83 \leq V_{CEQ} \leq 7.63 \text{ V}$$

3.52

$$\text{a. } R_{TH} = 500 \text{ k}\Omega || 500 \text{ k}\Omega || 70 \text{ k}\Omega = 250 \text{ k}\Omega || 70 \text{ k}\Omega$$

$$\Rightarrow R_{TH} = 54.7 \text{ k}\Omega$$

$$\frac{5 - V_{TH}}{500} + \frac{3 - V_{TH}}{500} = \frac{V_{TH} - (-5)}{70}$$

$$\frac{5}{500} + \frac{3}{500} - \frac{5}{70} = V_{TH} \left(\frac{1}{500} + \frac{1}{500} + \frac{1}{70} \right)$$

$$-0.0554 = V_{TH}(0.0183)$$

$$V_{TH} = -3.03 \text{ V}$$

b.

$$I_{BQ} = \frac{V_{TH} - V_{BE(\text{on})} - (-5)}{R_{TH} + (1 + \beta)R_E}$$

$$= \frac{-3.03 - 0.7 + 5}{54.7 + (101)(5)}$$

$$I_{BQ} = 0.00227 \text{ mA}$$

$$I_{CQ} = 0.227 \text{ mA}, \quad I_{EQ} = 0.229$$

$$V_{CEQ} = 20 - (0.227)(50) - (0.229)(5)$$

$$V_{CEQ} = 7.51 \text{ V}$$

3.53

$$R_{TH} = 30 || 60 || 20 \Rightarrow R_{TH} = 10 \text{ k}\Omega$$

$$\frac{5 - V_{TH}}{30} + \frac{5 - V_{TH}}{60} = \frac{V_{TH}}{20}$$

$$\left(\frac{5}{30} + \frac{5}{60} \right) = V_{TH} \left(\frac{1}{30} + \frac{1}{60} + \frac{1}{20} \right)$$

$$V_{TH} = 2.5 \text{ V}$$

For $\beta = 100$

$$I_{BQ} = \frac{V_{TH} - V_{BE(\text{on})} - (-5)}{R_{TH} + (1 + \beta)R_E}$$

$$= \frac{2.5 - 0.7 + 5}{10 + (101)(0.2)}$$

$$I_{BQ} = 0.225 \text{ mA}$$

$$I_{CQ} = 22.5 \text{ mA}, \quad I_{EQ} = 22.7 \text{ mA}$$

$$V_{CEQ} = 15 - (22.5)(0.5) - (22.7)(0.2)$$

$$V_{CEQ} = -0.79 \text{ V} \Rightarrow \text{In saturation}$$

$$\Rightarrow V_{CEQ} = 0.2 \text{ V}$$

$$V_E = V_{TH} - I_{BQ}R_{TH} - V_{BE(\text{on})}$$

$$= 2.5 - (0.225)(10) - 0.7$$

$$V_E = -0.45 \text{ V} \Rightarrow V_C = -0.45 + 0.2 = -0.25 \text{ V}$$

$$I_{CQ} = \frac{10 - (-0.25)}{0.5} \Rightarrow I_{CQ} = 20.5 \text{ mA}$$

3.54

$$R_{TH} = R_1 || R_2 = 100 || 40 = 28.6 \text{ k}\Omega$$

$$V_{TH} = \left(\frac{R_2}{R_1 + R_2} \right) (10) = \left(\frac{40}{40 + 100} \right) (10) = 2.86 \text{ V}$$

$$I_{B1} = \frac{V_{TH} - V_{BE(\text{on})}}{R_{TH} + (1 + \beta)R_{E1}} = \frac{2.86 - 0.7}{28.6 + (121)(1)}$$

$$I_{B1} = 0.0144 \text{ mA}$$

$$I_{C1} = 1.73 \text{ mA}, \quad I_{E1} = 1.75 \text{ mA}$$

$$\frac{10 - V_{B2}}{3} = I_{C1} + I_{B2}$$

$$I_{E2} = \frac{V_{B2} - V_{BE(\text{on})} - (-10)}{5}$$

$$\frac{10 - V_{B2}}{3} = I_{C1} + \frac{V_{B2} - 0.7 + 10}{(121)(5)}$$

$$\frac{10}{3} - 1.73 - \frac{9.3}{605} = V_{B2} \left(\frac{1}{3} + \frac{1}{(121)(5)} \right)$$

$$1.59 = V_{B2}(0.335) \Rightarrow V_{B2} = 4.75 \text{ V}$$

$$I_{E2} = \frac{4.75 - 0.7 - (-10)}{5} \Rightarrow I_{E2} = 2.81 \text{ mA}$$

$$I_{B2} = 0.0232 \text{ mA}$$

$$I_{C2} = 2.79 \text{ mA}$$

$$V_{CEQ1} = 4.75 - (1.75)(1) \Rightarrow V_{CEQ1} = 3.0 \text{ V}$$

$$V_{CEQ2} = 10 - (4.75 - 0.7) \Rightarrow V_{CEQ2} = 5.95 \text{ V}$$

3.55

$$V_{E1} = -0.7$$

$$I_{R1} = \frac{-0.7 - (-5)}{20} = 0.215 \text{ mA}$$

$$V_{E2} = -0.7 - 0.7 = -1.4$$

$$I_{E2} = \frac{-1.4 - (-5)}{1} \Rightarrow I_{E2} = 3.6 \text{ mA}$$

$$I_{B2} = 0.0444 \text{ mA}$$

$$I_{C1} = 3.56 \text{ mA}$$

$$I_{E1} = I_{R1} + I_{B2} = 0.215 + 0.0444$$

$$I_{E1} = 0.259 \text{ mA}$$

$$I_{B1} = 0.00320 \text{ mA}$$

$$I_{C1} = 0.256 \text{ mA}$$

3.56

$$\text{Current through } V^- \text{ source} = I_{E1} + I_{E2} \text{ and}$$

$$I_{E1} = I_{E2} = (1 + \beta)I_{B1} = (51)(8.26) \mu\text{A}$$

$$\text{So total current} = 2(51)(8.26) \mu\text{A} = 843 \mu\text{A}$$

$$P^- = I \cdot |V^-| = (0.843)(5) \Rightarrow P^- = 4.22 \text{ mW}$$

(From V^- source)

$$\text{From Example 3.15, } I_Q = 0.413 \text{ mA}$$

$$\text{So } I_{C0} = \left(\frac{50}{51}\right)(0.413) = 0.405 \text{ mA}$$

$$P^+ = I \cdot V^+ = (0.405)(5) \Rightarrow P^+ = 2.03 \text{ mW}$$

(From V^+ source)

3.57

$$R_{TH} = R_1 \parallel R_2 = 50 \parallel 100 = 33.3 \text{ k}\Omega$$

$$V_{TH} = \left(\frac{R_2}{R_1 + R_2}\right)(10) - 5$$

$$= \left(\frac{100}{100 + 50}\right)(10) - 5 = 1.67 \text{ V}$$

$$5 = I_{E1}R_{E1} + V_{EB}(\text{on}) + I_{B1}R_{TH} + V_{TH}$$

$$I_{E1} = \left(\frac{101}{100}\right)(0.8) = 0.808 \text{ mA}$$

$$I_{B1} = 0.008 \text{ mA}$$

$$5 = (0.808)R_{E1} + 0.7 + (0.008)(33.3) + 1.67$$

$$R_{E1} = 2.93 \text{ k}\Omega$$

$$V_{E1} = 5 - (0.808)(2.93) = 2.63 \text{ V}$$

$$V_{C1} = V_{E1} - V_{ECQ1} = 2.63 - 3.5 = -0.87 \text{ V}$$

$$V_{E2} = -0.87 - 0.70 = -1.57 \text{ V}$$

$$I_{E2} = \frac{-1.57 - (-5)}{R_{E2}} = 0.808 \Rightarrow R_{E2} = 4.25 \text{ k}\Omega$$

$$V_{CEQ2} = 4 \Rightarrow V_{C2} = -1.57 + 4 = 2.43 \text{ V}$$

$$R_{C2} = \frac{5 - 2.43}{0.8} \Rightarrow R_{C2} = 3.21 \text{ k}\Omega$$

$$I_{RC1} = I_{C1} - I_{B2} = 0.8 - 0.008 = 0.792 \text{ mA}$$

$$R_{C1} = \frac{-0.87 - (-5)}{0.792} \Rightarrow R_{C1} = 5.21 \text{ k}\Omega$$