

47. We use Eq. 29-37 where  $\vec{\mu}$  is the magnetic dipole moment of the wire loop and  $\vec{B}$  is the magnetic field, as well as Newton's second law. Since the plane of the loop is parallel to the incline the dipole moment is normal to the incline. The forces acting on the cylinder are the force of gravity  $mg$ , acting downward from the center of mass, the normal force of the incline  $N$ , acting perpendicularly to the incline through the center of mass, and the force of friction  $f$ , acting up the incline at the point of contact. We take the  $x$  axis to be positive down the incline. Then the  $x$  component of Newton's second law for the center of mass yields

$$mg \sin \theta - f = ma .$$

For purposes of calculating the torque, we take the axis of the cylinder to be the axis of rotation. The magnetic field produces a torque with magnitude  $\mu B \sin \theta$ , and the force of friction produces a torque with magnitude  $fr$ , where  $r$  is the radius of the cylinder. The first tends to produce an angular acceleration in the counterclockwise direction, and the second tends to produce an angular acceleration in the clockwise direction. Newton's second law for rotation about the center of the cylinder,  $\tau = I\alpha$ , gives

$$fr - \mu B \sin \theta = I\alpha .$$

Since we want the current that holds the cylinder in place, we set  $a = 0$  and  $\alpha = 0$ , and use one equation to eliminate  $f$  from the other. The result is  $mgr = \mu B$ . The loop is rectangular with two sides of length  $L$  and two of length  $2r$ , so its area is  $A = 2rL$  and the dipole moment is  $\mu = NiA = 2NirL$ . Thus,  $mgr = 2NirLB$  and

$$i = \frac{mg}{2NLB} = \frac{(0.250 \text{ kg})(9.8 \text{ m/s}^2)}{2(10.0)(0.100 \text{ m})(0.500 \text{ T})} = 2.45 \text{ A} .$$