

19. (a) We read the amplitude from the graph. It is about 5.0 cm.
- (b) We read the wavelength from the graph. The curve crosses $y = 0$ at about $x = 15$ cm and again with the same slope at about $x = 55$ cm, so $\lambda = 55 \text{ cm} - 15 \text{ cm} = 40 \text{ cm} = 0.40 \text{ m}$.
- (c) The wave speed is $v = \sqrt{\tau/\mu}$, where τ is the tension in the string and μ is the linear mass density of the string. Thus,

$$v = \sqrt{\frac{3.6 \text{ N}}{25 \times 10^{-3} \text{ kg/m}}} = 12 \text{ m/s} .$$

- (d) The frequency is $f = v/\lambda = (12 \text{ m/s})/(0.40 \text{ m}) = 30 \text{ Hz}$ and the period is $T = 1/f = 1/(30 \text{ Hz}) = 0.033 \text{ s}$.
- (e) The maximum string speed is $u_m = \omega y_m = 2\pi f y_m = 2\pi(30 \text{ Hz})(5.0 \text{ cm}) = 940 \text{ cm/s} = 9.4 \text{ m/s}$.
- (f) The string displacement is assumed to have the form $y(x, t) = y_m \sin(kx + \omega t + \phi)$. A plus sign appears in the argument of the trigonometric function because the wave is moving in the negative x direction. The amplitude is $y_m = 5.0 \times 10^{-2} \text{ m}$, the angular frequency is $\omega = 2\pi f = 2\pi(30 \text{ Hz}) = 190 \text{ rad/s}$, and the angular wave number is $k = 2\pi/\lambda = 2\pi/(0.40 \text{ m}) = 16 \text{ m}^{-1}$. According to the graph, the displacement at $x = 0$ and $t = 0$ is $4.0 \times 10^{-2} \text{ m}$. The formula for the displacement gives $y(0, 0) = y_m \sin \phi$. We wish to select ϕ so that $5.0 \times 10^{-2} \sin \phi = 4.0 \times 10^{-2}$. The solution is either 0.93 rad or 2.21 rad. In the first case the function has a positive slope at $x = 0$ and matches the graph. In the second case it has negative slope and does not match the graph. We select $\phi = 0.93 \text{ rad}$. The expression for the displacement is

$$y(x, t) = (5.0 \times 10^{-2} \text{ m}) \sin [(16 \text{ m}^{-1})x + (190 \text{ s}^{-1})t + 0.93] .$$