

14. (a) We choose clockwise as the negative rotational sense and rightwards as the positive translational direction. Thus, since this is the moment when it begins to roll smoothly, Eq. 12-2 becomes

$$v_{\text{com}} = -R\omega = (-0.11 \text{ m})\omega .$$

This velocity is positive-valued (rightward) since ω is negative-valued (clockwise) as shown in Fig. 12-34.

- (b) The force of friction exerted on the ball of mass m is $-\mu_k mg$ (negative since it points left), and setting this equal to ma_{com} leads to

$$a_{\text{com}} = -\mu g = -(0.21)(9.8 \text{ m/s}^2) = -2.1 \text{ m/s}^2$$

where the minus sign indicates that the center of mass acceleration points left, opposite to its velocity, so that the ball is decelerating.

- (c) Measured about the center of mass, the torque exerted on the ball due to the frictional force is given by $\tau = -\mu mgR$. Using Table 11-2(f) for the rotational inertia, the angular acceleration becomes (using Eq. 11-37)

$$\alpha = \frac{\tau}{I} = \frac{-\mu mgR}{\frac{2mR^2}{5}} = \frac{-5\mu g}{2R} = \frac{-5(0.21)(9.8)}{2(0.11)} = -47 \text{ rad/s}^2$$

where the minus sign indicates that the angular acceleration is clockwise, the same direction as ω (so its angular motion is “speeding up”).

- (d) The center-of-mass of the sliding ball decelerates from $v_{\text{com},0}$ to v_{com} during time t according to Eq. 2-11:

$$v_{\text{com}} = v_{\text{com},0} - \mu g t .$$

During this time, the angular speed of the ball increases (in magnitude) from zero to $|\omega|$ according to Eq. 11-12:

$$|\omega| = |\alpha| t = \frac{5\mu g t}{2R} = \frac{v_{\text{com}}}{R}$$

where we have made use of our part (a) result in the last equality. We have two equations involving v_{com} , so we eliminate that variable and find

$$t = \frac{2v_{\text{com},0}}{7\mu g} = \frac{2(8.5)}{7(0.21)(9.8)} = 1.2 \text{ s} .$$

- (e) The skid length of the ball is (using Eq. 2-15)

$$\Delta x = v_{\text{com},0}t - \frac{1}{2}(\mu g)t^2 = (8.5)(1.2) - \frac{1}{2}(0.21)(9.8)(1.2)^2 = 8.6 \text{ m} .$$

- (f) The center of mass velocity at the time found in part (d) is

$$v_{\text{com}} = v_{\text{com},0} - \mu g t = 8.5 - (0.21)(9.8)(1.2) = 6.1 \text{ m/s} .$$