

64. (a) The most obvious input-heat step is the constant-volume process. Since the gas is monatomic, we know from Chapter 20 that $C_V = \frac{3}{2}R$. Therefore,

$$\begin{aligned} Q_V &= nC_V\Delta T \\ &= (1 \text{ mol}) \left(\frac{3}{2} \right) \left(8.31 \frac{\text{J}}{\text{mol} \cdot \text{K}} \right) (600 \text{ K} - 300 \text{ K}) \\ &= 3740 \text{ J} . \end{aligned}$$

Since the heat transfer during the isothermal step is positive, we may consider it also to be an input-heat step. The isothermal Q is equal to the isothermal work (calculated in the next part) because $\Delta E_{\text{int}} = 0$ for an ideal gas isothermal process (see Eq. 20-45). Borrowing from the part (b) computation, we have

$$Q_{\text{isotherm}} = nRT_H \ln 2 = (1 \text{ mol}) \left(8.31 \frac{\text{J}}{\text{mol} \cdot \text{K}} \right) (600 \text{ K}) \ln 2 = 3456 \text{ J} .$$

Therefore, $Q_H = Q_V + Q_{\text{isotherm}} = 7.2 \times 10^3 \text{ J}$.

- (b) We consider the sum of works done during the processes (noting that no work is done during the constant-volume step). Using Eq. 20-14 and Eq. 20-16, we have

$$W = nRT_H \ln \left(\frac{V_{\text{max}}}{V_{\text{min}}} \right) + p_{\text{min}} (V_{\text{min}} - V_{\text{max}})$$

where (by the gas law in ratio form, as illustrated in Sample Problem 20-1) the volume ratio is

$$\frac{V_{\text{max}}}{V_{\text{min}}} = \frac{T_H}{T_L} = \frac{600 \text{ K}}{300 \text{ K}} = 2 .$$

Thus, the net work is

$$\begin{aligned} W &= nRT_H \ln 2 + p_{\text{min}} V_{\text{min}} \left(1 - \frac{V_{\text{max}}}{V_{\text{min}}} \right) \\ &= nRT_H \ln 2 + nRT_L (1 - 2) \\ &= nR (T_H \ln 2 - T_L) \\ &= (1 \text{ mol}) \left(8.31 \frac{\text{J}}{\text{mol} \cdot \text{K}} \right) ((600 \text{ K}) \ln 2 - (300 \text{ K})) \\ &= 9.6 \times 10^2 \text{ J} . \end{aligned}$$

- (c) Eq. 21-9 gives

$$\varepsilon = \frac{W}{Q_H} = 0.134 \approx 13\% .$$