

16. In coming to equilibrium, the heat lost by the 100 cm^3 of liquid water (of mass $m_w = 100 \text{ g}$ and specific heat capacity $c_w = 4190 \text{ J/kg}\cdot\text{K}$) is absorbed by the ice (of mass m_i which melts and reaches $T_f > 0^\circ\text{C}$). We begin by finding the equilibrium temperature:

$$\begin{aligned}\sum Q &= 0 \\ Q_{\text{warm water cools}} + Q_{\text{ice warms to } 0^\circ} + Q_{\text{ice melts}} + Q_{\text{melted ice warms}} &= 0 \\ c_w m_w (T_f - 20^\circ) + c_i m_i (0^\circ - (-10^\circ)) + L_F m_i + c_w m_i (T_f - 0^\circ) &= 0\end{aligned}$$

which yields, after using $L_F = 333000 \text{ J/kg}$ and values cited in the problem, $T_f = 12.24^\circ$ which is equivalent to $T_f = 285.39 \text{ K}$. Sample Problem 20-2 shows that

$$\Delta S_{\text{temp change}} = mc \ln\left(\frac{T_2}{T_1}\right)$$

for processes where $\Delta T = T_2 - T_1$, and Eq. 21-2 gives

$$\Delta S_{\text{melt}} = \frac{L_F m}{T_o}$$

for the phase change experienced by the ice (with $T_o = 273.15 \text{ K}$). The total entropy change is (with T in Kelvins)

$$\begin{aligned}\Delta S_{\text{system}} &= m_w c_w \ln\left(\frac{285.39}{293.15}\right) + m_i c_i \ln\left(\frac{273.15}{263.15}\right) + m_i c_w \ln\left(\frac{285.39}{273.15}\right) + \frac{L_F m_i}{273.15} \\ &= -11.24 + 0.66 + 1.47 + 9.75 = 0.64 \text{ J/K} .\end{aligned}$$