

83. (a) By Eq. 16-13, the mass of the block is

$$m_b = \frac{kT_0^2}{4\pi^2} = 2.43 \text{ kg} .$$

Therefore, with $m_p = 0.50 \text{ kg}$, the new period is

$$T = 2\pi\sqrt{\frac{m_p + m_b}{k}} = 0.44 \text{ s} .$$

(b) The speed before the collision (since it is at its maximum, passing through equilibrium) is $v_0 = x_m\omega_0$ where $\omega_0 = 2\pi/T_0$; thus, $v_0 = 3.14 \text{ m/s}$. Using momentum conservation (along the horizontal direction) we find the speed after the collision.

$$V = v_0 \frac{m_b}{m_p + m_b} = 2.61 \text{ m/s} .$$

The equilibrium position has not changed, so (for the new system of greater mass) this represents the maximum speed value for the subsequent harmonic motion: $V = x'_m\omega$ where $\omega = 2\pi/T = 14.3 \text{ rad/s}$. Therefore, $x'_m = 0.18 \text{ m}$.