

38. Our approach (based on Eq. 23-29) consists of several steps. The first is to find an *approximate* value of  $e$  by taking differences between all the given data. The smallest difference is between the fifth and sixth values:  $18.08 \times 10^{-19} \text{ C} - 16.48 \times 10^{-19} \text{ C} = 1.60 \times 10^{-19} \text{ C}$  which we denote  $e_{\text{approx}}$ . The goal at this point is to assign integers  $n$  using this approximate value of  $e$ :

$$\begin{array}{rcl}
\text{datum 1} & \frac{6.563 \times 10^{-19} \text{ C}}{e_{\text{approx}}} = 4.10 & \implies n_1 = 4 \\
\text{datum 2} & \frac{8.204 \times 10^{-19} \text{ C}}{e_{\text{approx}}} = 5.13 & \implies n_2 = 5 \\
\text{datum 3} & \frac{11.50 \times 10^{-19} \text{ C}}{e_{\text{approx}}} = 7.19 & \implies n_3 = 7 \\
\text{datum 4} & \frac{13.13 \times 10^{-19} \text{ C}}{e_{\text{approx}}} = 8.21 & \implies n_4 = 8 \\
\text{datum 5} & \frac{16.48 \times 10^{-19} \text{ C}}{e_{\text{approx}}} = 10.30 & \implies n_5 = 10 \\
\text{datum 6} & \frac{18.08 \times 10^{-19} \text{ C}}{e_{\text{approx}}} = 11.30 & \implies n_6 = 11 \\
\text{datum 7} & \frac{19.71 \times 10^{-19} \text{ C}}{e_{\text{approx}}} = 12.32 & \implies n_7 = 12 \\
\text{datum 8} & \frac{22.89 \times 10^{-19} \text{ C}}{e_{\text{approx}}} = 14.31 & \implies n_8 = 14 \\
\text{datum 9} & \frac{26.13 \times 10^{-19} \text{ C}}{e_{\text{approx}}} = 16.33 & \implies n_9 = 16
\end{array}$$

Next, we construct a new data set  $(e_1, e_2, e_3 \dots)$  by dividing the given data by the respective exact integers  $n_i$  (for  $i = 1, 2, 3 \dots$ ):

$$(e_1, e_2, e_3 \dots) = \left( \frac{6.563 \times 10^{-19} \text{ C}}{n_1}, \frac{8.204 \times 10^{-19} \text{ C}}{n_2}, \frac{11.50 \times 10^{-19} \text{ C}}{n_3} \dots \right)$$

which gives (carrying a few more figures than are significant)

$$(1.64075 \times 10^{-19} \text{ C}, 1.6408 \times 10^{-19} \text{ C}, 1.64286 \times 10^{-19} \text{ C} \dots)$$

as the new data set (our experimental values for  $e$ ). We compute the average and standard deviation of this set, obtaining

$$e_{\text{exptal}} = e_{\text{avg}} \pm \Delta e = (1.641 \pm 0.004) \times 10^{-19} \text{ C}$$

which does not agree (to within one standard deviation) with the modern accepted value for  $e$ . The lower bound on this spread is  $e_{\text{avg}} - \Delta e = 1.637 \times 10^{-19} \text{ C}$  which is still about 2% too high.