

93. (a) The surface area of the cylinder is given by $A_1 = 2\pi r_1^2 + 2\pi r_1 h_1 = 2\pi(2.5 \times 10^{-2} \text{ m})^2 + 2\pi(2.5 \times 10^{-2} \text{ m})(5.0 \times 10^{-2} \text{ m}) = 1.18 \times 10^{-2} \text{ m}^2$, its temperature is $T_1 = 273 + 30 = 303 \text{ K}$, and the temperature of the environment is $T_{\text{env}} = 273 + 50 = 323 \text{ K}$. From Eq. 19-39 we have

$$\begin{aligned} P_1 &= \sigma \varepsilon A_1 (T_{\text{env}}^4 - T^4) \\ &= (0.85)(1.18 \times 10^{-2} \text{ m}^2) ((323 \text{ K})^4 - (303 \text{ K})^4) \\ &= 1.39 \text{ W} . \end{aligned}$$

- (b) Let the new height of the cylinder be h_2 . Since the volume V of the cylinder is fixed, we must have $V = \pi r_1^2 h_1 = \pi r_2^2 h_2$. We solve for h_2 :

$$\begin{aligned} h_2 &= \left(\frac{r_1}{r_2} \right)^2 h_1 \\ &= \left(\frac{2.5 \text{ cm}}{0.50 \text{ cm}} \right)^2 (5.0 \text{ cm}) \\ &= 125 \text{ cm} = 1.25 \text{ m} . \end{aligned}$$

The corresponding new surface area A_2 of the cylinder is

$$A_2 = 2\pi r_2^2 + 2\pi r_2 h_2 = 2\pi(0.50 \times 10^{-2} \text{ m})^2 + 2\pi(0.50 \times 10^{-2} \text{ m})(1.25 \text{ m}) = 3.94 \times 10^{-2} \text{ m}^2 .$$

Consequently,

$$\frac{P_2}{P_1} = \frac{A_2}{A_1} = \frac{3.94 \times 10^{-2} \text{ m}^2}{1.18 \times 10^{-2} \text{ m}^2} = 3.3 .$$