

78. (a) Initially, the capacitance is

$$C_0 = \frac{\varepsilon_0 A}{d} = \frac{\left(8.85 \times 10^{-12} \frac{\text{C}^2}{\text{N} \cdot \text{m}^2}\right) (0.12 \text{ m}^2)}{1.2 \times 10^{-2} \text{ m}} = 89 \text{ pF} .$$

(b) Working through Sample Problem 26-6 algebraically, we find:

$$C = \frac{\varepsilon_0 A \kappa}{\kappa(d-b) + b} = \frac{\left(8.85 \times 10^{-12} \frac{\text{C}^2}{\text{N} \cdot \text{m}^2}\right) (0.12 \text{ m}^2)(4.8)}{(4.8)(1.2 - 0.40)(10^{-2} \text{ m}) + (4.0 \times 10^{-3} \text{ m})} = 120 \text{ pF} .$$

(c) Before the insertion, $q = C_0 V (89 \text{ pF})(120 \text{ V}) = 11 \text{ nC}$. Since the battery is disconnected, q will remain the same after the insertion of the slab.

(d) $E = q/\varepsilon_0 A = 11 \times 10^{-9} \text{ C} / \left(8.85 \times 10^{-12} \frac{\text{C}^2}{\text{N} \cdot \text{m}^2}\right) (0.12 \text{ m}^2) = 10 \text{ kV/m}$.

(e) $E' = E/\kappa = (10 \text{ kV/m})/4.8 = 2.1 \text{ kV/m}$.

(f) $V = E(d-b) + E'b = (10 \text{ kV/m})(0.012 \text{ m} - 0.0040 \text{ m}) + (2.1 \text{ kV/m})(0.40 \times 10^{-3} \text{ m}) = 88 \text{ V}$.

(g) The work done is

$$\begin{aligned} W_{\text{ext}} &= \Delta U = \frac{q^2}{2} \left(\frac{1}{C} - \frac{1}{C_0} \right) \\ &= \frac{(11 \times 10^{-9} \text{ C})^2}{2} \left(\frac{1}{89 \times 10^{-12} \text{ F}} - \frac{1}{120 \times 10^{-12} \text{ F}} \right) \\ &= -1.7 \times 10^{-7} \text{ J} . \end{aligned}$$