

58. Since the volume of the monatomic ideal gas is kept constant it does not do any work in the heating process. Therefore the heat Q it absorbs is equal to the change in its internal energy: $dQ = dE_{\text{int}} = \frac{3}{2}nRdT$. Thus

$$\begin{aligned}\Delta S &= \int \frac{dQ}{T} = \int_{T_i}^{T_f} \frac{(3nR/2)dT}{T} = \frac{3}{2}nR \ln \left(\frac{T_f}{T_i} \right) \\ &= \frac{3}{2}(1.0 \text{ mol}) \left(8.31 \frac{\text{J}}{\text{mol} \cdot \text{K}} \right) \ln \left(\frac{400 \text{ K}}{300 \text{ K}} \right) = 3.59 \text{ J/K} .\end{aligned}$$