

18. (a) In frame  $S$ , our coordinates are such that  $x_1 = +1200$  m for the big flash, and  $x_2 = 1200 - 720 = 480$  m for the small flash (which occurred later). Thus,  $\Delta x = x_2 - x_1 = -720$  m. If we set  $\Delta x' = 0$  in Eq. 38-24, we find

$$0 = \gamma (\Delta x - v\Delta t) = \gamma (-720 \text{ m} - v(5.00 \times 10^{-6} \text{ s}))$$

which yields  $v = -1.44 \times 10^8$  m/s. Therefore, frame  $S'$  must be moving in the  $-x$  direction with a speed of  $0.480c$ .

- (b) Eq. 38-27 leads to

$$\Delta t' = \gamma \left( \Delta t - \frac{v\Delta x}{c^2} \right) = \gamma \left( 5.00 \times 10^{-6} \text{ s} - \frac{(-1.44 \times 10^8 \text{ m/s})(-720 \text{ m})}{(2.998 \times 10^8 \text{ m/s})^2} \right)$$

which turns out to be positive (regardless of the specific value of  $\gamma$ ). Thus, the order of the flashes is the same in the  $S'$  frame as it is in the  $S$  frame (where  $\Delta t$  is also positive). Thus, the big flash occurs first, and the small flash occurs later.

- (c) Finishing the computation begun in part (b), we obtain

$$\Delta t' = \frac{5.00 \times 10^{-6} \text{ s} - \frac{(-1.44 \times 10^8 \text{ m/s})(-720 \text{ m})}{(2.998 \times 10^8 \text{ m/s})^2}}{\sqrt{1 - 0.480^2}} = 4.39 \times 10^{-6} \text{ s} .$$