

46. (a) Using Eq. 27-11 and Eq. 25-42, we obtain

$$\left| \vec{J}_A \right| = \frac{\left| \vec{E}_A \right|}{\rho} = \frac{|\Delta V_A|}{\rho L} = \frac{40 \times 10^{-6} \text{ V}}{(100 \Omega \cdot \text{m})(20 \text{ m})} = 2.0 \times 10^{-8} \text{ A/m}^2 .$$

(b) Similarly, in region B we find

$$\left| \vec{J}_B \right| = \frac{|\Delta V_B|}{\rho L} = \frac{60 \times 10^{-6} \text{ V}}{(100 \Omega \cdot \text{m})(20 \text{ m})} = 3.0 \times 10^{-8} \text{ A/m}^2 .$$

(c) With $w = 1.0 \text{ m}$ and $d_A = 3.8 \text{ m}$ (so that the cross-section area is $d_A w$) we have (using Eq. 27-5)

$$i_A = \left| \vec{J}_A \right| d_A w = (2.0 \times 10^{-8} \text{ A/m}^2) (1.0 \text{ m})(3.8 \text{ m}) = 7.6 \times 10^{-8} \text{ A} .$$

(d) Assuming $i_A = i_B$ we obtain

$$d_B = \frac{i_B}{\left| \vec{J}_B \right| w} = \frac{7.6 \times 10^{-8} \text{ A}}{(3.0 \times 10^{-8} \text{ A/m}^2) (1.0 \text{ m})} = 2.5 \text{ m} .$$

(e) We do not show the graph-and-figure here, but describe it briefly. To be meaningful (as a function of x) we would plot $V(x)$ measured relative to $V(0)$ (the voltage at, say, the left edge of the figure, which we are effectively setting equal to 0). From the problem statement, we note that $V(x)$ would grow linearly in region A , increasing by $40 \mu\text{V}$ for each 20 m distance. Once we reach the transition region (between A and B) we might assume a parabolic shape for $V(x)$ as it changes from the $40 \mu\text{V}$ -per- 20 m slope to a $60 \mu\text{V}$ -per- 20 m slope (which becomes its constant slope once we are into region B , where the function is again linear). The figure goes further than region B , so as we leave region B , we might assume again a parabolic shape for the function as it tends back down toward some lower slope value.