

24. Let the energy of the state in question be an amount ΔE above the Fermi energy E_F . Then, Eq. 42-6 gives the occupancy probability of the state as

$$P = \frac{1}{e^{(E_F + \Delta E - E_F)/kT} + 1} = \frac{1}{e^{\Delta E/kT} + 1} .$$

We solve for ΔE to obtain

$$\Delta E = kT \ln\left(\frac{1}{P} - 1\right) = (1.38 \times 10^{23} \text{ J/K})(300 \text{ K}) \ln\left(\frac{1}{0.10} - 1\right) = 9.1 \times 10^{-21} \text{ J} ,$$

which is equivalent to $5.7 \times 10^{-2} \text{ eV} = 57 \text{ meV}$.