

41. The string is fixed at both ends so the resonant wavelengths are given by  $\lambda = 2L/n$ , where  $L$  is the length of the string and  $n$  is an integer. The resonant frequencies are given by  $f = v/\lambda = nv/2L$ , where  $v$  is the wave speed on the string. Now  $v = \sqrt{\tau/\mu}$ , where  $\tau$  is the tension in the string and  $\mu$  is the linear mass density of the string. Thus  $f = (n/2L)\sqrt{\tau/\mu}$ . Suppose the lower frequency is associated with  $n = n_1$  and the higher frequency is associated with  $n = n_1 + 1$ . There are no resonant frequencies between so you know that the integers associated with the given frequencies differ by 1. Thus  $f_1 = (n_1/2L)\sqrt{\tau/\mu}$  and

$$f_2 = \frac{n_1 + 1}{2L} \sqrt{\frac{\tau}{\mu}} = \frac{n_1}{2L} \sqrt{\frac{\tau}{\mu}} + \frac{1}{2L} \sqrt{\frac{\tau}{\mu}} = f_1 + \frac{1}{2L} \sqrt{\frac{\tau}{\mu}} .$$

This means  $f_2 - f_1 = (1/2L)\sqrt{\tau/\mu}$  and

$$\begin{aligned} \tau &= 4L^2\mu(f_2 - f_1)^2 \\ &= 4(0.300\text{ m})^2(0.650 \times 10^{-3}\text{ kg/m})(1320\text{ Hz} - 880\text{ Hz})^2 \\ &= 45.3\text{ N} . \end{aligned}$$