

32. First, we find the speed of the receding galaxy from Eq. 38-30:

$$\begin{aligned}\beta &= \frac{1 - (f/f_0)^2}{1 + (f/f_0)^2} = \frac{1 - (\lambda_0/\lambda)^2}{1 + (\lambda_0/\lambda)^2} \\ &= \frac{1 - (590.0 \text{ nm}/602.0 \text{ nm})^2}{1 + (590.0 \text{ nm}/602.0 \text{ nm})^2} = 0.02013\end{aligned}$$

where we use $f = c/\lambda$ and $f_0 = c/\lambda_0$. Then from Eq. 45-19,

$$r = \frac{v}{H} = \frac{\beta c}{H} = \frac{(0.02013)(2.998 \times 10^8 \text{ m/s})}{19.3 \text{ mm/s}\cdot\text{ly}} = 3.13 \times 10^8 \text{ ly} .$$

(Note: if one uses the classical Doppler shift formula instead of the relativistic version in Eq. 38-30, one obtains $r = 31.7 \times 10^8 \text{ ly}$, which is reasonably close to the value we obtained above. This is to be expected since $\beta \approx 0.02 \ll 1$.)