

42. (a) In the first case

$$\begin{aligned}
 i' &= \frac{\mathcal{E}}{R_{\text{eq}}} = \frac{\mathcal{E}}{R_A + R_0 + R_V R / (R + R_V)} \\
 &= \frac{12.0 \text{ V}}{3.00 \Omega + 100 \Omega + (300 \Omega)(85.0 \Omega) / (300 \Omega + 85.0 \Omega)} \\
 &= 7.09 \times 10^{-2} \text{ A} ,
 \end{aligned}$$

and $V = \mathcal{E} - i'(R_A + R_0) = 12.0 \text{ V} - (0.0709 \text{ A})(103.00 \Omega) = 4.70 \text{ V}$. In the second case $V = \mathcal{E} R' / (R' + R_0)$, where

$$R' = \frac{R_V (R + R_A)}{R_V + R + R_A} = \frac{(300 \Omega)(300 \Omega + 85.0 \Omega)}{300 \Omega + 85.0 \Omega + 3.00 \Omega} = 68.0 \Omega .$$

So $V = (12.0 \text{ V})(68.0 \Omega) / (68.0 \Omega + 100 \Omega) = 4.86 \text{ V}$, and $i' = V / (R + R_A) = 4.86 \text{ V} / (300 \Omega + 85.0 \Omega) = 5.52 \times 10^{-2} \text{ A}$.

(b) In the first case $R' = V / i' = 4.70 \text{ V} / (7.09 \times 10^{-2} \text{ A}) = 66.3 \Omega$. In the second case $R' = V / i' = 4.86 \text{ V} / (5.52 \times 10^{-2} \text{ A}) = 88.0 \Omega$.