

86. (a) Eqs. 33-4 and 33-14 lead to

$$Q = \frac{I}{\omega} = I\sqrt{LC} = 1.27 \times 10^{-6} \text{ C} .$$

(b) We choose the phase constant in Eq. 33-12 to be $\phi = -\pi/2$, so that $i_0 = I$ in Eq. 33-15). Thus, the energy in the capacitor is

$$U_E = \frac{q^2}{2C} = \frac{Q^2}{2C} (\sin \omega t)^2 .$$

Differentiating and using the fact that $2 \sin \theta \cos \theta = \sin 2\theta$, we obtain

$$\frac{dU_E}{dt} = \frac{Q^2}{2C} \omega \sin 2\omega t .$$

We find the maximum value occurs whenever $\sin 2\omega t = 1$, which leads (with $n = \text{odd integer}$) to

$$t = \frac{1}{2\omega} \frac{n\pi}{2} = \frac{n\pi}{4\omega} = \frac{n\pi}{4} \sqrt{LC} = 8.31 \times 10^{-5} \text{ s}, 2.49 \times 10^{-4} \text{ s}, \dots .$$

(c) Returning to the above expression for dU_E/dt with the requirement that $\sin 2\omega t = 1$, we obtain

$$\left(\frac{dU_E}{dt} \right)_{\max} = \frac{Q^2}{2C} \omega = \frac{(I\sqrt{LC})^2}{2C} \frac{1}{\sqrt{LC}} = \frac{I^2}{2} \sqrt{\frac{L}{C}} = 5.44 \times 10^{-3} \text{ J/s} .$$