

26. The equation of motion for the proton is

$$\begin{aligned}\vec{F} &= q\vec{v} \times \vec{B} = q(v_x\hat{i} + v_y\hat{j} + v_z\hat{k}) \times B\hat{i} = qB(v_z\hat{j} - v_y\hat{k}) \\ &= m_p\vec{a} = m_p \left[\left(\frac{dv_x}{dt} \right) \hat{i} + \left(\frac{dv_y}{dt} \right) \hat{j} + \left(\frac{dv_z}{dt} \right) \hat{k} \right].\end{aligned}$$

Thus,

$$\begin{aligned}\frac{dv_x}{dt} &= 0 \\ \frac{dv_y}{dt} &= \omega v_z \\ \frac{dv_z}{dt} &= -\omega v_y,\end{aligned}$$

where $\omega = eB/m_p$. The solution is $v_x = v_{0x}$, $v_y = v_{0y} \cos \omega t$ and $v_z = -v_{0y} \sin \omega t$. In summary, we have $\vec{v}(t) = v_{0x}\hat{i} + v_{0y} \cos(\omega t)\hat{j} - v_{0y}(\sin \omega t)\hat{k}$.