

66. (a) Since the field is constant and the capacitors are in parallel (each with 600 V across them) with identical distances ($d = 0.00300$ m) between the plates, then the field in A is equal to the field in B :

$$\left| \vec{E} \right| = \frac{V}{d} = 2.00 \times 10^5 \text{ V/m} .$$

- (b) See the note in part (a).

- (c) For the air-filled capacitor, Eq. 26-4 leads to

$$\sigma = \frac{q}{A} = \varepsilon_0 \left| \vec{E} \right| = 1.77 \times 10^{-6} \text{ C/m}^2 .$$

- (d) For the dielectric-filled capacitor, we use Eq. 26-27:

$$\sigma = \kappa \varepsilon_0 \left| \vec{E} \right| = 4.60 \times 10^{-6} \text{ C/m}^2 .$$

- (e) Although the discussion in the textbook (§26-8) is in terms of the charge being held fixed (while a dielectric is inserted), it is readily adapted to this situation (where comparison is made of two capacitors which have the same *voltage* and are identical except for the fact that one has a dielectric). The fact that capacitor B has a relatively large charge but only produces the field that A produces (with its smaller charge) is in line with the point being made (in the text) with Eq. 26-32 and in the material that follows. Adapting Eq. 26-33 to this problem, we see that the difference in charge densities between parts (c) and (d) is due, in part, to the (negative) layer of charge at the top surface of the dielectric; consequently,

$$\sigma' = (1.77 \times 10^{-6}) - (4.60 \times 10^{-6}) = -2.83 \times 10^{-6} \text{ C/m}^2 .$$