

17. Think of the quadrupole as composed of two dipoles, each with dipole moment of magnitude  $p = qd$ . The moments point in opposite directions and produce fields in opposite directions at points on the quadrupole axis. Consider the point P on the axis, a distance  $z$  to the right of the quadrupole center and take a rightward pointing field to be positive. Then, the field produced by the right dipole of the pair is  $qd/2\pi\epsilon_0(z - d/2)^3$  and the field produced by the left dipole is  $-qd/2\pi\epsilon_0(z + d/2)^3$ . Use the binomial expansions  $(z - d/2)^{-3} \approx z^{-3} - 3z^{-4}(-d/2)$  and  $(z + d/2)^{-3} \approx z^{-3} - 3z^{-4}(d/2)$  to obtain

$$E = \frac{qd}{2\pi\epsilon_0} \left[ \frac{1}{z^3} + \frac{3d}{2z^4} - \frac{1}{z^3} + \frac{3d}{2z^4} \right] = \frac{6qd^2}{4\pi\epsilon_0 z^4} .$$

Let  $Q = 2qd^2$ . Then,

$$E = \frac{3Q}{4\pi\epsilon_0 z^4} .$$