

66. (a) We denote the surface charge density of the disk as σ_1 for $0 < r < R/2$, and as σ_2 for $R/2 < r < R$. Thus the total charge on the disk is given by

$$\begin{aligned}
 q &= \int_{\text{disk}} dq = \int_0^{R/2} 2\pi\sigma_1 r \, dr + \int_{R/2}^R 2\pi\sigma_2 r \, dr = \frac{\pi}{4} R^2 (\sigma_1 + 3\sigma_2) \\
 &= \frac{\pi}{4} (2.20 \times 10^{-2} \text{ m})^2 [1.50 \times 10^{-6} \text{ C/m}^2 + 3(8.00 \times 10^{-7} \text{ C/m}^2)] \\
 &= 1.48 \times 10^{-9} \text{ C} .
 \end{aligned}$$

- (b) We use Eq. 25-36:

$$\begin{aligned}
 V(z) &= \int_{\text{disk}} dV = k \left[\int_0^{R/2} \frac{\sigma_1 (2\pi R') dR'}{\sqrt{z^2 + R'^2}} + \int_{R/2}^R \frac{\sigma_2 (2\pi R') dR'}{\sqrt{z^2 + R'^2}} \right] \\
 &= \frac{\sigma_1}{2\epsilon_0} \left(\sqrt{z^2 + \frac{R^2}{4}} - z \right) + \frac{\sigma_2}{2\epsilon_0} \left(\sqrt{z^2 + R^2} - \sqrt{z^2 + \frac{R^2}{4}} \right) .
 \end{aligned}$$

Substituting the numerical values of σ_1 , σ_2 , R and z , we obtain $V(z) = 7.95 \times 10^2 \text{ V}$.