

34. We take the moment of applying brakes to be  $t = 0$ . The deceleration is constant so that Table 2-1 can be used. Our primed variables (such as  $v'_o = 72 \text{ km/h} = 20 \text{ m/s}$ ) refer to one train (moving in the  $+x$  direction and located at the origin when  $t = 0$ ) and unprimed variables refer to the other (moving in the  $-x$  direction and located at  $x_o = +950 \text{ m}$  when  $t = 0$ ). We note that the acceleration vector of the unprimed train points in the *positive* direction, even though the train is slowing down; its initial velocity is  $v_o = -144 \text{ km/h} = -40 \text{ m/s}$ . Since the primed train has the lower initial speed, it should stop sooner than the other train would (were it not for the collision). Using Eq 2-16, it should stop (meaning  $v' = 0$ ) at

$$x' = \frac{(v')^2 - (v'_o)^2}{2a'} = \frac{0 - 20^2}{-2} = 200 \text{ m} .$$

The speed of the other train, when it reaches that location, is

$$v = \sqrt{v_o^2 + 2a\Delta x} = \sqrt{(-40)^2 + 2(1.0)(200 - 950)} = \sqrt{100} = 10 \text{ m/s}$$

using Eq 2-16 again. Specifically, its velocity at that moment would be  $-10 \text{ m/s}$  since it is still traveling in the  $-x$  direction when it crashes. If the computation of  $v$  had failed (meaning that a negative number would have been inside the square root) then we would have looked at the possibility that there was no collision and examined how far apart they finally were. A concern that can be brought up is whether the primed train collides before it comes to rest; this can be studied by computing the time it stops (Eq. 2-11 yields  $t = 20 \text{ s}$ ) and seeing where the unprimed train is at that moment (Eq. 2-18 yields  $x = 350 \text{ m}$ , still a good distance away from contact).