

21. Studying Sample Problem 23-3, we see that the field evaluated at the center of curvature due to a charged distribution on a circular arc is given by

$$\vec{E} = \frac{\lambda}{4\pi\epsilon_0 r} \left[\sin \theta \right]_{-\theta/2}^{\theta/2} \quad \text{along the symmetry axis}$$

where $\lambda = q/r\theta$ with θ in radians. In this problem, each charged quarter-circle produces a field of magnitude

$$|\vec{E}| = \frac{|q|}{r\pi/2} \frac{1}{4\pi\epsilon_0 r} \left[\sin \theta \right]_{-\pi/4}^{\pi/4} = \frac{|q|}{\epsilon_0 \pi^2 r^2 \sqrt{2}} .$$

That produced by the positive quarter-circle points at -45° , and that of the negative quarter-circle points at $+45^\circ$. By symmetry, we conclude that their net field is horizontal (and rightward in the textbook figure) with magnitude

$$E_x = 2 \left(\frac{|q|}{\epsilon_0 \pi^2 r^2 \sqrt{2}} \right) \cos 45^\circ = \frac{|q|}{\epsilon_0 \pi^2 r^2} .$$