

8. The goal is to arrive at the least magnitude of \vec{F}_{net} , and as long as the magnitudes of \vec{F}_2 and \vec{F}_3 are (in total) less than or equal to $|\vec{F}_1|$ then we should orient them opposite to the direction of \vec{F}_1 (which is the $+x$ direction).

- (a) We orient both \vec{F}_2 and \vec{F}_3 in the $-x$ direction. Then, the magnitude of the net force is $50 - 30 - 20 = 0$, resulting in zero acceleration for the tire.
- (b) We again orient \vec{F}_2 and \vec{F}_3 in the negative x direction. We obtain an acceleration along the $+x$ axis with magnitude

$$a = \frac{F_1 - F_2 - F_3}{m} = \frac{50 \text{ N} - 30 \text{ N} - 10 \text{ N}}{12 \text{ kg}} = 0.83 \text{ m/s}^2 .$$

- (c) In this case, the forces \vec{F}_2 and \vec{F}_3 are collectively strong enough to have y components (one positive and one negative) which cancel each other and still have enough x contributions (in the $-x$ direction) to cancel \vec{F}_1 . Since $|\vec{F}_2| = |\vec{F}_3|$, we see that the angle above the $-x$ axis to one of them should equal the angle below the $-x$ axis to the other one (we denote this angle θ). We require

$$\begin{aligned} -50 \text{ N} &= \vec{F}_{2x} + \vec{F}_{3x} \\ &= -(30 \text{ N}) \cos \theta - (30 \text{ N}) \cos \theta \end{aligned}$$

which leads to

$$\theta = \cos^{-1} \left(\frac{50 \text{ N}}{60 \text{ N}} \right) = 34^\circ .$$