

35. (a) Since the pipe is open at both ends there are displacement antinodes at both ends and an integer number of half-wavelengths fit into the length of the pipe. If L is the pipe length and λ is the wavelength then $\lambda = 2L/n$, where n is an integer. If v is the speed of sound then the resonant frequencies are given by $f = v/\lambda = nv/2L$. Now $L = 0.457$ m, so $f = n(344 \text{ m/s})/2(0.457 \text{ m}) = 376.4n$ Hz. To find the resonant frequencies that lie between 1000 Hz and 2000 Hz, first set $f = 1000$ Hz and solve for n , then set $f = 2000$ Hz and again solve for n . You should get 2.66 and 5.32. This means $n = 3, 4$, and 5 are the appropriate values of n . For $n = 3$, $f = 3(376.4 \text{ Hz}) = 1129$ Hz; for $n = 4$, $f = 4(376.4 \text{ Hz}) = 1526$ Hz; and for $n = 5$, $f = 5(376.4 \text{ Hz}) = 1882$ Hz.
- (b) For any integer value of n the displacement has n nodes and $n + 1$ antinodes, counting the ends. The nodes (N) and antinodes (A) are marked on the diagrams below for the three resonances found in part (a).

