

50. (a) We use Eq. 21-14. For configuration  $A$

$$W_A = \frac{N!}{(N/2)!(N/2)!} = \frac{50!}{(25!)(25!)} = 1.26 \times 10^{14} .$$

(b) For configuration  $B$

$$W_B = \frac{N!}{(0.6N)!(0.4N)!} = \frac{50!}{[0.6(50)]![0.4(50)]!} = 4.71 \times 10^{13} .$$

(c) Since all microstates are equally probable,

$$f = \frac{W_B}{W_A} = \frac{1265}{3393} \approx 0.37 .$$

(d) We use these formulas for  $N = 100$ :  $W_A = 1.01 \times 10^{29}$ ,  $W_B = 1.37 \times 10^{28}$ , and  $f \approx 0.14$ .

(e) For  $N = 200$  we have  $W_A = 9.05 \times 10^{58}$ ,  $W_B = 1.64 \times 10^{57}$ , and  $f = 0.018$ .

(f) We see from the calculation above that  $f$  decreases as  $N$  increases, as expected.