

18. (a) Regardless of the direction of the thrust, the change in linear momentum of the space probe is given by the impulse-momentum theorem (also using Eq. 10-8):

$$\Delta p = (3000 \text{ N})(65.0 \text{ s}) = 1.95 \times 10^5 \text{ kg}\cdot\text{m/s} .$$

- (b) The change in speed for the probe of mass m is

$$\Delta v = \frac{\Delta p}{m} = \frac{1.95 \times 10^5 \text{ kg}\cdot\text{m/s}}{2500 \text{ kg}} = 78.0 \text{ m/s} .$$

Let the initial and final speeds of the probe be v_i and v_f , respectively. Then, the change in its kinetic energy is $\Delta K = \frac{1}{2}m(v_f^2 - v_i^2)$. If the thrust is backward then $v_f = v_i - \Delta v$, and

$$\begin{aligned} \Delta K &= \frac{1}{2}m((v_i - \Delta v)^2 - v_i^2) \\ &= \frac{1}{2}(2500 \text{ kg})((300 \text{ m/s} - 78.0 \text{ m/s})^2 - (300 \text{ m/s})^2) \\ &= -5.09 \times 10^7 \text{ J} \end{aligned}$$

If the thrust is forward then $v_f = v_i + \Delta v$, and

$$\begin{aligned} \Delta K &= \frac{1}{2}m((v_i + \Delta v)^2 - v_i^2) \\ &= \frac{1}{2}(2500 \text{ kg})((300 \text{ m/s} + 78.0 \text{ m/s})^2 - (300 \text{ m/s})^2) \\ &= 6.61 \times 10^7 \text{ J} . \end{aligned}$$

If the thrust is sideways then $v_f = \sqrt{(\Delta v)^2 + v_i^2}$, and

$$\Delta K = \frac{1}{2}m((\Delta v)^2 + v_i^2 - v_i^2) = \frac{1}{2}(2500 \text{ kg})(78.0 \text{ m/s})^2 = 7.61 \times 10^6 \text{ J} .$$