

31. (a) The half-life $T_{1/2}$ and the disintegration constant are related by $T_{1/2} = (\ln 2)/\lambda$, so $T_{1/2} = (\ln 2)/(0.0108 \text{ h}^{-1}) = 64.2 \text{ h}$.
- (b) At time t , the number of undecayed nuclei remaining is given by

$$N = N_0 e^{-\lambda t} = N_0 e^{-(\ln 2)t/T_{1/2}} .$$

We substitute $t = 3T_{1/2}$ to obtain

$$\frac{N}{N_0} = e^{-3 \ln 2} = 0.125 .$$

In each half-life, the number of undecayed nuclei is reduced by half. At the end of one half-life, $N = N_0/2$, at the end of two half-lives, $N = N_0/4$, and at the end of three half-lives, $N = N_0/8 = 0.125N_0$.

- (c) We use

$$N = N_0 e^{-\lambda t} .$$

10.0 d is 240 h , so $\lambda t = (0.0108 \text{ h}^{-1})(240 \text{ h}) = 2.592$ and

$$\frac{N}{N_0} = e^{-2.592} = 0.0749 .$$