

49. (a) To hold the crate at equilibrium in the final situation, \vec{F} must have the same magnitude as the horizontal component of the rope's tension $T \sin \theta$, where θ is the angle between the rope (in the final position) and vertical:

$$\theta = \sin^{-1} \left(\frac{4.00}{12.0} \right) = 19.5^\circ .$$

But the vertical component of the tension supports against the weight: $T \cos \theta = mg$. Thus, the tension is $T = (230)(9.8) / \cos 19.5^\circ = 2391 \text{ N}$ and $F = (2391) \sin 19.5^\circ = 797 \text{ N}$. An alternative approach based on drawing a vector triangle (of forces) in the final situation provides a quick solution.

- (b) Since there is no change in kinetic energy, the net work on it is zero.
- (c) The work done by gravity is $W_g = \vec{F}_g \cdot \vec{d} = -mgh$, where $h = L(1 - \cos \theta)$ is the vertical component of the displacement. With $L = 12.0 \text{ m}$, we obtain $W_g = -1547 \text{ J}$ which should be rounded to three figures: -1.55 kJ .
- (d) The tension vector is everywhere perpendicular to the direction of motion, so its work is zero (since $\cos 90^\circ = 0$).
- (e) The implication of the previous three parts is that the work due to \vec{F} is $-W_g$ (so the net work turns out to be zero). Thus, $W_F = -W_g = 1.55 \text{ kJ}$.
- (f) Since \vec{F} does not have constant magnitude, we cannot expect Eq. 7-8 to apply.