

64. (a) For the isothermal process the final temperature of the gas is $T_f = T_i = 300$ K. The final pressure is

$$p_f = \frac{p_i V_i}{V_f} = \frac{(32 \text{ atm})(1.0 \text{ L})}{4.0 \text{ L}} = 8.0 \text{ atm} ,$$

and the work done is

$$\begin{aligned} W &= nRT_i \ln \left(\frac{V_f}{V_i} \right) = p_i V_i \ln \left(\frac{V_f}{V_i} \right) \\ &= (32 \text{ atm})(1.01 \times 10^5 \text{ Pa/atm})(1.0 \times 10^{-3} \text{ m}^3) \ln \left(\frac{4.0 \text{ L}}{1.0 \text{ L}} \right) \\ &= 4.4 \times 10^3 \text{ J} . \end{aligned}$$

- (b) For the adiabatic process $p_i V_i^\gamma = p_f V_f^\gamma$. Thus,

$$\begin{aligned} p_f &= p_i \left(\frac{V_i}{V_f} \right)^\gamma = (32 \text{ atm}) \left(\frac{1.0 \text{ L}}{4.0 \text{ L}} \right)^{5/3} = 3.2 \text{ atm} , \\ T_f &= \frac{p_f V_f T_i}{p_i V_i} = \frac{(3.2 \text{ atm})(4.0 \text{ L})(300 \text{ K})}{(32 \text{ atm})(1.0 \text{ L})} = 120 \text{ K} , \text{ and} \\ W &= Q - \Delta E_{\text{int}} = -\Delta E_{\text{int}} = -\frac{3}{2} nR\Delta T = -\frac{3}{2} (p_f V_f - p_i V_i) \\ &= -\frac{3}{2} [(3.2 \text{ atm})(4.0 \text{ L}) - (32 \text{ atm})(1.0 \text{ L})](1.01 \times 10^5 \text{ Pa/atm})(10^{-3} \text{ m}^3/\text{L}) \\ &= 2.9 \times 10^3 \text{ J} . \end{aligned}$$

- (c) Now, $\gamma = 1.4$ so

$$\begin{aligned} p_f &= p_i \left(\frac{V_i}{V_f} \right)^\gamma = (32 \text{ atm}) \left(\frac{1.0 \text{ L}}{4.0 \text{ L}} \right)^{1.4} = 4.6 \text{ atm} , \\ T_f &= \frac{p_f V_f T_i}{p_i V_i} = \frac{(4.6 \text{ atm})(4.0 \text{ L})(300 \text{ K})}{(32 \text{ atm})(1.0 \text{ L})} = 170 \text{ K} , \text{ and} \\ W &= Q - \Delta E_{\text{int}} = -\frac{5}{2} nR\Delta T = -\frac{5}{2} (p_f V_f - p_i V_i) \\ &= -\frac{5}{2} [(4.6 \text{ atm})(4.0 \text{ L}) - (32 \text{ atm})(1.0 \text{ L})](1.01 \times 10^5 \text{ Pa/atm})(10^{-3} \text{ m}^3/\text{L}) \\ &= 3.4 \times 10^3 \text{ J} . \end{aligned}$$