

62. We use $B(x, y, z) = (\mu_0/4\pi)i \Delta \vec{s} \times \vec{r}/r^3$, where $\Delta \vec{s} = \Delta s \hat{j}$ and $\vec{r} = x\hat{i} + y\hat{j} + z\hat{k}$. Thus,

$$\vec{B}(x, y, z) = \left(\frac{\mu_0}{4\pi}\right) \frac{i \Delta s \hat{j} \times (x\hat{i} + y\hat{j} + z\hat{k})}{(x^2 + y^2 + z^2)^{3/2}} = \frac{\mu_0 i \Delta s (z\hat{i} - x\hat{k})}{4\pi(x^2 + y^2 + z^2)^{3/2}} .$$

(a) The field on the z axis (at $z = 5.0$ m) is

$$\begin{aligned} \vec{B}(0, 0, 5.0 \text{ m}) &= \frac{(4\pi \times 10^{-7} \text{ T} \cdot \text{m/A})(2.0 \text{ A})(3.0 \times 10^{-2} \text{ m})(5.0 \text{ m})\hat{i}}{4\pi(0^2 + 0^2 + (5.0 \text{ m})^2)^{3/2}} \\ &= 2.4 \times 10^{-10} \text{ T } \hat{i} . \end{aligned}$$

(b) $\vec{B}(0, 6.0 \text{ m}, 0)$, since $x = z = 0$.

(c) The field in the xy plane, at $(x, y) = (7, 7)$, is

$$\begin{aligned} \vec{B}(7.0 \text{ m}, 7.0 \text{ m}, 0) &= \frac{(4\pi \times 10^{-7} \text{ T} \cdot \text{m/A})(2.0 \text{ A})(3.0 \times 10^{-2} \text{ m})(-7.0 \text{ m})\hat{k}}{4\pi((7.0 \text{ m})^2 + (7.0 \text{ m})^2 + 0^2)^{3/2}} \\ &= 4.3 \times 10^{-11} \text{ T } \hat{k} . \end{aligned}$$

(d) The field in the xy plane, at $(x, y) = (-3, -4)$, is

$$\begin{aligned} \vec{B}(-3.0 \text{ m}, -4.0 \text{ m}, 0) &= \frac{(4\pi \times 10^{-7} \text{ T} \cdot \text{m/A})(2.0 \text{ A})(3.0 \times 10^{-2} \text{ m})(3.0 \text{ m})\hat{k}}{4\pi((-3.0 \text{ m})^2 + (-4.0 \text{ m})^2 + 0^2)^{3/2}} \\ &= 1.4 \times 10^{-10} \text{ T } \hat{k} . \end{aligned}$$