

48. (a) We consider the radial field produced at points within a uniform cylindrical distribution of charge. The volume enclosed by a Gaussian surface in this case is  $L\pi r^2$ . Thus, Gauss' law leads to

$$E = \frac{|q_{\text{enc}}|}{\varepsilon_0 A_{\text{cylinder}}} = \frac{|\rho| (L\pi r^2)}{\varepsilon_0 (2\pi r L)} = \frac{|\rho| r}{2\varepsilon_0} .$$

- (b) We note from the above expression that the magnitude of the radial field grows with  $r$ .  
(c) Since the charged powder is negative, the field points radially inward.  
(d) The largest value of  $r$  which encloses charged material is  $r_{\text{max}} = R$ . Therefore, with  $|\rho| = 0.0011 \text{ C/m}^3$  and  $R = 0.050 \text{ m}$ , we obtain

$$E_{\text{max}} = \frac{|\rho| R}{2\varepsilon_0} = 3.1 \times 10^6 \text{ N/C} .$$

- (e) According to condition 1 mentioned in the problem, the field is high enough to produce an electrical discharge (at  $r = R$ ).