

29. The magnitudes of the forces on the sides of the rectangle which are parallel to the long straight wire (with $i_1 = 30$ A) are computed using Eq. 30-15, but the force on each of the sides lying perpendicular to it (along our y axis, with the origin at the top wire and $+y$ downward) would be figured by integrating as follows:

$$F_{\perp \text{ sides}} = \int_a^{a+b} \frac{i_2 \mu_0 i_1}{2\pi y} dy .$$

Fortunately, these forces on the two perpendicular sides of length b cancel out. For the remaining two (parallel) sides of length L , we obtain

$$\begin{aligned} F &= \frac{\mu_0 i_1 i_2 L}{2\pi} \left(\frac{1}{a} - \frac{1}{a+d} \right) = \frac{\mu_0 i_1 i_2 b}{2\pi a(a+b)} \\ &= \frac{(4\pi \times 10^{-7} \text{ T}\cdot\text{m/A})(30 \text{ A})(20 \text{ A})(8.0 \text{ cm})(30 \times 10^{-2} \text{ m})}{2\pi(1.0 \text{ cm} + 8.0 \text{ cm})} \\ &= 3.2 \times 10^{-3} \text{ N} , \end{aligned}$$

and \vec{F} points toward the wire.