

29. (a) The net work done is the rectangular “area” enclosed in the  $pV$  diagram:

$$W = (V - V_0)(p - p_0) = (2V_0 - V_0)(2p_0 - p_0) = V_0 p_0 .$$

Inserting the values stated in the problem, we obtain  $W = 2.27$  kJ.

- (b) We compute the energy added as heat during the “heat-intake” portions of the cycle using Eq. 20-39, Eq. 20-43, and Eq. 20-46:

$$\begin{aligned} Q_{abc} &= nC_V(T_b - T_a) + nC_p(T_c - T_b) \\ &= n\left(\frac{3}{2}R\right)T_a\left(\frac{T_b}{T_a} - 1\right) + n\left(\frac{5}{2}R\right)T_a\left(\frac{T_c}{T_a} - \frac{T_b}{T_a}\right) \\ &= nRT_a\left(\frac{3}{2}\left(\frac{T_b}{T_a} - 1\right) + \frac{5}{2}\left(\frac{T_c}{T_a} - \frac{T_b}{T_a}\right)\right) \\ &= p_0V_0\left(\frac{3}{2}(2 - 1) + \frac{5}{2}(4 - 2)\right) = \frac{13}{2}p_0V_0 \end{aligned}$$

where, to obtain the last line, the gas law in ratio form has been used (see Sample Problem 20-1). Therefore, since  $W = p_0V_0$ , we have  $Q_{abc} = 13W/2 = 14.8$  kJ.

- (c) The efficiency is given by Eq. 21-9:

$$\varepsilon = \frac{W}{|Q_H|} = \frac{2}{13} = 0.154 = 15.4\% .$$

- (d) A Carnot engine operating between  $T_c$  and  $T_a$  has efficiency equal to

$$\varepsilon = 1 - \frac{T_a}{T_c} = 1 - \frac{1}{4} = 0.750 = 75.0\%$$

where the gas law in ratio form has been used. This is greater than our result in part (c), as expected from the second law of thermodynamics.