

49. Energy and momentum are conserved. We assume the residual thorium nucleus is in its ground state. Let  $K_\alpha$  be the kinetic energy of the alpha particle and  $K_{\text{Th}}$  be the kinetic energy of the thorium nucleus. Then,  $Q = K_\alpha + K_{\text{Th}}$ . We assume the uranium nucleus is initially at rest. Then, conservation of momentum yields  $0 = p_\alpha + p_{\text{Th}}$ , where  $p_\alpha$  is the momentum of the alpha particle and  $p_{\text{Th}}$  is the momentum of the thorium nucleus. Both particles travel slowly enough that the classical relationship between momentum and energy can be used. Thus  $K_{\text{Th}} = p_{\text{Th}}^2/2m_{\text{Th}}$ , where  $m_{\text{Th}}$  is the mass of the thorium nucleus. We substitute  $p_{\text{Th}} = -p_\alpha$  and use  $K_\alpha = p_\alpha^2/2m_\alpha$  to obtain  $K_{\text{Th}} = (m_\alpha/m_{\text{Th}})K_\alpha$ . Consequently,

$$Q = K_\alpha + \frac{m_\alpha}{m_{\text{Th}}}K_\alpha = \left(1 + \frac{m_\alpha}{m_{\text{Th}}}\right) K_\alpha = \left(1 + \frac{4.00 \text{ u}}{234 \text{ u}}\right) (4.196 \text{ MeV}) = 4.27 \text{ MeV} .$$