

22. (a) Since $A = \pi D^2/4$, we have the differential $dA = 2(\pi D/4)dD$. Dividing the latter relation by the former, we obtain $dA/A = 2 dD/D$. In terms of Δ 's, this reads

$$\frac{\Delta A}{A} = 2 \frac{\Delta D}{D} \quad \text{for} \quad \frac{\Delta D}{D} \ll 1 .$$

We can think of the factor of 2 as being due to the fact that area is a two-dimensional quantity. Therefore, the area increases by $2(0.18\%) = 0.36\%$.

- (b) Assuming that all dimension are allowed to freely expand, then the thickness increases by 0.18%.
(c) The volume (a three-dimensional quantity) increases by $3(0.18\%) = 0.54\%$.
(d) The mass does not change.
(e) The coefficient of linear expansion is

$$\alpha = \frac{\Delta D}{D \Delta T} = \frac{0.18 \times 10^{-2}}{100^\circ\text{C}} = 18 \times 10^{-6}/^\circ\text{C} .$$