

14. (a) The value of  $l$  satisfies  $\sqrt{l(l+1)}\hbar \approx \sqrt{l^2}\hbar = l\hbar = L$ , so  $l \simeq L/\hbar \simeq 3 \times 10^{74}$ .  
 (b) The number is  $2l+1 \approx 2(3 \times 10^{74}) = 6 \times 10^{74}$ .  
 (c) Since

$$\cos \theta_{\min} = \frac{m_{l\max}\hbar}{\sqrt{l(l+1)}\hbar} = \frac{l}{\sqrt{l(l+1)}} \approx 1 - \frac{1}{2l} = 1 - \frac{1}{2(3 \times 10^{74})}$$

or  $\cos \theta_{\min} \simeq 1 - \theta_{\min}^2/2 \approx 1 - 10^{-74}/6$ , we have  $\theta_{\min} \simeq \sqrt{10^{-74}/3} = 6 \times 10^{-38}$  rad. The correspondence principle requires that all the quantum effects vanish as  $\hbar \rightarrow 0$ . In this case  $\hbar/L$  is extremely small so the quantization effects are barely existent, with  $\theta_{\min} \simeq 10^{-38}$  rad  $\simeq 0$ .