

72. (a) We denote the mass of the car (and cannon) as M (excluding that of the cannonballs) and the mass of all the cannonballs as m . For concreteness, we assume that before firing all the cannonballs are at the front (left side of Fig. 9-52) of the car, which we choose to be the origin of the x axis; we choose $+x$ rightward. The coordinate of the center of mass of the car-cannonball system is

$$x_{\text{com}} = \frac{(0)m + \left(\frac{L}{2}\right)M}{M + m} = \frac{LM}{2(M + m)} .$$

After the firing, we assume all the cannonballs are at the other end of the car; the train will have moved (in the negative x direction) by a distance d , at which time

$$x_{\text{com}} = \frac{\left(\frac{L}{2} - d\right)M + (L - d)m}{M + m} .$$

Equating the two expressions, we obtain $d = \frac{mL}{M+m} < L$. If $m \gg M$, the distance d can be very close to (but can never exceed) L . Thus $d_{\text{max}} = L$.

- (b) After each impact, there is no relative motion in the system; thus, the final speed of the car is equal to that of the center of mass of the system, which is zero.