

60. (a) The energy delivered by the battery is the integral of Eq. 28-14 (where we use Eq. 31-43 for the current):

$$\begin{aligned}
 \int_0^t P_{\text{battery}} dt &= \int_0^t \frac{\mathcal{E}^2}{R} (1 - e^{-Rt/L}) dt = \frac{\mathcal{E}^2}{R} \left[t + \frac{L}{R} (e^{-Rt/L} - 1) \right] \\
 &= \frac{(10.0 \text{ V})^2}{6.70 \Omega} \left[2.00 \text{ s} + \frac{(5.50 \text{ H}) (e^{-(6.70 \Omega)(2.00 \text{ s})/5.50 \text{ H}} - 1)}{6.70 \Omega} \right] \\
 &= 18.7 \text{ J} .
 \end{aligned}$$

- (b) The energy stored in the magnetic field is given by Eq. 31-51:

$$\begin{aligned}
 U_B &= \frac{1}{2} Li^2(t) = \frac{1}{2} L \left(\frac{\mathcal{E}}{R} \right)^2 (1 - e^{-Rt/L})^2 \\
 &= \frac{1}{2} (5.50 \text{ H}) \left(\frac{10.0 \text{ V}}{6.70 \Omega} \right)^2 \left[1 - e^{-(6.70 \Omega)(2.00 \text{ s})/5.50 \text{ H}} \right]^2 \\
 &= 5.10 \text{ J} .
 \end{aligned}$$

- (c) The difference of the previous two results gives the amount “lost” in the resistor: $18.7 \text{ J} - 5.10 \text{ J} = 13.6 \text{ J}$.