

31. We denote the magnitude of the frictional force  $\alpha v$ , where  $\alpha = 70 \text{ N} \cdot \text{s/m}$ . We take the direction of the boat's motion to be positive. Newton's second law gives

$$-\alpha v = m \frac{dv}{dt} .$$

Thus,

$$\int_{v_0}^v \frac{dv}{v} = -\frac{\alpha}{m} \int_0^t dt$$

where  $v_0$  is the velocity at time zero and  $v$  is the velocity at time  $t$ . The integrals are evaluated with the result

$$\ln \frac{v}{v_0} = -\frac{\alpha t}{m} .$$

We take  $v = v_0/2$  and solve for time:

$$t = \frac{m}{\alpha} \ln 2 = \frac{1000 \text{ kg}}{70 \text{ N} \cdot \text{s/m}} \ln 2 = 9.9 \text{ s} .$$