

94. (First problem in **Cluster 1**)

We take the bottom of the incline to be the  $y = 0$  reference level. The incline angle is  $\theta = 30^\circ$ . The distance along the incline  $d$  (measured from the bottom) is related to height  $y$  by the relation  $y = d \sin \theta$ .

(a) Using the conservation of energy, we have

$$K_0 + U_0 = K_{\text{top}} + U_{\text{top}} \implies \frac{1}{2}mv_0^2 + 0 = 0 + mgy$$

with  $v_0 = 5.0$  m/s. This yields  $y = 1.3$  m, from which we obtain  $d = 2.6$  m.

(b) An analysis of forces in the manner of Chapter 6 reveals that the magnitude of the friction force is  $f_k = \mu_k mg \cos \theta$ . Now, we write Eq. 8-31 as

$$\begin{aligned} K_0 + U_0 &= K_{\text{top}} + U_{\text{top}} + f_k d \\ \frac{1}{2}mv_0^2 + 0 &= 0 + mgy + f_k d \\ \frac{1}{2}mv_0^2 &= mgd \sin \theta + \mu_k mgd \cos \theta \end{aligned}$$

which – upon cancelling the mass and rearranging – provides the result for  $d$ :

$$d = \frac{v_0^2}{2g(\mu_k \cos \theta + \sin \theta)} = 1.5 \text{ m} .$$

(c) The thermal energy generated by friction is  $f_k d = \mu_k mgd \cos \theta = 26$  J.

(d) The slide back down, from the height  $y = 1.5 \sin 30^\circ$  is also described by Eq. 8-31. With  $\Delta E_{\text{th}}$  again equal to 26 J, we have

$$K_{\text{top}} + U_{\text{top}} = K_{\text{bot}} + U_{\text{bot}} + f_k d \implies 0 + mgy = \frac{1}{2}mv_{\text{bot}}^2 + 0 + 26$$

from which we find  $v_{\text{bot}} = 2.1$  m/s.