

20. (a) The first step is to add energy to produce ${}^4\text{He} \rightarrow p + {}^3\text{H}$, which – to make the electrons “balance” – may be rewritten as ${}^4\text{He} \rightarrow {}^1\text{H} + {}^3\text{H}$. The energy needed is $\Delta E_1 = (m_{{}^3\text{H}} + m_{{}^1\text{H}} - m_{{}^4\text{He}})c^2 = (3.01605 \text{ u} + 1.00783 \text{ u} - 4.00260 \text{ u})(931.5 \text{ MeV/u}) = 19.8 \text{ MeV}$. The second step is to add energy to produce ${}^3\text{H} \rightarrow n + {}^2\text{H}$. The energy needed is $\Delta E_2 = (m_{{}^2\text{H}} + m_n - m_{{}^3\text{H}})c^2 = (2.01410 \text{ u} + 1.00867 \text{ u} - 3.01605 \text{ u})(931.5 \text{ MeV/u}) = 6.26 \text{ MeV}$. The third step: ${}^2\text{H} \rightarrow p + n$, which – to make the electrons “balance” – may be rewritten as ${}^2\text{H} \rightarrow {}^1\text{H} + n$. The work required is $\Delta E_3 = (m_{{}^1\text{H}} + m_n - m_{{}^2\text{H}})c^2 = (1.00783 \text{ u} + 1.00867 \text{ u} - 2.01410 \text{ u})(931.5 \text{ MeV/u}) = 2.23 \text{ MeV}$.
- (b) The total binding energy is $\Delta E_{\text{be}} = \Delta E_1 + \Delta E_2 + \Delta E_3 = 19.8 \text{ MeV} + 6.26 \text{ MeV} + 2.23 \text{ MeV} = 28.3 \text{ MeV}$.
- (c) The binding energy per nucleon is $\Delta E_{\text{ben}} = \Delta E_{\text{be}}/A = 28.3 \text{ MeV}/4 = 7.07 \text{ MeV}$.