

83. When the switch is open, we have a series  $LRC$  circuit involving just the one capacitor near the upper right corner. Eq. 33-65 leads to

$$\frac{\omega_d L - \frac{1}{\omega_d C}}{R} = \tan \phi_o = \tan(-20^\circ) = -\tan 20^\circ .$$

Now, when the switch is in position 1, the equivalent capacitance in the circuit is  $2C$ . In this case, we have

$$\frac{\omega_d L - \frac{1}{2\omega_d C}}{R} = \tan \phi_1 = \tan 10.0^\circ .$$

Finally, with the switch in position 2, the circuit is simply an  $LC$  circuit with current amplitude

$$I_2 = \frac{\mathcal{E}_m}{Z_{LC}} = \frac{\mathcal{E}_m}{\sqrt{\left(\omega_d L - \frac{1}{\omega_d C}\right)^2}} = \frac{\mathcal{E}_m}{\frac{1}{\omega_d C} - \omega_d L}$$

where we use the fact that  $\frac{1}{\omega_d C} > \omega_d L$  in simplifying the square root (this fact is evident from the description of the first situation, when the switch was open). We solve for  $L$ ,  $R$  and  $C$  from the three equations above:

$$\begin{aligned} R &= \frac{-\mathcal{E}_m}{I_2 \tan \phi_o} = \frac{120 \text{ V}}{(2.00 \text{ A}) \tan 20.0^\circ} = 165 \text{ } \Omega \\ C &= \frac{I_2}{2\omega_d \mathcal{E}_m \left(1 - \frac{\tan \phi_1}{\tan \phi_o}\right)} = \frac{2.00 \text{ A}}{2(2\pi)(60.0 \text{ Hz})(120 \text{ V}) \left(1 + \frac{\tan 10.0^\circ}{\tan 20.0^\circ}\right)} = 1.49 \times 10^{-5} \text{ F} \\ L &= \frac{\mathcal{E}_m}{\omega_d I_2} \left(1 - 2 \frac{\tan \phi_1}{\tan \phi_o}\right) = \frac{120 \text{ V}}{2\pi(60.0 \text{ Hz})(2.00 \text{ A})} \left(1 + 2 \frac{\tan 10.0^\circ}{\tan 20.0^\circ}\right) = 0.313 \text{ H} \end{aligned}$$