

33. (a) The power is given by $P = Fv$ and the work done by \vec{F} from time t_1 to time t_2 is given by

$$W = \int_{t_1}^{t_2} P \, dt = \int_{t_1}^{t_2} Fv \, dt .$$

Since \vec{F} is the net force, the magnitude of the acceleration is $a = F/m$, and, since the initial velocity is $v_0 = 0$, the velocity as a function of time is given by $v = v_0 + at = (F/m)t$. Thus

$$W = \int_{t_1}^{t_2} (F^2/m)t \, dt = \frac{1}{2}(F^2/m)(t_2^2 - t_1^2) .$$

For $t_1 = 0$ and $t_2 = 1.0$ s,

$$W = \frac{1}{2} \left(\frac{(5.0 \, \text{N})^2}{15 \, \text{kg}} \right) (1.0 \, \text{s})^2 = 0.83 \, \text{J} .$$

- (b) For $t_1 = 1.0$ s and $t_2 = 2.0$ s,

$$W = \frac{1}{2} \left(\frac{(5.0 \, \text{N})^2}{15 \, \text{kg}} \right) ((2.0 \, \text{s})^2 - (1.0 \, \text{s})^2) = 2.5 \, \text{J} .$$

- (c) For $t_1 = 2.0$ s and $t_2 = 3.0$ s,

$$W = \frac{1}{2} \left(\frac{(5.0 \, \text{N})^2}{15 \, \text{kg}} \right) ((3.0 \, \text{s})^2 - (2.0 \, \text{s})^2) = 4.2 \, \text{J} .$$

- (d) Substituting $v = (F/m)t$ into $P = Fv$ we obtain $P = F^2t/m$ for the power at any time t . At the end of the third second

$$P = \frac{(5.0 \, \text{N})^2(3.0 \, \text{s})}{15 \, \text{kg}} = 5.0 \, \text{W} .$$