

27. (a) If v is the speed of the positron then $v \sin \phi$ is the component of its velocity in the plane that is perpendicular to the magnetic field. Here ϕ is the angle between the velocity and the field (89°). Newton's second law yields $eBv \sin \phi = m_e(v \sin \phi)^2/r$, where r is the radius of the orbit. Thus $r = (m_e v / eB) \sin \phi$. The period is given by

$$T = \frac{2\pi r}{v \sin \phi} = \frac{2\pi m_e}{eB} = \frac{2\pi(9.11 \times 10^{-31} \text{ kg})}{(1.60 \times 10^{-19} \text{ C})(0.10 \text{ T})} = 3.6 \times 10^{-10} \text{ s} .$$

The equation for r is substituted to obtain the second expression for T .

- (b) The pitch is the distance traveled along the line of the magnetic field in a time interval of one period. Thus $p = vT \cos \phi$. We use the kinetic energy to find the speed: $K = \frac{1}{2}m_e v^2$ means

$$v = \sqrt{\frac{2K}{m_e}} = \sqrt{\frac{2(2.0 \times 10^3 \text{ eV})(1.60 \times 10^{-19} \text{ J/eV})}{9.11 \times 10^{-31} \text{ kg}}} = 2.651 \times 10^7 \text{ m/s} .$$

Thus

$$p = (2.651 \times 10^7 \text{ m/s})(3.58 \times 10^{-10} \text{ s}) \cos 89^\circ = 1.7 \times 10^{-4} \text{ m} .$$

- (c) The orbit radius is

$$R = \frac{m_e v \sin \phi}{eB} = \frac{(9.11 \times 10^{-31} \text{ kg})(2.651 \times 10^7 \text{ m/s}) \sin 89^\circ}{(1.60 \times 10^{-19} \text{ C})(0.10 \text{ T})} = 1.5 \times 10^{-3} \text{ m} .$$