

31. (a) The work done by you in moving the sphere of mass m_2 equals the change in the potential energy of the three-sphere system. The initial potential energy is

$$U_i = -\frac{Gm_1m_2}{d} - \frac{Gm_1m_3}{L} - \frac{Gm_2m_3}{L-d}$$

and the final potential energy is

$$U_f = -\frac{Gm_1m_2}{L-d} - \frac{Gm_1m_3}{L} - \frac{Gm_2m_3}{d} .$$

The work done is

$$\begin{aligned} W &= U_f - U_i = Gm_2 \left(m_1 \left(\frac{1}{d} - \frac{1}{L-d} \right) + m_3 \left(\frac{1}{L-d} - \frac{1}{d} \right) \right) \\ &= (6.67 \times 10^{-11} \text{ m}^3/\text{s}^2 \cdot \text{kg})(0.10 \text{ kg}) \left[(0.80 \text{ kg}) \left(\frac{1}{0.040 \text{ m}} - \frac{1}{0.080 \text{ m}} \right) \right. \\ &\quad \left. + (0.20 \text{ kg}) \left(\frac{1}{0.080 \text{ m}} - \frac{1}{0.040 \text{ m}} \right) \right] \\ &= +5.0 \times 10^{-11} \text{ J} . \end{aligned}$$

- (b) The work done by the force of gravity is $-(U_f - U_i) = -5.0 \times 10^{-11} \text{ J}$.