

69. (a) We are told

$$e^{-bt/2m} = \frac{3}{4} \quad \text{where } t = 4T$$

where $T = 2\pi/\omega' \approx 2\pi\sqrt{m/k}$ (neglecting the second term in Eq. 16.41). Thus,

$$T \approx 2\pi\sqrt{(2.00\text{ kg})/(10.0\text{ N/m})} = 2.81\text{ s}$$

and we find

$$\frac{b(4T)}{2m} = \ln\left(\frac{4}{3}\right) = 0.288 \implies b = \frac{2(2.00)(0.288)}{4(2.81)} = 0.102\text{ kg/s}.$$

(b) Initially, the energy is $E_o = \frac{1}{2}kx_{mo}^2 = \frac{1}{2}(10.0)(0.250)^2 = 0.313\text{ J}$. At $t = 4T$, $E = \frac{1}{2}k(\frac{3}{4}x_{mo})^2 = 0.176\text{ J}$. Therefore, $E_o - E = 0.137\text{ J}$.