

57. (a) The four tires act as resistors in parallel, with an equivalent value given by

$$\frac{1}{R_{\text{eq}}} = \sum_{n=1}^4 \frac{1}{R_{\text{tire}}} = \frac{4}{R_{\text{tire}}} \implies R_{\text{eq}} = \frac{R_{\text{tire}}}{4} .$$

Using the stated values ( $C = 5.0 \times 10^{-10} \text{ F}$  and  $10^8 \Omega < R_{\text{tire}} < 10^{11} \Omega$ ) we find the capacitive time constant  $\tau = R_{\text{eq}}C$  in the range  $0.012 \text{ s} < \tau < 13 \text{ s}$ .

- (b) Eq. 26-22 leads to

$$U_0 = \frac{1}{2}CV^2 = \frac{1}{2} (5.00 \times 10^{-10} \text{ F}) (30.0 \times 10^3 \text{ V})^2 = 0.225 \text{ J} .$$

- (c) As demonstrated in Sample Problem 28-5, the energy “decays” exponentially according to

$$U = U_0 e^{-2t/\tau} .$$

Solving for the time which gives  $U = 0.050 \text{ J}$ , we find

$$t = \frac{\tau}{2} \ln\left(\frac{U_0}{U}\right) = \frac{\tau}{2} \ln\left(\frac{0.225}{0.050}\right)$$

which yields, for the range of time constants found in part (a), values of  $t$  in the range  $0.094 \text{ s} < t < 9.4 \text{ s}$ . To obtain these particular values, we used 3-figure versions of the part (a) results ( $0.0125 \text{ s} < \tau < 12.5 \text{ s}$ ).

- (d) The lower range of resistance leads to the smaller times to discharge, which is the more desirable situation. Based on this criterion, low resistance tires are favored.
- (e) There are a variety of ways to safely and quickly ground a large charged object. A large metal cable connected to, say, the (metal) building frame and held at the end of, say, a long lucite rod might be used (to touch a part of the car that does not have much paint or grease on it) to make the car safe to handle.