

45. (a) If  $r$  is the radius of the orbit then the magnitude of the gravitational force acting on the satellite is given by  $GMm/r^2$ , where  $M$  is the mass of Earth and  $m$  is the mass of the satellite. The magnitude of the acceleration of the satellite is given by  $v^2/r$ , where  $v$  is its speed. Newton's second law yields  $GMm/r^2 = mv^2/r$ . Since the radius of Earth is  $6.37 \times 10^6$  m the orbit radius is  $r = 6.37 \times 10^6 \text{ m} + 160 \times 10^3 \text{ m} = 6.53 \times 10^6 \text{ m}$ . The solution for  $v$  is

$$v = \sqrt{\frac{GM}{r}} = \sqrt{\frac{(6.67 \times 10^{-11} \text{ m}^3/\text{s}^2 \cdot \text{kg})(5.98 \times 10^{24} \text{ kg})}{6.53 \times 10^6 \text{ m}}} = 7.82 \times 10^3 \text{ m/s} .$$

- (b) Since the circumference of the circular orbit is  $2\pi r$ , the period is

$$T = \frac{2\pi r}{v} = \frac{2\pi(6.53 \times 10^6 \text{ m})}{7.82 \times 10^3 \text{ m/s}} = 5.25 \times 10^3 \text{ s} .$$

This is equivalent to 87.4 min.