

59. (a) If the battery is applied at time $t = 0$ the current is given by

$$i = \frac{\mathcal{E}}{R} \left(1 - e^{-t/\tau_L} \right) ,$$

where \mathcal{E} is the emf of the battery, R is the resistance, and τ_L is the inductive time constant (L/R). This leads to

$$e^{-t/\tau_L} = 1 - \frac{iR}{\mathcal{E}} \implies -\frac{t}{\tau_L} = \ln \left(1 - \frac{iR}{\mathcal{E}} \right) .$$

Since

$$\ln \left(1 - \frac{iR}{\mathcal{E}} \right) = \ln \left[1 - \frac{(2.00 \times 10^{-3} \text{ A})(10.0 \times 10^3 \Omega)}{50.0 \text{ V}} \right] = -0.5108 ,$$

the inductive time constant is $\tau_L = t/0.5108 = (5.00 \times 10^{-3} \text{ s})/0.5108 = 9.79 \times 10^{-3} \text{ s}$ and the inductance is

$$L = \tau_L R = (9.79 \times 10^{-3} \text{ s})(10.0 \times 10^3 \Omega) = 97.9 \text{ H} .$$

- (b) The energy stored in the coil is

$$U_B = \frac{1}{2} L i^2 = \frac{1}{2} (97.9 \text{ H})(2.00 \times 10^{-3} \text{ A})^2 = 1.96 \times 10^{-4} \text{ J} .$$