

27. Let  $f$  be the fraction of the incident beam intensity that is reflected. The fraction absorbed is  $1 - f$ . The reflected portion exerts a radiation pressure of

$$p_r = \frac{2fI_0}{c}$$

and the absorbed portion exerts a radiation pressure of

$$p_a = \frac{(1 - f)I_0}{c},$$

where  $I_0$  is the incident intensity. The factor 2 enters the first expression because the momentum of the reflected portion is reversed. The total radiation pressure is the sum of the two contributions:

$$p_{\text{total}} = p_r + p_a = \frac{2fI_0 + (1 - f)I_0}{c} = \frac{(1 + f)I_0}{c}.$$

To relate the intensity and energy density, we consider a tube with length  $\ell$  and cross-sectional area  $A$ , lying with its axis along the propagation direction of an electromagnetic wave. The electromagnetic energy inside is  $U = uA\ell$ , where  $u$  is the energy density. All this energy passes through the end in time  $t = \ell/c$ , so the intensity is

$$I = \frac{U}{At} = \frac{uA\ell c}{A\ell} = uc.$$

Thus  $u = I/c$ . The intensity and energy density are positive, regardless of the propagation direction. For the partially reflected and partially absorbed wave, the intensity just outside the surface is  $I = I_0 + fI_0 = (1 + f)I_0$ , where the first term is associated with the incident beam and the second is associated with the reflected beam. Consequently, the energy density is

$$u = \frac{I}{c} = \frac{(1 + f)I_0}{c},$$

the same as radiation pressure.