

43. (a) Let  $M$  be the mass of the Sun at time  $t$  and  $E$  be the energy radiated to that time. Then, the power output is  $P = dE/dt = (dM/dt)c^2$ , where  $E = Mc^2$  is used. At the present time,

$$\frac{dM}{dt} = \frac{P}{c^2} = \frac{3.9 \times 10^{26} \text{ W}}{(2.998 \times 10^8 \text{ m/s})^2} = 4.33 \times 10^9 \text{ kg/s} .$$

- (b) We assume the rate of mass loss remained constant. Then, the total mass loss is  $\Delta M = (dM/dt) \Delta t = (4.33 \times 10^9 \text{ kg/s})(4.5 \times 10^9 \text{ y})(3.156 \times 10^7 \text{ s/y}) = 6.15 \times 10^{26} \text{ kg}$ . The fraction lost is

$$\frac{\Delta M}{M + \Delta M} = \frac{6.15 \times 10^{26} \text{ kg}}{2.0 \times 10^{30} \text{ kg} + 6.15 \times 10^{26} \text{ kg}} = 3.07 \times 10^{-4} .$$