

42. (a) Since $P = i^2 R = J^2 A^2 R$, the current density is

$$\begin{aligned} J &= \frac{1}{A} \sqrt{\frac{P}{R}} = \frac{1}{A} \sqrt{\frac{P}{\rho L/A}} = \sqrt{\frac{P}{\rho L A}} \\ &= \sqrt{\frac{1.0 \text{ W}}{\pi (3.5 \times 10^{-5} \Omega \cdot \text{m}) (2.0 \times 10^{-2} \text{ m}) (5.0 \times 10^{-3} \text{ m})^2}} = 1.3 \times 10^5 \text{ A/m}^2 . \end{aligned}$$

(b) From $P = iV = JAV$ we get

$$V = \frac{P}{AJ} = \frac{P}{\pi r^2 J} = \frac{1.0 \text{ W}}{\pi (5.0 \times 10^{-3} \text{ m})^2 (1.3 \times 10^5 \text{ A/m}^2)} = 9.4 \times 10^{-2} \text{ V} .$$