

53. The average acceleration during contact with the floor is given by  $a_{\text{avg}} = (v_2 - v_1)/\Delta t$ , where  $v_1$  is its velocity just before striking the floor,  $v_2$  is its velocity just as it leaves the floor, and  $\Delta t$  is the duration of contact with the floor ( $12 \times 10^{-3}$  s). Taking the  $y$  axis to be positively upward and placing the origin at the point where the ball is dropped, we first find the velocity just before striking the floor, using  $v_1^2 = v_0^2 - 2gy$ . With  $v_0 = 0$  and  $y = -4.00$  m, the result is

$$v_1 = -\sqrt{-2gy} = -\sqrt{-2(9.8)(-4.00)} = -8.85 \text{ m/s}$$

where the negative root is chosen because the ball is traveling downward. To find the velocity just after hitting the floor (as it ascends without air friction to a height of 2.00 m), we use  $v^2 = v_2^2 - 2g(y - y_0)$  with  $v = 0$ ,  $y = -2.00$  m (it ends up two meters *below* its initial drop height), and  $y_0 = -4.00$  m. Therefore,

$$v_2 = \sqrt{2g(y - y_0)} = \sqrt{2(9.8)(-2.00 + 4.00)} = 6.26 \text{ m/s} .$$

Consequently, the average acceleration is

$$a_{\text{avg}} = \frac{v_2 - v_1}{\Delta t} = \frac{6.26 + 8.85}{12.0 \times 10^{-3}} = 1.26 \times 10^3 \text{ m/s}^2 .$$

The positive nature of the result indicates that the acceleration vector points upward. In a later chapter, this will be directly related to the magnitude and direction of the force exerted by the ground on the ball during the collision.