

83. (a) Using Kepler's law of periods, we obtain

$$T = \sqrt{\left(\frac{4\pi^2}{GM}\right) r^3} = 2.15 \times 10^4 \text{ s} .$$

- (b) The speed is constant (before she fires the thrusters), so  $v_o = 2\pi r/T = 1.23 \times 10^4 \text{ m/s}$ .  
(c) A two percent reduction in the previous value gives  $v = 0.98v_o = 1.20 \times 10^4 \text{ m/s}$ .  
(d) The kinetic energy is  $K = \frac{1}{2}mv^2 = 2.17 \times 10^{11} \text{ J}$ .  
(e) The potential energy is  $U = -GmM/r = -4.53 \times 10^{11} \text{ J}$ .  
(f) Adding these two results gives  $E = K + U = -2.35 \times 10^{11} \text{ J}$ .  
(g) Using Eq. 14-46, we find the semimajor axis to be

$$a = \frac{-GMm}{2E} = 4.04 \times 10^7 \text{ m} .$$

- (h) Using Kepler's law of periods for elliptical orbits (using  $a$  instead of  $r$ ) we find the new period is

$$T' = \sqrt{\left(\frac{4\pi^2}{GM}\right) a^3} = 2.03 \times 10^4 \text{ s} .$$

This is smaller than our result for part (a) by  $T - T' = 1.22 \times 10^3 \text{ s}$ .