

46. We denote the ice with subscript I and the coffee with c , respectively. Let the final temperature be T_f . The heat absorbed by the ice is $Q_I = \lambda_F m_I + m_I c_w (T_f - 0^\circ\text{C})$, and the heat given away by the coffee is $|Q_c| = m_w c_w (T_I - T_f)$. Setting $Q_I = |Q_c|$, we solve for T_f :

$$\begin{aligned} T_f &= \frac{m_w c_w T_I - \lambda_F m_I}{(m_I + m_c) c_w} \\ &= \frac{(130 \text{ g}) (4190 \text{ J/kg}\cdot^\circ\text{C}) (80.0^\circ\text{C}) - (333 \times 10^3 \text{ J/g}) (12.0 \text{ g})}{(12.0 \text{ g} + 130 \text{ g}) (4190 \text{ J/kg}\cdot^\circ\text{C})} \\ &= 66.5^\circ\text{C} . \end{aligned}$$

Note that we work in Celsius temperature, which poses no difficulty for the J/kg·K values of specific heat capacity (see Table 19-3) since a change of Kelvin temperature is numerically equal to the corresponding change on the Celsius scale. Therefore, the temperature of the coffee will cool by $|\Delta T| = 80.0^\circ\text{C} - 66.5^\circ\text{C} = 13.5^\circ\text{C}$.