

55. A small section of the distribution has charge  $dq$  is  $\lambda dx$ , where  $\lambda = 9.0 \times 10^{-9}$  C/m. Its contribution to the field at  $x_P = 4.0$  m is

$$d\vec{E} = \frac{dq}{4\pi \varepsilon_0 (x - x_P)^2}$$

pointing in the  $+x$  direction. Thus, we have

$$\vec{E} = \int_0^{3.0 \text{ m}} \frac{\lambda dx}{4\pi \varepsilon_0 (x - x_P)^2} \hat{i}$$

which becomes, using the substitution  $u = x - x_P$ ,

$$\vec{E} = \frac{\lambda}{4\pi \varepsilon_0} \int_{-4.0 \text{ m}}^{-1.0 \text{ m}} \frac{du}{u^2} \hat{i} = \frac{\lambda}{4\pi \varepsilon_0} \left( \frac{-1}{-1.0 \text{ m}} - \frac{-1}{-4.0 \text{ m}} \right) \hat{i}$$

which yields 61 N/C in the  $+x$  direction.