

43. Consider an infinitesimal segment of the loop, of length ds . The magnetic field is perpendicular to the segment, so the magnetic force on it is has magnitude $dF = iB ds$. The horizontal component of the force has magnitude $dF_h = (iB \cos \theta) ds$ and points inward toward the center of the loop. The vertical component has magnitude $dF_v = (iB \sin \theta) ds$ and points upward. Now, we sum the forces on all the segments of the loop. The horizontal component of the total force vanishes, since each segment of wire can be paired with another, diametrically opposite, segment. The horizontal components of these forces are both toward the center of the loop and thus in opposite directions. The vertical component of the total force is

$$F_v = iB \sin \theta \int ds = (iB \sin \theta) 2\pi a .$$

We note the i , B , and θ have the same value for every segment and so can be factored from the integral.