

8. The individual magnitudes  $|\vec{E}_1|$  and  $|\vec{E}_2|$  are figured from Eq. 23-3, where the absolute value signs for  $q$  are unnecessary since these charges are both positive. Whether we add the magnitudes or subtract them depends on if  $\vec{E}_1$  is in the same, or opposite, direction as  $\vec{E}_2$ . At points to the left of  $q_1$  (along the  $-x$  axis) both fields point leftward, and at points right of  $q_2$  (at  $x > d$ ) both fields point rightward; in these regions the magnitude of the net field is the sum  $|\vec{E}_1| + |\vec{E}_2|$ . In the region between the charges ( $0 < x < d$ )  $\vec{E}_1$  points rightward and  $\vec{E}_2$  points leftward, so the net field in this range is  $\vec{E}_{\text{net}} = |\vec{E}_1| - |\vec{E}_2|$  in the  $\hat{i}$  direction. Summarizing, we have

$$\vec{E}_{\text{net}} = \hat{i} \frac{1}{4\pi\epsilon_0} \begin{cases} -\frac{q_1}{x^2} - \frac{q_2}{(d+|x|)^2} & \text{for } x < 0 \\ \frac{q_1}{x^2} - \frac{q_2}{(d-x)^2} & \text{for } 0 < x < d \\ \frac{q_1}{x^2} + \frac{q_2}{(x-d)^2} & \text{for } d < x \end{cases} .$$

We note that these can be written as a single expression applying to all three regions:

$$\vec{E}_{\text{net}} = \frac{1}{4\pi\epsilon_0} \left( \frac{q_1 x}{|x|^3} + \frac{q_2 (x-d)}{|x-d|^3} \right) \hat{i} .$$

For  $-0.09 \leq x \leq 0.20$  m with  $d = 0.10$  m and charge values as specified in the problem, we find

