

67. (a) The energy per unit volume associated with the magnetic field is

$$u_B = \frac{B^2}{2\mu_0} = \frac{1}{2\mu_0} \left(\frac{\mu_0 i}{2R} \right)^2 = \frac{\mu_0 i^2}{8R^2} = \frac{(4\pi \times 10^{-7} \text{ H/m}) (10 \text{ A})^2}{8(2.5 \times 10^{-3} \text{ m}/2)^2} = 1.0 \text{ J/m}^3 .$$

(b) The electric energy density is

$$\begin{aligned} u_E &= \frac{1}{2} \varepsilon_0 E^2 = \frac{\epsilon_0}{2} (\rho J)^2 = \frac{\varepsilon_0}{2} \left(\frac{iR}{\ell} \right)^2 \\ &= \frac{1}{2} (8.85 \times 10^{-12} \text{ F/m}) [(10 \text{ A})(3.3 \Omega/10^3 \text{ m})]^2 \\ &= 4.8 \times 10^{-15} \text{ J/m}^3 . \end{aligned}$$

Here we used $J = i/A$ and $R = \rho\ell/A$ to obtain $\rho J = iR/\ell$.