

67. For a cylinder of height  $h$ , the surface area is  $A_c = 2\pi rh$ , and the area of a sphere is  $A_o = 4\pi R^2$ . The net radiative heat transfer is given by Eq. 19-40.

- (a) We estimate the surface area  $A$  of the body as that of a cylinder of height 1.8 m and radius  $r = 0.15$  m plus that of a sphere of radius  $R = 0.10$  m. Thus, we have  $A \approx A_c + A_o = 1.8 \text{ m}^2$ . The emissivity  $\varepsilon = 0.80$  is given in the problem, and the Stefan-Boltzmann constant is found in §19-11:  $\sigma = 5.67 \times 10^{-8} \text{ W/m}^2 \cdot \text{K}^4$ . The “environment” temperature is  $T_{\text{env}} = 303 \text{ K}$ , and the skin temperature is  $T = \frac{5}{9}(102 - 32) + 273 = 312 \text{ K}$ . Therefore,

$$P_{\text{net}} = \sigma \varepsilon A (T_{\text{env}}^4 - T^4) = -86 \text{ W} .$$

The corresponding sign convention is discussed in the textbook immediately after Eq. 19-40. We conclude that heat is being lost by the body at a rate of roughly 90 W.

- (b) Half the body surface area is roughly  $A = 1.8/2 = 0.9 \text{ m}^2$ . Now, with  $T_{\text{env}} = 248 \text{ K}$ , we find

$$|P_{\text{net}}| = |\sigma \varepsilon A (T_{\text{env}}^4 - T^4)| \approx 230 \text{ W} .$$

- (c) Finally, with  $T_{\text{env}} = 193 \text{ K}$  (and still with  $A = 0.9 \text{ m}^2$ ) we obtain  $|P_{\text{net}}| = 330 \text{ W}$ .