

97. (a) The energy density is

$$u_B = \frac{B_e^2}{2\mu_0} = \frac{(50 \times 10^{-6} \text{ T})^2}{2(4\pi \times 10^{-7} \text{ H/m})} = 1.0 \times 10^{-3} \text{ J/m}^3 .$$

(b) The volume of the shell of thickness h is $\mathcal{V} \approx 4\pi R_e^2 h$, where R_e is the radius of the Earth. So

$$U_B \approx \mathcal{V} u_B \approx 4\pi (6.4 \times 10^6 \text{ m})^2 (16 \times 10^3 \text{ m}) (1.0 \times 10^{-3} \text{ J/m}^3) = 8.4 \times 10^{15} \text{ J} .$$