

12. (a) From Eqs. 35-3 and 35-4, we obtain $i = pf/(p - f) = pr/(2p - r)$. Differentiating both sides with respect to time and using $v_O = -dp/dt$, we find

$$v_I = \frac{di}{dt} = \frac{d}{dt} \left(\frac{pr}{2p - r} \right) = \frac{-rv_O(2p - r) + 2v_Opr}{(2p - r)^2} = \left(\frac{r}{2p - r} \right)^2 v_O .$$

- (b) If $p = 30$ cm, we obtain

$$v_I = \left[\frac{15 \text{ cm}}{2(30 \text{ cm}) - 15 \text{ cm}} \right]^2 (5.0 \text{ cm/s}) = 0.56 \text{ cm/s} .$$

- (c) If $p = 8.0$ cm, we obtain

$$v_I = \left[\frac{15 \text{ cm}}{2(8.0 \text{ cm}) - 15 \text{ cm}} \right]^2 (5.0 \text{ cm/s}) = 1.1 \times 10^3 \text{ cm/s} .$$

- (d) If $p = 1.0$ cm, we obtain

$$v_I = \left[\frac{15 \text{ cm}}{2(1.0 \text{ cm}) - 15 \text{ cm}} \right]^2 (5.0 \text{ cm/s}) = 6.7 \text{ cm/s} .$$