

25. (a) We solve for  $B$  from  $m = B^2 q x^2 / 8V$  (see Sample Problem 29-3):

$$B = \sqrt{\frac{8Vm}{qx^2}} .$$

We evaluate this expression using  $x = 2.00$  m:

$$B = \sqrt{\frac{8(100 \times 10^3 \text{ V})(3.92 \times 10^{-25} \text{ kg})}{(3.20 \times 10^{-19} \text{ C})(2.00 \text{ m})^2}} = 0.495 \text{ T} .$$

- (b) Let  $N$  be the number of ions that are separated by the machine per unit time. The current is  $i = qN$  and the mass that is separated per unit time is  $M = mN$ , where  $m$  is the mass of a single ion.  $M$  has the value

$$M = \frac{100 \times 10^{-6} \text{ kg}}{3600 \text{ s}} = 2.78 \times 10^{-8} \text{ kg/s} .$$

Since  $N = M/m$  we have

$$i = \frac{qM}{m} = \frac{(3.20 \times 10^{-19} \text{ C})(2.78 \times 10^{-8} \text{ kg/s})}{3.92 \times 10^{-25} \text{ kg}} = 2.27 \times 10^{-2} \text{ A} .$$

- (c) Each ion deposits energy  $qV$  in the cup, so the energy deposited in time  $\Delta t$  is given by

$$E = NqV \Delta t = \frac{iqV}{q} \Delta t = iV \Delta t .$$

For  $\Delta t = 1.0$ h,

$$E = (2.27 \times 10^{-2} \text{ A})(100 \times 10^3 \text{ V})(3600 \text{ s}) = 8.17 \times 10^6 \text{ J} .$$

To obtain the second expression,  $i/q$  is substituted for  $N$ .