

12. (a) For ^{55}Mn the mass density is

$$\rho_m = \frac{M}{V} = \frac{0.055 \text{ kg/mol}}{(4\pi/3)[(1.2 \times 10^{-15} \text{ m})(55)^{1/3}]^3(6.02 \times 10^{23}/\text{mol})} = 2.3 \times 10^{17} \text{ kg/m}^3 ,$$

and for ^{209}Bi

$$\rho_m = \frac{M}{V} = \frac{0.209 \text{ kg/mol}}{(4\pi/3)[(1.2 \times 10^{-15} \text{ m})(209)^{1/3}]^3(6.02 \times 10^{23}/\text{mol})} = 2.3 \times 10^{17} \text{ kg/m}^3 .$$

(b) For ^{55}Mn the charge density is

$$\rho_q = \frac{Ze}{V} = \frac{(25)(1.6 \times 10^{-19} \text{ C})}{(4\pi/3)[(1.2 \times 10^{-15} \text{ m})(55)^{1/3}]^3} = 1.0 \times 10^{25} \text{ C/m}^3 ,$$

and for ^{209}Bi

$$\rho_q = \frac{Ze}{V} = \frac{(83)(1.6 \times 10^{-19} \text{ C})}{(4\pi/3)[(1.2 \times 10^{-15} \text{ m})(209)^{1/3}]^3} = 8.8 \times 10^{24} \text{ C/m}^3 .$$

(c) Since $V \propto r^3 = (r_0 A^{1/3})^3 \propto A$, we expect $\rho_m \propto A/V \propto A/A \approx \text{const.}$ for all nuclides, while $\rho_q \propto Z/V \propto Z/A$ should gradually decrease since $A > 2Z$ for large nuclides.