

49. (a) If the battery is switched into the circuit at $t = 0$, then the current at a later time t is given by

$$i = \frac{\mathcal{E}}{R} \left(1 - e^{-t/\tau_L} \right) ,$$

where $\tau_L = L/R$. Our goal is to find the time at which $i = 0.800\mathcal{E}/R$. This means

$$0.800 = 1 - e^{-t/\tau_L} \implies e^{-t/\tau_L} = 0.200 .$$

Taking the natural logarithm of both sides, we obtain $-(t/\tau_L) = \ln(0.200) = -1.609$. Thus

$$t = 1.609\tau_L = \frac{1.609L}{R} = \frac{1.609(6.30 \times 10^{-6} \text{ H})}{1.20 \times 10^3 \Omega} = 8.45 \times 10^{-9} \text{ s} .$$

- (b) At $t = 1.0\tau_L$ the current in the circuit is

$$i = \frac{\mathcal{E}}{R} (1 - e^{-1.0}) = \left(\frac{14.0 \text{ V}}{1.20 \times 10^3 \Omega} \right) (1 - e^{-1.0}) = 7.37 \times 10^{-3} \text{ A} .$$