

40. We imagine a spherical Gaussian surface of radius r centered at the point charge $+q$. From symmetry consideration E is the same throughout the surface, so

$$\oint \vec{E} \cdot d\vec{A} = 4\pi r^2 E = \frac{q_{\text{encl}}}{\epsilon_0} ,$$

which gives

$$E(r) = \frac{q_{\text{encl}}}{4\pi\epsilon_0 r^2} ,$$

where q_{encl} is the net charge enclosed by the Gaussian surface.

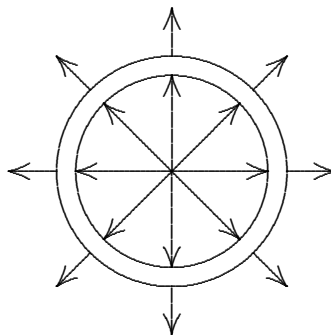
- (a) Now $a < r < b$, where $E = 0$. Thus $q_{\text{encl}} = 0$, so the charge on the inner surface of the shell is $q_i = -q$.
- (b) The shell as a whole is electrically neutral, so the outer shell must carry a charge of $q_o = +q$.
- (c) For $r < a$ $q_{\text{encl}} = +q$, so

$$E \Big|_{r < a} = \frac{q}{4\pi\epsilon_0 r^2} .$$

- (d) For $b > r > a$ $E = 0$, since this region is inside the metallic part of the shell.
- (e) For $r > b$ $q_{\text{encl}} = +q$, so

$$E \Big|_{r > a} = \frac{q}{4\pi\epsilon_0 r^2} .$$

The field lines are sketched to the right.



- (f) The net charge of the central point charge-inner surface combination is zero. Thus the electric field it produces is also zero.
- (g) The outer shell has a spherically symmetric charge distribution with a net charge $+q$. Thus the field it produces for $r > b$ is $E = q/(4\pi\epsilon_0 r^2)$.
- (h) Yes. In fact there will be a distribution of induced charges on the outer shell, as a result of a flow of positive charges toward the side of the surface that is closer to the negative point charge outside the shell.
- (i) No. The change in the charge distribution on the outer shell cancels the effect of the negative point charge. The field lines are sketched below.