

87. (Third problem in **Cluster 2**)

Our analysis of spool 2 is exactly as in the solution of part (b) of the previous problem, but with  $a_f$  replaced with  $-a_s$ . The negative sign is due to the wording of the problem (which refers to a “downward acceleration  $a_s$ ”):

$$\begin{aligned} T - Mg &= Ma_1 \\ TR_1 &= I_1\alpha_1 = I_1 \left( \frac{-a_s - a_1}{R_1} \right) \end{aligned}$$

In our analysis of spool 1, we pay close attention to signs: positive (downward)  $a_s$  corresponds to clockwise (conventionally taken to be negative) rotation of spool 1; hence,  $R_2\alpha_2 = -a_s$ . For spool 1, we therefore have

$$\sum \tau_z = -TR_2 = I_2\alpha_1 = I_2 \left( \frac{-a_s}{R_2} \right) .$$

(a) Simultaneous solution (certainly non-trivial) of these three equations yields

$$a_1 = - \frac{g}{1 + \frac{MR_1^2}{I_1} + \frac{MR_2^2}{I_2}} .$$

The problem asks for the magnitude of this (which eliminates the negative sign).

(b) This amounts to eliminating the  $\frac{MR_2^2}{I_2}$  term in the expression for  $a_1$ .