

31. (a) Let v be the final velocity of the ball-gun system. Since the total momentum of the system is conserved $mv_i = (m + M)v$. Therefore, $v = mv_i/(m + M)$.
- (b) The initial kinetic energy is $K_i = \frac{1}{2}mv_i^2$ and the final kinetic energy is $K_f = \frac{1}{2}(m + M)v^2 = \frac{1}{2}m^2v_i^2/(m + M)$. The problem indicates $\Delta E_{\text{th}} = 0$, so the difference $K_i - K_f$ must equal the energy U_s stored in the spring:

$$U_s = \frac{1}{2}mv_i^2 - \frac{1}{2}\frac{m^2v_i^2}{(m + M)} = \frac{1}{2}mv_i^2 \left(1 - \frac{m}{m + M}\right) = \frac{1}{2}mv_i^2 \frac{M}{m + M} .$$

Consequently, the fraction of the initial kinetic energy that becomes stored in the spring is $U_s/K_i = M/(m + M)$.