

19. If we write  $\vec{r} = x\hat{i} + y\hat{j} + z\hat{k}$ , then (using Eq. 3-30) we find  $\vec{r} \times \vec{F}$  is equal to

$$(yF_z - zF_y)\hat{i} + (zF_x - xF_z)\hat{j} + (xF_y - yF_x)\hat{k}.$$

- (a) In the above expression, we set (with SI units understood)  $x = 0$ ,  $y = -4$ ,  $z = 3$ ,  $F_x = 2$ ,  $F_y = 0$  and  $F_z = 0$ . Then we obtain  $\vec{\tau} = \vec{r} \times \vec{F} = (6\hat{j} + 8\hat{k}) \text{ N}\cdot\text{m}$ . This has magnitude  $\sqrt{6^2 + 8^2} = 10 \text{ N}\cdot\text{m}$  and is seen to be parallel to the  $yz$  plane. Its angle (measured counterclockwise from the  $+y$  direction) is  $\tan^{-1}(8/6) = 53^\circ$ .
- (b) In the above expression, we set  $x = 0$ ,  $y = -4$ ,  $z = 3$ ,  $F_x = 0$ ,  $F_y = 2$  and  $F_z = 4$ . Then we obtain  $\vec{\tau} = \vec{r} \times \vec{F} = -22\hat{i} \text{ N}\cdot\text{m}$ . This has magnitude  $22 \text{ N}\cdot\text{m}$  and points in the  $-x$  direction.