

88. • Using a ruler, we find the diameter of the period D to be roughly 0.5 mm. Therefore, its area is $A = \pi D^2/4 \approx 2 \times 10^{-7} \text{ m}^2$. Meanwhile, we estimate the diameter d of an air molecule to be roughly $2 \times 10^{-10} \text{ m}$ (this is “in the ballpark” of the value used in Sample Problem 20-4). So the area an air molecule covers is $a = \pi d^2/4 \approx 3 \times 10^{-20} \text{ m}^2$. Thus

$$\frac{A}{a} \approx \frac{2 \times 10^{-7}}{3 \times 10^{-20}} \approx 10^{13} .$$

This tells us that roughly 10^{13} air molecules are needed to cover the period.

- Assume that every second there are N air molecules which collide with the period. If each one of them bounces back elastically after the collision then the change in linear momentum per molecule per collision is $2mv_x$, where m is the molecular mass and v_x is the component of the molecular velocity in the direction perpendicular to the surface of the paper containing the period. We take v_x to mean the *average* velocity x -component. Thus, the pressure exerted by the air molecules on the period is

$$p = \frac{2mNv_x}{A\Delta t} \quad \text{where } \Delta t = 1 \text{ s}$$

and $v_x \approx v_{\text{rms}}/\sqrt{3}$ (see the discussion immediately preceding Eq. 20-20). Also we have $m = M/N_A$, where M is the average molar mass of the air molecules. We solve for N :

$$\begin{aligned} N &= \frac{\sqrt{3}pAN_A\Delta t}{2Mv_{\text{rms}}} = \frac{pAN_A\Delta t}{2\sqrt{MRT}} \\ &= \frac{(1.01 \times 10^5 \text{ Pa})(2 \times 10^{-7} \text{ m}^2)(6.02 \times 10^{23}/\text{mol})(1 \text{ s})}{2\sqrt{(0.028 \text{ kg/mol}) (8.31 \frac{\text{J}}{\text{mol}\cdot\text{K}}) (300 \text{ K})}} \approx 7 \times 10^{20} . \end{aligned}$$