

71. The downward force on the balloon is  $mg$  and the upward force is  $F_b = \rho_{\text{out}}Vg$ . Newton's second law (with  $m = \rho_{\text{in}}V$ ) leads to

$$\rho_{\text{out}}Vg - \rho_{\text{in}}Vg = \rho_{\text{in}}Va \implies \left( \frac{\rho_{\text{out}}}{\rho_{\text{in}}} - 1 \right) g = a .$$

The problem specifies  $\rho_{\text{out}}/\rho_{\text{in}} = 1.39$  (the outside air is cooler and thus more dense than the hot air inside the balloon). Thus, the upward acceleration is  $(1.39 - 1)(9.8) = 3.8 \text{ m/s}^2$ .