

79. (a) The transmission coefficient  $T$  for a particle of mass  $m$  and energy  $E$  that is incident on a barrier of height  $U$  and width  $L$  is given by

$$T = e^{-2kL} ,$$

where

$$k = \sqrt{\frac{8\pi^2 m(U - E)}{h^2}} .$$

For the proton,

$$\begin{aligned} k &= \sqrt{\frac{8\pi^2(1.6726 \times 10^{-27} \text{ kg})(10 \text{ MeV} - 3.0 \text{ MeV})(1.6022 \times 10^{-13} \text{ J/MeV})}{(6.6261 \times 10^{-34} \text{ J} \cdot \text{s})^2}} \\ &= 5.8082 \times 10^{14} \text{ m}^{-1} , \end{aligned}$$

$$kL = (5.8082 \times 10^{14} \text{ m}^{-1})(10 \times 10^{-15} \text{ m}) = 5.8082, \text{ and}$$

$$T = e^{-2 \times 5.8082} = 9.02 \times 10^{-6} .$$

The value of  $k$  was computed to a greater number of significant digits than usual because an exponential is quite sensitive to the value of the exponent. The mass of a deuteron is  $2.0141 \text{ u} = 3.3454 \times 10^{-27} \text{ kg}$ , so

$$\begin{aligned} k &= \sqrt{\frac{8\pi^2(3.3454 \times 10^{-27} \text{ kg})(10 \text{ MeV} - 3.0 \text{ MeV})(1.6022 \times 10^{-13} \text{ J/MeV})}{(6.6261 \times 10^{-34} \text{ J} \cdot \text{s})^2}} \\ &= 8.2143 \times 10^{14} \text{ m}^{-1} , \end{aligned}$$

$$kL = (8.2143 \times 10^{14} \text{ m}^{-1})(10 \times 10^{-15} \text{ m}) = 8.2143, \text{ and}$$

$$T = e^{-2 \times 8.2143} = 7.33 \times 10^{-8} .$$

- (b) Mechanical energy is conserved. Before the particles reach the barrier, each of them has a kinetic energy of 3.0 MeV and a potential energy of zero. After passing through the barrier, each again has a potential energy of zero, so each has a kinetic energy of 3.0 MeV.
- (c) Energy is also conserved for the reflection process. After reflection, each particle has a potential energy of zero, so each has a kinetic energy of 3.0 MeV.