

21. Consider a (thin) strip of area of height  $dy$  and width  $\ell = 0.020$  m. The strip is located at some  $0 < y < \ell$ . The element of flux through the strip is

$$d\Phi_B = B dA = (4t^2 y)(\ell dy)$$

where SI units (and 2 significant figures) are understood. To find the total flux through the square loop, we integrate:

$$\Phi_B = \int d\Phi_B = \int_0^\ell (4t^2 y \ell) dy = 2t^2 \ell^3 .$$

Thus, Faraday's law yields

$$|\mathcal{E}| = \left| \frac{d\Phi_B}{dt} \right| = 4t\ell^3 .$$

At  $t = 2.5$  s, we find the magnitude of the induced emf is  $8.0 \times 10^{-5}$  V. Its “direction” (or “sense”) is clockwise, by Lenz's law.