

25. Since  $\omega \approx \omega'$ , we may write  $T = 2\pi/\omega$  as the period and  $\omega = 1/\sqrt{LC}$  as the angular frequency. The time required for 50 cycles (with 3 significant figures understood) is

$$\begin{aligned} t &= 50T = 50 \left( \frac{2\pi}{\omega} \right) = 50 \left( 2\pi\sqrt{LC} \right) \\ &= 50 \left( 2\pi\sqrt{(220 \times 10^{-3} \text{ H})(12.0 \times 10^{-6} \text{ F})} \right) = 0.5104 \text{ s} . \end{aligned}$$

The maximum charge on the capacitor decays according to

$$q_{\max} = Qe^{-Rt/2L}$$

(this is called the *exponentially decaying amplitude* in §33-5), where  $Q$  is the charge at time  $t = 0$  (if we take  $\phi = 0$  in Eq. 33-25). Dividing by  $Q$  and taking the natural logarithm of both sides, we obtain

$$\ln\left(\frac{q_{\max}}{Q}\right) = -\frac{Rt}{2L}$$

which leads to

$$R = -\frac{2L}{t} \ln\left(\frac{q_{\max}}{Q}\right) = -\frac{2(220 \times 10^{-3} \text{ H})}{0.5104 \text{ s}} \ln(0.99) = 8.66 \times 10^{-3} \text{ } \Omega .$$