

41. (a) The root-mean-square speed is given by  $v_{\text{rms}} = \sqrt{3RT/M}$ . See Eq. 20–34. The molar mass of hydrogen is  $2.02 \times 10^{-3} \text{ kg/mol}$ , so

$$v_{\text{rms}} = \sqrt{\frac{3(8.31 \text{ J/mol} \cdot \text{K})(4000 \text{ K})}{2.02 \times 10^{-3} \text{ kg/mol}}} = 7.0 \times 10^3 \text{ m/s} .$$

- (b) When the surfaces of the spheres that represent an  $\text{H}_2$  molecule and an Ar atom are touching, the distance between their centers is the sum of their radii:  $d = r_1 + r_2 = 0.5 \times 10^{-8} \text{ cm} + 1.5 \times 10^{-8} \text{ cm} = 2.0 \times 10^{-8} \text{ cm}$ .
- (c) The argon atoms are essentially at rest so in time  $t$  the hydrogen atom collides with all the argon atoms in a cylinder of radius  $d$  and length  $vt$ , where  $v$  is its speed. That is, the number of collisions is  $\pi d^2 vt N/V$ , where  $N/V$  is the concentration of argon atoms. The number of collisions per unit time is

$$\frac{\pi d^2 v N}{V} = \pi (2.0 \times 10^{-10} \text{ m})^2 (7.0 \times 10^3 \text{ m/s}) (4.0 \times 10^{25} \text{ m}^{-3}) = 3.5 \times 10^{10} \text{ collisions/s} .$$