

6. We choose  $+y$  upward, which implies  $a > 0$  (the acceleration is upward since it represents a deceleration of his downward motion through the snow).

- (a) The maximum deceleration  $a_{\max}$  of the paratrooper (of mass  $m$  and initial speed  $v = 56$  m/s) is found from Newton's second law

$$F_{\text{snow}} - mg = ma_{\max}$$

where we require  $F_{\text{snow}} = 1.2 \times 10^5$  N. Using Eq. 2-15  $v^2 = 2a_{\max}d$ , we find the minimum depth of snow for the man to survive:

$$d = \frac{v^2}{2a_{\max}} = \frac{mv^2}{2(F_{\text{snow}} - mg)} \approx \frac{(85 \text{ kg})(56 \text{ m/s})^2}{2(1.2 \times 10^5 \text{ N})} = 1.1 \text{ m} .$$

- (b) His short trip through the snow involves a change in momentum

$$\vec{p}_f - \vec{p}_i = 0 - (85 \text{ kg})(-56 \text{ m/s})$$

(the negative value of the initial velocity is due to the fact that downward is the negative direction) which yields  $4.8 \times 10^3$  kg·m/s. By the impulse-momentum theorem, this equals the impulse due to the net force  $F_{\text{snow}} - mg$ , but since  $F_{\text{snow}} \gg mg$  we can approximate this as the impulse on him just from the snow.