

6. (a) The round-trip (discounting the time needed to “turn around”) should be one year according to the clock you are carrying (this is your proper time interval  $\Delta t_0$ ) and 1000 years according to the clocks on Earth which measure  $\Delta t$ . We solve Eq. 38-7 for  $v$  and then plug in:

$$\begin{aligned}v &= c\sqrt{1 - \left(\frac{\Delta t_0}{\Delta t}\right)^2} \\&= (299792458 \text{ m/s})\sqrt{1 - \left(\frac{1 \text{ y}}{1000 \text{ y}}\right)^2} \\&= 299792308 \text{ m/s}\end{aligned}$$

which may also be expressed as  $v = c\sqrt{1 - (1000)^{-2}} = 0.999\,999\,50c$ . The discussion in Sample Problem 38-7 dealing with these sorts of values may prove helpful for those whose calculators do not yield this answer.

- (b) The equations do not show a dependence on acceleration (or on the direction of the velocity vector), which suggests that a circular journey (with its constant magnitude centripetal acceleration) would give the same result (if the speed is the same) as the one described in the problem. A more careful argument can be given to support this, but it should be admitted that this is a fairly subtle question which has occasionally precipitated debates among professional physicists.