

53. We follow the approach shown in Sample Problem 14-7. In our system, we have  $m_1 = m_2 = M$  (the mass of our Sun,  $1.99 \times 10^{30}$  kg). From Eq. 14-37, we see that  $r = 2r_1$  in this system (so  $r_1$  is one-half the Earth-to-Sun distance  $r$ ). And Eq. 14-39 gives  $v = \pi r/T$  for the speed. Plugging these observations into Eq. 14-35 leads to

$$\frac{Gm_1m_2}{r^2} = m_1 \frac{(\pi r/T)^2}{r/2} \implies T = \sqrt{\frac{2\pi^2 r^3}{GM}} .$$

With  $r = 1.5 \times 10^{11}$  m, we obtain  $T = 2.2 \times 10^7$  s. We can express this in terms of Earth-years, by setting up a ratio:

$$T = \left( \frac{T}{1 \text{ y}} \right) (1 \text{ y}) = \left( \frac{2.2 \times 10^7 \text{ s}}{3.156 \times 10^7 \text{ s}} \right) (1 \text{ y}) = 0.71 \text{ y} .$$