

49. We denote the mass of the slab as  $m$ , its density as  $\rho$ , and volume as  $V$ . The angle of inclination is  $\theta = 26^\circ$ .

(a) The component of the weight of the slab along the incline is

$$\begin{aligned} F_1 &= mg \sin \theta = \rho V g \sin \theta \\ &= (3.2 \times 10^3 \text{ kg/m}^3)(43 \text{ m})(2.5 \text{ m})(12 \text{ m})(9.8 \text{ m/s}^2) \sin 26^\circ = 1.77 \times 10^7 \text{ N} . \end{aligned}$$

(b) The static force of friction is

$$\begin{aligned} f_s &= \mu_s N = \mu_s mg \cos \theta = \mu_s \rho V g \cos \theta \\ &= (0.39)(3.2 \times 10^3 \text{ kg/m}^3)(43 \text{ m})(2.5 \text{ m})(12 \text{ m})(9.8 \text{ m/s}^2) \cos 26^\circ = 1.42 \times 10^7 \text{ N} . \end{aligned}$$

(c) The minimum force needed from the bolts to stabilize the slab is

$$F_2 = F_1 - f_s = 1.77 \times 10^7 \text{ N} - 1.42 \times 10^7 \text{ N} = 3.5 \times 10^6 \text{ N} .$$

If the minimum number of bolts needed is  $n$ , then  $F_2/nA \leq 3.6 \times 10^8 \text{ N/m}^2$ , or

$$n \geq \frac{3.5 \times 10^6 \text{ N}}{(3.6 \times 10^8 \text{ N/m}^2)(6.4 \times 10^{-4} \text{ m}^2)} = 15.2 .$$

Thus 16 bolts are needed.