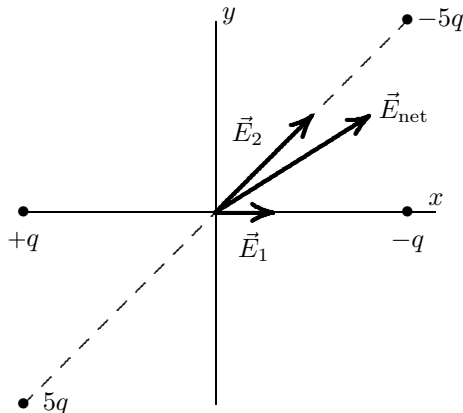


64. From symmetry, the only two pairs of charges which

produce a non-vanishing field \vec{E}_{net} are: pair 1, which is in the middle of the two vertical sides of the square (the $+q, -2q$ pair); and pair 2, the $+5q, -5q$ pair. We denote the electric fields produced by each pair as \vec{E}_1 and \vec{E}_2 , respectively. We set up a coordinate system as shown to the right, with the origin at the center of the square. Now,



$$E_1 = \frac{1}{4\pi\epsilon_0} \left(\frac{q}{d^2} + \frac{2q}{d^2} \right) = \frac{3q}{4\pi\epsilon_0 d^2} \quad \text{and} \quad E_2 = k \left[\frac{5q}{(\sqrt{2}d)^2} + \frac{5q}{(\sqrt{2}d)^2} \right] = \frac{5q}{4\pi\epsilon_0 d^2} .$$

Therefore, the components of \vec{E}_{net} are given by

$$\begin{aligned} E_x &= E_{1x} + E_{2x} = E_1 + E_2 \cos 45^\circ \\ &= \frac{3q}{4\pi\epsilon_0 d^2} + \left(\frac{5q}{4\pi\epsilon_0 d^2} \right) \cos 45^\circ = 6.536 \left(\frac{q}{4\pi\epsilon_0 d^2} \right) , \end{aligned}$$

and

$$E_y = E_{1y} + E_{2y} = E_2 \sin 45^\circ = \left(\frac{5q}{4\pi\epsilon_0 d^2} \right) \sin 45^\circ = 3.536 \left(\frac{q}{4\pi\epsilon_0 d^2} \right) .$$

Thus, the magnitude of \vec{E}_{net} is

$$E = \sqrt{E_x^2 + E_y^2} = \sqrt{(6.536)^2 + (3.536)^2} \left(\frac{q}{4\pi\epsilon_0 d^2} \right) = \frac{7.43q}{4\pi\epsilon_0 d^2} ,$$

and \vec{E}_{net} makes an angle θ with the positive x axis, where

$$\theta = \tan^{-1} \left(\frac{E_y}{E_x} \right) = \tan^{-1} \left(\frac{3.536}{6.536} \right) = 28.4^\circ .$$