

66. We consider a three-step reversible process as follows: the supercooled water drop (of mass m) starts at state 1 ($T_1 = 268\text{ K}$), moves on to state 2 (still in liquid form but at $T_2 = 273\text{ K}$), freezes to state 3 ($T_3 = T_2$), and then cools down to state 4 (in solid form, with $T_4 = T_1$). The change in entropy for each of the stages is given as follows: $\Delta S_{12} = mc_w \ln(T_2/T_1)$, $\Delta S_{23} = -mL_F/T_2$, and $\Delta S_{34} = mc_I \ln(T_4/T_3) = mc_I \ln(T_1/T_2) = -mc_I \ln(T_2/T_1)$. Thus the net entropy change for the water drop is

$$\begin{aligned}
 \Delta S &= \Delta S_{12} + \Delta S_{23} + \Delta S_{34} = m(c_w - c_I) \ln\left(\frac{T_2}{T_1}\right) - \frac{mL_F}{T_2} \\
 &= (1.00\text{ g})(4.19\text{ J/g}\cdot\text{K} - 2.22\text{ J/g}\cdot\text{K}) \ln\left(\frac{273\text{ K}}{268\text{ K}}\right) - \frac{(1.00\text{ g})(333\text{ J/g})}{273\text{ K}} \\
 &= -1.18\text{ J/K} .
 \end{aligned}$$