

60. (a) For  $r = R_p$ ,

$$\begin{aligned} v_p^2 &= GM_s \left( \frac{2}{R_p} - \frac{1}{a} \right) \\ &= (6.67 \times 10^{-11} \text{ m}^3/\text{s}^2 \cdot \text{kg}) (1.99 \times 10^{30} \text{ kg}) \left( \frac{2}{8.9 \times 10^{10} \text{ m}} - \frac{1}{2.7 \times 10^{12} \text{ m}} \right) \\ v_p &= 5.4 \times 10^4 \text{ m/s} . \end{aligned}$$

(b) For  $r = R_a$ ,

$$\begin{aligned} v_a^2 &= GM_s \left( \frac{2}{R_a} - \frac{1}{a} \right) \\ &= (6.67 \times 10^{-11} \text{ m}^3/\text{s}^2 \cdot \text{kg}) (1.99 \times 10^{30} \text{ kg}) \left( \frac{2}{5.3 \times 10^{12} \text{ m}} - \frac{1}{2.7 \times 10^{12} \text{ m}} \right) \\ v_a &= 9.6 \times 10^2 \text{ m/s} . \end{aligned}$$

(c) We appeal to angular momentum conservation:

$$L = mvr = mv_a R_a = mv_p R_p = \text{constant} \quad \implies \quad \frac{v_a}{v_p} = \frac{R_p}{R_a} .$$