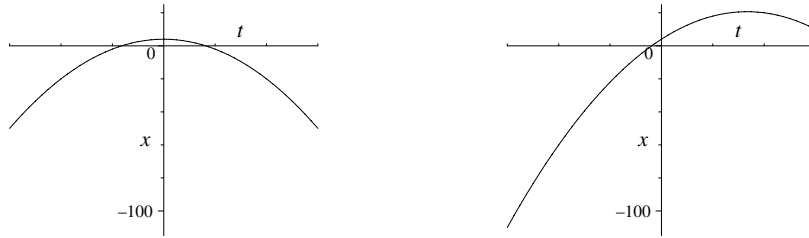


91. We use the functional notation $x(t)$, $v(t)$ and $a(t)$ in this solution, where the latter two quantities are obtained by differentiation:

$$v(t) = \frac{dx(t)}{dt} = -12t \quad \text{and} \quad a(t) = \frac{dv(t)}{dt} = -12$$

with SI units understood.

- (a) From $v(t) = 0$ we find it is (momentarily) at rest at $t = 0$.
- (b) We obtain $x(0) = 4.0$ m
- (c) Requiring $x(t) = 0$ in the expression $x(t) = 4.0 - 6.0t^2$ leads to $t = \pm 0.82$ s for the times when the particle can be found passing through the origin.
- (d) We show both the asked-for graph (on the left) as well as the “shifted” graph which is relevant to part (e). In both cases, the time axis is given by $-3 \leq t \leq 3$ (SI units understood).



- (e) We arrived at the graph on the right (shown above) by adding $20t$ to the $x(t)$ expression.
- (f) Examining where the slopes of the graphs become zero, it is clear that the shift causes the $v = 0$ point to correspond to a larger value of x (the top of the second curve shown in part (d) is higher than that of the first).