

20. (a) Plugging $R_h = 2GM_h/c^2$ into the indicated expression, we find

$$a_g = \frac{GM_h}{(1.001R_h)^2} = \frac{GM_h}{(1.001)^2 (2GM_h/c^2)^2} = \frac{c^4}{(2.002)^2 G} \frac{1}{M_h}$$

which yields $a_g = (3.02 \times 10^{43} \text{ kg} \cdot \text{m/s}^2) / M_h$.

- (b) Since M_h is in the denominator of the above result, a_g decreases as M_h increases.
(c) With $M_h = (1.55 \times 10^{12}) (1.99 \times 10^{30} \text{ kg})$, we obtain $a_g = 9.8 \text{ m/s}^2$.
(d) This part refers specifically to the very large black hole treated in the previous part. With that mass for M in Eq. 14-15, and $r = 2.002GM/c^2$, we obtain

$$da_g = -2 \frac{GM}{(2.002GM/c^2)^3} dr = -\frac{2c^6}{(2.002)^3 (GM)^2} dr$$

where $dr \rightarrow 1.70 \text{ m}$ as in the Sample Problem. This yields (in absolute value) an acceleration difference of $7.3 \times 10^{-15} \text{ m/s}^2$.

- (e) The miniscule result of the previous part implies that, in this case, any effects due to the differences of gravitational forces on the body are negligible.