

47. (a) The angular frequency is  $\omega = 8.0\pi/2 = 4.0\pi$  rad/s, so the frequency is  $f = \omega/2\pi = (4.0\pi \text{ rad/s})/2\pi = 2.0$  Hz.
- (b) The angular wave number is  $k = 2.0\pi/2 = 1.0\pi \text{ m}^{-1}$ , so the wavelength is  $\lambda = 2\pi/k = 2\pi/(1.0\pi \text{ m}^{-1}) = 2.0$  m.
- (c) The wave speed is

$$v = \lambda f = (2.0 \text{ m})(2.0 \text{ Hz}) = 4.0 \text{ m/s} .$$

- (d) We need to add two cosine functions. First convert them to sine functions using  $\cos \alpha = \sin(\alpha + \pi/2)$ , then apply Eq. 42. The steps are as follows:

$$\begin{aligned} \cos \alpha + \cos \beta &= \sin \left( \alpha + \frac{\pi}{2} \right) + \sin \left( \beta + \frac{\pi}{2} \right) = 2 \sin \left( \frac{\alpha + \beta + \pi}{2} \right) \cos \left( \frac{\alpha - \beta}{2} \right) \\ &= 2 \cos \left( \frac{\alpha + \beta}{2} \right) \cos \left( \frac{\alpha - \beta}{2} \right) \end{aligned}$$

Letting  $\alpha = kx$  and  $\beta = \omega t$ , we find

$$y_m \cos(kx + \omega t) + y_m \cos(kx - \omega t) = 2y_m \cos(kx) \cos(\omega t) .$$

Nodes occur where  $\cos(kx) = 0$  or  $kx = n\pi + \pi/2$ , where  $n$  is an integer (including zero). Since  $k = 1.0\pi \text{ m}^{-1}$ , this means  $x = (n + \frac{1}{2})(1.0 \text{ m})$ . Nodes occur at  $x = 0.50 \text{ m}$ ,  $1.5 \text{ m}$ ,  $2.5 \text{ m}$ , etc.

- (e) The displacement is a maximum where  $\cos(kx) = \pm 1$ . This means  $kx = n\pi$ , where  $n$  is an integer. Thus,  $x = n(1.0 \text{ m})$ . Maxima occur at  $x = 0$ ,  $1.0 \text{ m}$ ,  $2.0 \text{ m}$ ,  $3.0 \text{ m}$ , etc.