

17. (a) It should be emphasized that the result, given in terms of  $\sin(2\pi ft)$ , could as easily be given in terms of  $\cos(2\pi ft)$  or even  $\cos(2\pi ft + \phi)$  where  $\phi$  is a phase constant as discussed in Chapter 16. The angular position  $\theta$  of the rotating coil is measured from some reference line (or plane), and which line one chooses will affect whether the magnetic flux should be written as  $BA \cos \theta$ ,  $BA \sin \theta$  or  $BA \cos(\theta + \phi)$ . Here our choice is such that  $\Phi_B = BA \cos \theta$ . Since the coil is rotating steadily,  $\theta$  increases linearly with time. Thus,  $\theta = \omega t$  (equivalent to  $\theta = 2\pi ft$ ) if  $\theta$  is understood to be in radians (and  $\omega$  would be the angular velocity). Since the area of the rectangular coil is  $A = ab$ , Faraday's law leads to

$$\mathcal{E} = -N \frac{d(BA \cos \theta)}{dt} = -NBA \frac{d \cos(2\pi ft)}{dt} = N Bab 2\pi f \sin(2\pi ft)$$

which is the desired result, shown in the problem statement. The second way this is written ( $\mathcal{E}_0 \sin(2\pi ft)$ ) is meant to emphasize that the voltage output is sinusoidal (in its time dependence) and has an amplitude of  $\mathcal{E}_0 = 2\pi f NabB$ .

- (b) We solve  $\mathcal{E}_0 = 150 \text{ V} = 2\pi f NabB$  when  $f = 60.0 \text{ rev/s}$  and  $B = 0.500 \text{ T}$ . The three unknowns are  $N$ ,  $a$ , and  $b$  which occur in a product; thus, we obtain  $Nab = 0.796 \text{ m}^2$ . This means, for instance, that if we wanted the coil to have a square shape and consist of 50 turns, then the side length of the square would be  $a = b = 0.126 \text{ m}$ .