

25. If a nucleus contains  $Z$  protons and  $N$  neutrons, its binding energy is  $\Delta E_{\text{be}} = (Zm_H + Nm_n - m)c^2$ , where  $m_H$  is the mass of a hydrogen atom,  $m_n$  is the mass of a neutron, and  $m$  is the mass of the atom containing the nucleus of interest. If the masses are given in atomic mass units, then mass excesses are defined by  $\Delta_H = (m_H - 1)c^2$ ,  $\Delta_n = (m_n - 1)c^2$ , and  $\Delta = (m - A)c^2$ . This means  $m_H c^2 = \Delta_H + c^2$ ,  $m_n c^2 = \Delta_n + c^2$ , and  $m c^2 = \Delta + A c^2$ . Thus  $E = (Z\Delta_H + N\Delta_n - \Delta) + (Z + N - A)c^2 = Z\Delta_H + N\Delta_n - \Delta$ , where  $A = Z + N$  is used. For  $^{197}_{79}\text{Au}$ ,  $Z = 79$  and  $N = 197 - 79 = 118$ . Hence,

$$\Delta E_{\text{be}} = (79)(7.29 \text{ MeV}) + (118)(8.07 \text{ MeV}) - (-31.2 \text{ MeV}) = 1560 \text{ MeV} .$$

This means the binding energy per nucleon is  $\Delta E_{\text{ben}} = (1560 \text{ MeV})/197 = 7.92 \text{ MeV}$ .