

23. (a) The change in kinetic energy is

$$\begin{aligned}\Delta K &= \frac{1}{2}mv_f^2 - \frac{1}{2}mv_i^2 \\&= \frac{1}{2}(2100 \text{ kg}) \left((51 \text{ km/h})^2 - (41 \text{ km/h})^2 \right) \\&= 9.66 \times 10^4 \text{ kg} \cdot (\text{km/h})^2 \left((10^3 \text{ m/km})(1 \text{ h}/3600 \text{ s}) \right)^2 \\&= 7.5 \times 10^4 \text{ J} .\end{aligned}$$

(b) The magnitude of the change in velocity is

$$\begin{aligned}|\Delta \vec{v}| &= \sqrt{(-v_i)^2 + (v_f)^2} \\&= \sqrt{(-41 \text{ km/h})^2 + (51 \text{ km/h})^2} \\&= 65.4 \text{ km/h}\end{aligned}$$

so the magnitude of the change in momentum is

$$|\Delta \vec{p}| = m |\Delta \vec{v}| = (2100 \text{ kg})(65.4 \text{ km/h}) \left(\frac{1000 \text{ m/km}}{3600 \text{ s/h}} \right) = 3.8 \times 10^4 \text{ kg} \cdot \text{m/s} .$$

(c) The vector $\Delta \vec{p}$ points at an angle θ south of east, where

$$\theta = \tan^{-1} \left(\frac{v_i}{v_f} \right) = \tan^{-1} \left(\frac{41 \text{ km/h}}{51 \text{ km/h}} \right) = 39^\circ .$$