

45. (a) Since the area of a hemisphere is $2\pi r^2$ then the magnitude of the current density vector is

$$|\vec{J}| = \frac{i}{A} = \frac{I}{2\pi r^2} .$$

- (b) Eq. 27-11 yields $|\vec{E}| = \rho |\vec{J}| = \rho I / 2\pi r^2$.

- (c) Eq. 25-18 leads to

$$\Delta V = V_r - V_b = - \int_b^r \vec{E} \cdot d\vec{r} = - \int_b^r \left(\frac{\rho I}{2\pi r^2} \right) dr = \frac{\rho I}{2\pi} \left(\frac{1}{r} - \frac{1}{b} \right) .$$

- (d) Using the given values, we obtain $|\vec{J}| = \frac{100}{2\pi(10)^2} = 0.16 \text{ A/m}^2$.

- (e) Also, $|\vec{E}| = 16 \text{ V/m}$ (or 16 N/C).

- (f) With $b = 0.010 \text{ m}$, the voltage is $\Delta V = -1.6 \times 10^5 \text{ V}$.