

38. The textbook notes (in the discussion immediately after Eq. 16-7) that the acceleration amplitude is $a_m = \omega^2 x_m$, where ω is the angular frequency and $x_m = 0.0020$ m is the amplitude. Thus, $a_m = 8000 \text{ m/s}^2$ leads to $\omega = 2000 \text{ rad/s}$.

(a) Using Newton's second law with $m = 0.010$ kg, we have

$$F = ma = m(-a_m \cos(\omega t + \phi)) = -(80 \text{ N}) \cos\left(2000t - \frac{\pi}{3}\right)$$

where t is understood to be in seconds.

(b) Eq. 16-5 gives $T = 2\pi/\omega = 3.1 \times 10^{-3}$ s.

(c) The relation $v_m = \omega x_m$ can be used to solve for v_m , or we can pursue the alternate (though related) approach of energy conservation. Here we choose the latter. By Eq. 16-12, the spring constant is $k = \omega^2 m = 40000 \text{ N/m}$. Then, energy conservation leads to

$$\frac{1}{2} k x_m^2 = \frac{1}{2} m v_m^2 \implies v_m = x_m \sqrt{\frac{k}{m}} = 4.0 \text{ m/s}.$$

(d) The total energy is $\frac{1}{2} k x_m^2 = \frac{1}{2} m v_m^2 = 0.080 \text{ J}$.