

22. (a) and (b) In the region $0 < x < L$, $U_0 = 0$, so Schrödinger's equation for the region is

$$\frac{d^2\psi}{dx^2} + \frac{8\pi^2m}{h^2}E\psi = 0$$

where $E > 0$. If $\psi^2(x) = B \sin^2 kx$, then $\psi(x) = B' \sin kx$, where B' is another constant satisfying $B'^2 = B$. Thus $d^2\psi/dx^2 = -k^2 B' \sin kx = -k^2\psi(x)$ and

$$\frac{d^2\psi}{dx^2} + \frac{8\pi^2m}{h^2}E\psi = -k^2\psi + \frac{8\pi^2m}{h^2}E\psi .$$

This is zero provided that

$$k^2 = \frac{8\pi^2mE}{h^2} .$$

The quantity on the right-hand side is positive, so k is real and the proposed function satisfies Schrödinger's equation. In this case, there exists no physical restriction as to the sign of k . It can assume either positive or negative values. Thus

$$k = \pm \frac{2\pi}{h} \sqrt{2mE} .$$