

70. (a) The equation preceding Eq. 14-40 is adapted as follows:

$$\frac{m_2^3}{(m_1 + m_2)^2} = \frac{v^3 T}{2\pi G}$$

where $m_1 = 0.9M_{\text{Sun}}$ is the estimated mass of the star. With $v = 70 \text{ m/s}$ and $T = 1500 \text{ days}$ (or $1500 \times 86400 = 1.3 \times 10^8 \text{ s}$), we find

$$\frac{m_2^3}{(0.9M_{\text{Sun}} + m_2)^2} = 1.06 \times 10^{23} \text{ kg} .$$

Since $M_{\text{Sun}} \approx 2 \times 10^{30} \text{ kg}$, we find $m_2 \approx 7 \times 10^{27} \text{ kg}$. This solution may be reached in several ways (see discussion in the Sample Problem). Dividing by the mass of Jupiter (see Appendix C), we obtain $m \approx 3.7m_J$.

(b) Since $v = 2\pi r_1/T$ is the speed of the star, we find

$$r_1 = \frac{vT}{2\pi} = \frac{(70 \text{ m/s})(1.3 \times 10^8 \text{ s})}{2\pi} = 1.4 \times 10^9 \text{ m}$$

for the star's orbital radius. If r is the distance between the star and the planet, then $r_2 = r - r_1$ is the orbital radius of the planet. And r can be figured from Eq. 14-37, which leads to

$$r_2 = r_1 \left(\frac{m_1 + m_2}{m_2} - 1 \right) = r_1 \frac{m_1}{m_2} = 3.7 \times 10^{11} \text{ m} .$$

Dividing this by $1.5 \times 10^{11} \text{ m}$ (Earth's orbital radius, r_E) gives $r_2 = 2.5r_E$.