

69. (a) Their initial potential energy is  $-Gm^2/R_i$  and they started from rest, so energy conservation leads to

$$-\frac{Gm^2}{R_i} = K_{\text{total}} - \frac{Gm^2}{0.5R_i} \implies K_{\text{total}} = \frac{Gm^2}{R_i} .$$

- (b) They have equal mass, and this is being viewed in the center-of-mass frame, so their speeds are identical and their kinetic energies are the same. Thus,

$$K = \frac{1}{2}K_{\text{total}} = \frac{Gm^2}{2R_i} .$$

- (c) With  $K = \frac{1}{2}mv^2$ , we solve the above equation and find  $v = \sqrt{Gm/R_i}$ .
- (d) Their relative speed is  $2v = 2\sqrt{Gm/R_i}$ . This is the (instantaneous) rate at which the gap between them is closing.
- (e) The premise of this part is that we assume we are not moving (that is, that body  $A$  acquires no kinetic energy in the process). Thus,  $K_{\text{total}} = K_B$  and the logic of part (a) leads to  $K_B = Gm^2/R_i$ .
- (f) And  $\frac{1}{2}mv_B^2 = K_B$  yields  $v_B = \sqrt{2Gm/R_i}$ .
- (g) The answer to part (f) is incorrect, due to having ignored the accelerated motion of “our” frame (that of body  $A$ ). Our computations were therefore carried out in a noninertial frame of reference, for which the energy equations of Chapter 8 are not directly applicable.