

63. (a) We use $p_i V_i^\gamma = p_f V_f^\gamma$ to compute γ :

$$\gamma = \frac{\log(p_i/p_f)}{\log(V_f/V_i)} = \frac{\log(1.0 \text{ atm}/1.0 \times 10^5 \text{ atm})}{\log(1.0 \times 10^3 \text{ L}/1.0 \times 10^6 \text{ L})} = \frac{5}{3} .$$

Therefore the gas is monatomic.

- (b) Using the gas law in ratio form (see Sample Problem 20-1), the final temperature is

$$T_f = T_i \frac{p_f V_f}{p_i V_i} = (273 \text{ K}) \frac{(1.0 \times 10^5 \text{ atm})(1.0 \times 10^3 \text{ L})}{(1.0 \text{ atm})(1.0 \times 10^6 \text{ L})} = 2.7 \times 10^4 \text{ K} .$$

- (c) The number of moles of gas present is

$$n = \frac{p_i V_i}{RT_i} = \frac{(1.01 \times 10^5 \text{ Pa})(1.0 \times 10^3 \text{ cm}^3)}{(8.31 \frac{\text{J}}{\text{mol} \cdot \text{K}})(273 \text{ K})} = 4.5 \times 10^4 \text{ mol} .$$

- (d) The total translational energy per mole before the compression is

$$K_i = \frac{3}{2} RT_i = \frac{3}{2} \left(8.31 \frac{\text{J}}{\text{mol} \cdot \text{K}} \right) (273 \text{ K}) = 3.4 \times 10^3 \text{ J} .$$

After the compression,

$$K_f = \frac{3}{2} RT_f = \frac{3}{2} \left(8.31 \frac{\text{J}}{\text{mol} \cdot \text{K}} \right) (2.7 \times 10^4 \text{ K}) = 3.4 \times 10^5 \text{ J} .$$

- (e) Since $v_{\text{rms}}^2 \propto T$, we have

$$\frac{v_{\text{rms},i}^2}{v_{\text{rms},f}^2} = \frac{T_i}{T_f} = \frac{273 \text{ K}}{2.7 \times 10^4 \text{ K}} = 0.01 .$$