

47. (a) The mass of a carbon atom is  $(12.0 \text{ u})(1.661 \times 10^{-27} \text{ kg/u}) = 1.99 \times 10^{-26} \text{ kg}$ , so the number of carbon atoms in 1.00 kg of carbon is  $(1.00 \text{ kg})/(1.99 \times 10^{-26} \text{ kg}) = 5.02 \times 10^{25}$ . The heat of combustion per atom is  $(3.3 \times 10^7 \text{ J/kg})/(5.02 \times 10^{25} \text{ atom/kg}) = 6.58 \times 10^{-19} \text{ J/atom}$ . This is 4.11 eV/atom.
- (b) In each combustion event, two oxygen atoms combine with one carbon atom, so the total mass involved is  $2(16.0 \text{ u}) + (12.0 \text{ u}) = 44 \text{ u}$ . This is  $(44 \text{ u})(1.661 \times 10^{-27} \text{ kg/u}) = 7.31 \times 10^{-26} \text{ kg}$ . Each combustion event produces  $6.58 \times 10^{-19} \text{ J}$  so the energy produced per unit mass of reactants is  $(6.58 \times 10^{-19} \text{ J})/(7.31 \times 10^{-26} \text{ kg}) = 9.00 \times 10^6 \text{ J/kg}$ .
- (c) If the Sun were composed of the appropriate mixture of carbon and oxygen, the number of combustion events that could occur before the Sun burns out would be  $(2.0 \times 10^{30} \text{ kg})/(7.31 \times 10^{-26} \text{ kg}) = 2.74 \times 10^{55}$ . The total energy released would be  $E = (2.74 \times 10^{55})(6.58 \times 10^{-19} \text{ J}) = 1.80 \times 10^{37} \text{ J}$ . If  $P$  is the power output of the Sun, the burn time would be

$$t = \frac{E}{P} = \frac{1.80 \times 10^{37} \text{ J}}{3.9 \times 10^{26} \text{ W}} = 4.62 \times 10^{10} \text{ s} = 1460 \text{ y} .$$