

12. (a) Eq. 30-12 gives the field at the center of the large loop with $R = 1.00$ m and current $i(t)$. This is approximately the field throughout the area ($A = 2.00 \times 10^{-4}$ m²) enclosed by the small loop. Thus, with $B = \mu_0 i / 2R$ and $i(t) = i_0 + kt$ (where $i_0 = 200$ A and $k = (-200 \text{ A} - 200 \text{ A}) / 1.00 \text{ s} = -400 \text{ A/s}$), we find

$$\begin{aligned} B|_{t=0} &= \frac{\mu_0 i_0}{2R} = \frac{(4\pi \times 10^{-7} \text{ H/m})(200 \text{ A})}{2(1.00 \text{ m})} = 1.26 \times 10^{-4} \text{ T} , \\ B|_{t=0.500 \text{ s}} &= \frac{(4\pi \times 10^{-7} \text{ H/m})[200 \text{ A} - (400 \text{ A/s})(0.500 \text{ s})]}{2(1.00 \text{ m})} = 0 , \\ B|_{t=1.00 \text{ s}} &= \frac{(4\pi \times 10^{-7} \text{ H/m})[200 \text{ A} - (400 \text{ A/s})(1.00 \text{ s})]}{2(1.00 \text{ m})} = -1.26 \times 10^{-4} \text{ T} . \end{aligned}$$

- (b) Let the area of the small loop be a . Then $\Phi_B = Ba$, and Faraday's law yields

$$\begin{aligned} \mathcal{E} &= -\frac{d\Phi_B}{dt} = -\frac{d(Ba)}{dt} = -a\frac{dB}{dt} = -a\left(\frac{\Delta B}{\Delta t}\right) \\ &= -(2.00 \times 10^{-4} \text{ m}^2) \left(\frac{-1.26 \times 10^{-4} \text{ T} - 1.26 \times 10^{-4} \text{ T}}{1.00 \text{ s}} \right) = 5.04 \times 10^{-8} \text{ V} . \end{aligned}$$