

81. The weight of the air inside the balloon of volume V is $W = \rho_{\text{gas}} Vg$, and the buoyant force exerted on it is given by $F_b = \rho_{\text{air}} Vg$. Thus, we have $F_b = W + mg$, where m is the mass of the payload. we have $\rho_{\text{air}} Vg = \rho_{\text{gas}} Vg + mg$, which gives

$$V = \frac{m}{\rho_{\text{air}} - \rho_{\text{gas}}} = \frac{40 \text{ kg} + 15 \text{ kg}}{0.035 \text{ kg/m}^3 - 0.0051 \text{ kg/m}^3} = 1.8 \times 10^3 \text{ m}^3 .$$