

8. We apply the law of refraction, assuming all angles are in radians:

$$\frac{\sin \theta}{\sin \theta'} = \frac{n_w}{n_{\text{air}}} ,$$

which in our case reduces to  $\theta' \approx \theta/n_w$  (since both  $\theta$  and  $\theta'$  are small, and  $n_{\text{air}} \approx 1$ ). We refer to our figure, below. The object  $O$  is a vertical distance  $h_1$  above the water, and the water surface is a vertical distance  $h_2$  above the mirror. We are looking for a distance  $d$  (treated as a positive number) below the mirror where the image  $I$  of the object is formed. In the triangle  $OAB$

$$|AB| = h_1 \tan \theta \approx h_1 \theta ,$$

and in the triangle  $CBD$

$$|BC| = 2h_2 \tan \theta' \approx 2h_2 \theta' \approx \frac{2h_2 \theta}{n_w} .$$

Finally, in the triangle  $ACI$ , we have  $|AI| = d + h_2$ . Therefore,

$$\begin{aligned} d &= |AI| - h_2 = \frac{|AC|}{\tan \theta} - h_2 \\ &\approx \frac{|AB| + |BC|}{\theta} - h_2 \\ &= \left( \frac{h_1}{\theta} + \frac{2h_2 \theta}{n_w} \right) \frac{1}{\theta} - h_2 = h_1 + \frac{2h_2}{n_w} - h_2 \\ &= 250 \text{ cm} + \frac{2(200 \text{ cm})}{1.33} - 200 \text{ cm} = 351 \text{ cm} . \end{aligned}$$

