

34. Let  $F_o$  be the buoyant force of air exerted on the object (of mass  $m$  and volume  $V$ ), and  $F_{\text{brass}}$  be the buoyant force on the brass weights (of total mass  $m_{\text{brass}}$  and volume  $V_{\text{brass}}$ ). Then we have

$$F_o = \rho_{\text{air}} V g = \rho_{\text{air}} \left( \frac{mg}{\rho} \right)$$

and

$$F_{\text{brass}} = \rho_{\text{air}} V_{\text{brass}} g = \rho_{\text{air}} \left( \frac{m_{\text{brass}}}{\rho_{\text{brass}}} \right) g.$$

For the two arms of the balance to be in mechanical equilibrium, we require  $mg - F_o = m_{\text{brass}}g - F_{\text{brass}}$ , or

$$mg - mg \left( \frac{\rho_{\text{air}}}{\rho} \right) = m_{\text{brass}}g - m_{\text{brass}}g \left( \frac{\rho_{\text{air}}}{\rho_{\text{brass}}} \right),$$

which leads to

$$m_{\text{brass}} = \left( \frac{1 - \rho_{\text{air}}/\rho}{1 - \rho_{\text{air}}/\rho_{\text{brass}}} \right) m.$$

Therefore, the percent error in the measurement of  $m$  is

$$\begin{aligned} \frac{\Delta m}{m} &= \frac{m - m_{\text{brass}}}{m} = 1 - \frac{1 - \rho_{\text{air}}/\rho}{1 - \rho_{\text{air}}/\rho_{\text{brass}}} = \frac{\rho_{\text{air}}(1/\rho - 1/\rho_{\text{brass}})}{1 - \rho_{\text{air}}/\rho_{\text{brass}}} \\ &= \frac{0.0012(1/\rho - 1/8.0)}{1 - 0.0012/8.0} \approx 0.0012 \left( \frac{1}{\rho} - \frac{1}{8.0} \right), \end{aligned}$$

where  $\rho$  is in  $\text{g/cm}^3$ . Stating this as a *percent* error, our result is 0.12% multiplied by  $\left( \frac{1}{\rho} - \frac{1}{8.0} \right)$ .