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Giancarlo Genta • Lorenzo Morello

# The Automotive Chassis

Vol. 2: System Design



Springer

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ISBN: 978-1-4020-8673-1

e-ISBN: 978-1-4020-8675-5

Library of Congress Control Number: 2008937827

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# SYMBOLS LIST

$a$	acceleration; generic distance; distance between center of mass and front axle
$b$	generic distance; distance between center of mass and rear axle
$c$	viscous damping coefficient; specific heat
$d$	generic distance, diameter
$e$	base of natural logarithms
$f$	rolling coefficient; friction coefficient
$f_0$	rolling coefficient at zero speed
$\mathbf{f}$	force vector
$g$	gravitational acceleration
$h$	wheel deflection
$h_G$	center of mass height on the ground
$k$	stiffness
$l$	wheelbase; length
$m$	mass
$p$	pressure
$r$	radius
$s$	stopping distance, thickness
$t$	temperature; time; track
$\mathbf{u}$	displacement vector
$v$	slipping speed
$z$	teeth number
$A$	area
$C$	cornering stiffness; damping coefficient

$C_\gamma$	camber stiffness
$C_0$	cohesiveness
$E$	energy; Young modulus
$F$	force
$G$	shear modulus
$H$	thermal convection coefficient
$I$	area moment of inertia
$J$	quadratic mass moment
$K$	rolling resistance coefficient; stiffness; thermal conductivity
<b>K</b>	stiffness matrix
$M$	moment
$M_f$	braking moment
$M_m$	engine moment
$M_z$	self-aligning moment
$P$	power; tire vertical stiffness; force
$P_d$	power at the wheel
$P_m$	power at the engine
$P_n$	required power
$Q$	thermal flux
$R$	undeformed wheel radius; path radius
$R_e$	rolling radius
$R_l$	loaded radius
$S$	surface
$T$	temperature, force
$V$	speed; volume
$W$	weight
$\alpha$	sideslip angle; road side inclination; angle
$\alpha_t$	road transverse inclination angle
$\gamma$	camber angle
$\delta$	steering angle
$\epsilon$	toe-in, -out; brake efficiency; deformation
$\eta$	efficiency
$\theta$	angle; pitch angle
$\mu$	torque transmission ratio; adherence coefficient
$\mu_p$	max friction coefficient
$\mu_x$	longitudinal friction coefficient
$\mu_{x_p}$	max longitudinal friction coefficient
$\mu_{x_s}$	slip longitudinal friction coefficient
$\mu_y$	transversal friction coefficient
$\mu_{y_p}$	max transversal friction coefficient
$\mu_{y_s}$	slip transversal friction coefficient
$\nu$	speed transmission ratio; kinematic viscosity
$\rho$	density
$\sigma$	normal pressure; slip

$\tau$	transversal pressure; transmission ratio
$\phi$	angle; roll angle, friction angle
$\omega$	frequency; circular frequency
$\Phi$	diameter
$\Pi$	tire torsional stiffness
$\chi$	torsional stiffness
$\Omega$	angular speed